The impact of ocean-wave coupling on the upper ocean circulation during storm events

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Key Points:

- Impact of ocean-wave coupling on Lagrangian trajectories during storm events is assessed and analysed
- Coupled system simulates more accurate surface dynamics than uncoupled models with larger improvement on the shelf
- The Coriolis-Stokes force is the dominant wave interaction for both surface and 15 m drogued drifters

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Abstract

Many human activities rely on accurate knowledge of the sea surface dynamics. This is especially true during storm events, when wave-current interactions might represent a leading order process of the upper ocean. In this study, we assess and analyse the impact of including three wave-dependent processes in the ocean momentum equation of the Met Office North West European Shelf (NWS) ocean-wave forecasting system on the accuracy of the simulated surface circulation. The analysis is conducted using ocean currents and Stokes drift data produced by different implementations of the coupled forecasting systems to simulate the trajectories of surface (iSphere) and 15 m drogued (SVP) drifters affected by four storms selected from winter 2016. Ocean and wave simulations differ only in the degree of coupling and the skills of the Lagrangian simulations are evaluated by comparing model results against the observed drifter tracks. Results show that, during extreme events, ocean-wave coupling improves the accuracy of the surface dynamics by 4%. Improvements are larger for ocean currents on the shelf (8%) than in the open ocean (4%): this is thought to be due to the synergy between strong tidal currents and more mature decaying waves. We found that the Coriolis-Stokes forcing is the dominant wave-current interaction for both type of drifters; for iSpheres the secondary wave effect is the wave-modulated water-side stress while for SVPs the wave-dependent sea surface roughness is more important. Our results indicate that coupled ocean-wave systems may play a key role for improving the accuracy of particle transport simulations.

Plain Language Summary

Precise data on ocean surface velocities are of fundamental importance for several human activities, such as search and rescue or oil spill and plastic dispersal monitoring and control operations. Measurements of the surface dynamics are usually scarce both in time and space and typically data from numerical models are used instead. Traditionally, ocean and wave-induced currents are computed by ocean and wave models which are run independently from each other. In this study, we investigate the impact on the predicted surface circulation of using a coupled system where the ocean model receives the feedbacks of three wave-related processes. Since during storm conditions large waves can exert a strong control on the upper ocean circulation, we focus our study on extreme events. Our results show that the coupled system generally improves the accuracy of the predicted surface circulation by 4%, with improvements larger on the shelf than in the open ocean.

1 Introduction

Accurate knowledge of the ocean surface dynamics is of fundamental importance for many human activities, such as shipping, commercial fishing, recreational boating, tidal energy quantification and marine ecosystems management (e.g., *Dohan and Maximenko* [2010]). One key application of ocean surface currents data is the ability to predict the motion of objects floating on the sea surface. This is the case, for example, of search and rescue and pollutant dispersal operations (e.g., *Breivik and Allen* [2008]; *Breivik et al.* [2013]; *De Dominicis et al.* [2016]; *Jones et al.* [2016]) or monitoring activities of floating marine debris fate and accumulation (e.g., *Liubartseva et al.* [2018]). However, the precision of such simulations drastically depends on the accuracy of the wind and ocean surface currents data used to force the Lagrangian transport model. For example, *De Dominicis et al.* [2016] showed that, after 24 hr, the distance between observed and predicted drifter locations can range from 2-5 km up to 15-25 km, depending on the model data used to force the particle tracking model. Similarly, *Dagestad and Röhrs* [2019] found that, after 48 hr, drifter trajectories simulated using surface currents detected from satellite or computed by a number of ocean models with different resolution may present a separation distance from the observed tracks of about 20-25 km.

The need for more precise and detailed predictions of the ocean surface currents initiated intense development of new and more accurate observation technology and numerical mod-

elling systems. For example, worldwide operational High Frequency (HF) coastal radar networks that provide real-time 2D surface current vector maps to a variety of end users represent nowadays a standard observational application (e.g., *Abascal et al.* [2012]). Also, the Sea surface KInematics Multiscale monitoring (SKIM) satellite mission designed to provide direct global-coverage measurements of the total surface current velocity was proposed as a candidate for the European Space Agency Earth Explorer 9 competition [*Marié et al.*, 2020]. However, the spatial and temporal coverage of observational data is generally not sufficient to fulfil the practical needs of operational activities and typically, surface currents data from prognostic numerical models of the ocean, atmosphere and sea state are used instead (*Cucco et al.* [2012]; *Breivik et al.* [2013]; *Zodiatis et al.* [2016]). It is crucial therefore to continuously assess and improve the accuracy of the surface circulation fields produced by our numerical models. One approach towards improving model data quality is to implement more integrated frameworks where numerical models of different sub-components of the Earth system (i.e., atmosphere, ocean, waves, land, ice) are combined with various degrees of coupling (e.g., *Staneva et al.* [2016a]; *Clementi et al.* [2017]; *Lewis et al.* [2019a,b]).

One method to evaluate the precision of the upper ocean circulation reproduced by a numerical model is to use the surface velocities data to force a Lagrangian particle transport model and compare the simulated trajectories against those of satellite-tracked drifters. For example, *Barron et al.* [2007] applied this method to assess the impact of assimilating sea surface height on the surface circulation predicted by a U.S. Navy global ocean model. Similarly, *De Dominicis et al.* [2014] compared observed and numerical drifter tracks to evaluate the quality of surface velocities data produced by a number of different relocatable ocean models. The same methodology has also been used to investigate the physical mechanisms driving the surface transport (e.g., *Carniel et al.* [2009]; *Röhrs et al.* [2012]; *Staneva et al.* [2021]).

Sea-state dependent processes strongly affect the upper ocean dynamics. For example, ocean waves directly contribute to the surface circulation inducing a mean Stokes drift in the direction of wave propagation [*Stokes*, 1847]. Such a wave-induced drift can range from 0.6 to 1.3% of the wind speed and can be of similar magnitude as the direct wind-induced currents [*Ardhuin et al.*, 2009], significantly affecting the transport of floating objects (e.g., *Clarke and Van Gorder* [2018]; *Tamtare et al.* [2021]; *Staneva et al.* [2021]). In addition, when the Stokes drift interacts with the planetary vorticity, a new forcing appears in the ocean momentum equation which significantly affects the upper ocean Ekman spiral and therefore the direction of the surface Lagrangian transport [*Polton et al.*, 2005; *Röhrs et al.*, 2012]. Ocean waves also modulates the transfer of momentum from the atmosphere to the ocean [*Komen et al.*, 1996], modifying the upper ocean circulation (e.g., *Wu et al.* [2019]) and hence Lagrangian trajectories (e.g., *Tang et al.* [2007]). In addition, surface gravity waves directly control the vertical structure of upper ocean currents. For example, the sea surface roughness, which is the length scale controlling the turbulent mixing at the sea surface (e.g., *Gemmrich and Farmer* [1999]), is sea-state dependent (e.g., *Rascle et al.* [2008]). Also, when wind-waves break, the turbulent dissipation in the uppermost part of the oceanic boundary layer is enhanced (e.g., *Gerbi et al.* [2009]). In shallow waters, wind-waves can interact with the bottom topography, enhancing the near-bed turbulence and hence modifying the bottom drag coefficient and the currents shear (e.g., *Davies and Lawrence* [1995]). Whilst the importance of including the Stokes drift on the total upper ocean transport has been investigated extensively (e.g., *De Dominicis et al.* [2016]; *Callies et al.* [2017]; *Tamtare et al.* [2021]), the impact of wave-current interactions on the surface circulation has received less attention (e.g., *Carniel et al.* [2009]; *Röhrs et al.* [2012]), especially for cases when more wave-related processes are considered at the same time [*Staneva et al.*, 2021].

During sea storm events, large waves can have a strong control on the surface ocean dynamics, making wave-current interactions a leading order process of the uppermost part of the ocean (e.g., *Carniel et al.* [2009]; *Staneva et al.* [2016b, 2017]; *Wu et al.* [2019]). The North West European shelf (NWS) is a shallow tidal flat with significant coastal populations and infrastructures which can be affected by extremely severe sea storms (e.g *Masselink et al.* [2016];

Wei et al. [2019]), increasing the demand for accurate predictions of the surface ocean dynamics. In 2020 for example, ocean currents represented $\approx 50\%$ of the NWS total downloaded physical ocean forecast products at 1.5 km, as reported by the Copernicus Marine Environment Monitoring Service (CMEMS; see, e.g. *Le Traon et al.* [2019] for a summary of the service) service desk. CMEMS ocean and wave analysis and forecast data at 1.5 km of resolution for the NWS area are produced by the Met Office ocean and wave forecasting system [*Saulter et al.*, 2017; *Tonani et al.*, 2019]. In order to improve the accuracy of these products, since 15 December 2020 the NWS operational system uses a coupled ocean-wave modelling framework. In this system, the momentum budget equation solved by the ocean model is modified to include three wave feedbacks, namely the Coriolis-Stokes force, a wave modified momentum flux and a sea-state dependent sea surface roughness as described in *Lewis et al.* [2019a,b].

This study has three objectives:

- assess and quantify the accuracy of the surface dynamics simulated by the NWS ocean-wave coupled forecasting system in the presence of severe sea-states;
- analyse the physical mechanisms underpinning the impact of the three wave-current interactions included in the NWS ocean-wave coupled system on the upper ocean circulation during storm events; and
- identify possible future models and coupling developments which may further improve the upper ocean physics represented by the NWS coupled system.

In order to address these questions, ocean currents and Stokes drift simulations produced by five versions of the NWS forecasting system differing only in the degree of ocean-wave coupling are compared. The assessment is conducted using surface velocity data from the five experiments to simulate the Lagrangian trajectories of a number of drifters affected by four Atlantic storms that crossed the NWS during winter 2016. The skills of the Lagrangian simulations are evaluated comparing model results against the observed drifters tracks.

The paper is organised as follows. Section 2.1 details the NWS ocean-wave forecasting system (the model components as well as the coupling strategy). The Lagrangian simulations are described in Sec. 2.2.1 and the experimental design is presented in Sec. 2.2.2. Drifter observations used for the assessment are presented in Sec. 2.3. In Sec. 3 we use an idealised model to conduct some first order analysis of the impact of the three wave feedbacks included in the coupling which will help also in interpreting the 3D model results. In Sec. 4 we present and analyse our results. In Sec. 5 the physical mechanism underlying the impact of ocean-wave coupling during extreme events are discussed. Finally, in Sec. 6 we summarise our main conclusions.

2 Methods and Data

2.1 The NWS ocean-wave forecasting system

Ocean and wave data to force the Lagrangian simulations were produced using the Met Office NWS ocean and wave forecasting system, a component of CMEMS.

2.1.1 The ocean component

The ocean component of the prediction system is a Forecasting Ocean Assimilation Model (FOAM) of the NWS including an ocean model and a variational data assimilation scheme. Here, only the aspects of the FOAM system which are relevant to our study are given, while a detailed description can be found in *Tonani et al.* [2019].

The ocean model is AMM15-ocean, the eddy resolving configuration of the Atlantic Margin Model described in *Graham et al.* [2018a] and based on version 3.6 of the Nucleus for European Modelling of the Ocean (NEMO) numerical code [*Madec and NEMO-team*, 2016]. AMM15-

ocean uses a horizontal curvilinear grid with a uniform grid spacing of ≈ 1.5 *km* with a $z^* -$ *s* vertical grid with 51 levels [*Siddorn and Furner*, 2013]. Tidal dynamics are represented employing a non-linear free surface along with a time-splitting scheme that separates the fast external mode from the slow baroclinic modes. Turbulent vertical viscosity and diffusivity are computed using the Generic Length Scale (GLS) scheme (*Umlauf and Burchard* [2003]; see also Sec.2.1.3 for more details). Air-sea fluxes are computed using the CORE bulk formulae [*Large and Yeager*, 2009] using 3-hourly atmospheric fields with a resolution of $0.125° \times 0.125°$ provided by the European Centre for Medium-Range Weather Forecasts (ECMWF) operational Integrated Forecasting System (IFS).

The data assimilation component of the FOAM-AMM15 system is NEMOVAR, an incremental first guess at an appropriate time 3DVAR scheme. The Met Office implementation of NEMOVAR includes bias correction scheme for both sea surface temperature (SST) and altimeter data (see *Waters et al.* [2015]; *King et al.* [2018] for the details). FOAM-AMM15 implements NEMOVAR version 4 and uses an assimilation window of 24 h, assimilating in-situ and satellite-swath SST observations, altimeter measurements of sea level anomaly (SLA) (in regions with depth> 700 *m*) and profile observations of temperature and salinity of the water column from different sources (see *King et al.* [2018] for the details). In this paper only hourly analysis ocean data are used.

Tonani et al. [2019] showed that FOAM-AMM15 correctly reproduces the main hydrographic and dynamical features of the NWS, both in coastal and off-shelf areas. The high resolution of this system allows to resolve oceanographic structures at meanders and eddies scales, improving the model skills in reproducing important circulation patterns such as the European slope currents or the across shelf transport [*Graham et al.*, 2018b]. The circulation in the shallow, tidally dominated area has a good agreement with observations.

2.1.2 The wave component

The wave component of the NWS prediction system is AMM15-wave, a regional implementation of the WAVEWATCH III spectral wave model version 4.18 [*Tolman*, 2014] as detailed in *Saulter et al.* [2017]. The domain of AMM15-wave covers the same area of AMM15-ocean model but uses a Spherical Multiple Cell (SMC) discretization scheme [*Li*, 2012] configured to have a variable horizontal resolution ranging from 3 km across much of the domain down to 1.5 km near the coast or where the average depth is shallower than 40 m. The wave model is forced with the same 3-hourly ECMWF wind fields that are used to force AMM15-ocean. In addition, the uncoupled wave model is forced with hourly externally provided AMM15-ocean surface currents [*Palmer and Saulter*, 2016] while in the coupled implementation surface currents are exchanged via the ocean-wave coupler [*Lewis et al.*, 2019a,b]. Wave growth and dissipation terms are parameterised using the ST4 physics following *Ardhuin et al.* [2010] while nonlinear wave-wave interactions use the Discrete Interaction Approximation (DIA) package according to *Hasselmann et al.* [1985]. In this paper we use hourly analysis wave data.

2.1.3 The coupled system

Ocean-wave coupling in FOAM-AMM15 is implemented as described by *Lewis et al.* [2019a,b], considering only wave feedbacks acting on the ocean momentum budget equation.

When wave-current interactions are not taken into account, AMM15-ocean solves the incompressible, hydrostatic and Boussinesq approximated ocean momentum budget equation

$$\begin{cases} \dfrac{\partial \boldsymbol{u}_h}{\partial t} + [\boldsymbol{u} \cdot \nabla \boldsymbol{u}]_h + f\hat{\boldsymbol{z}} \times \boldsymbol{u} = -\nabla \dfrac{p}{\rho_w} + b\hat{\boldsymbol{z}} + \boldsymbol{D}_h + \dfrac{\partial}{\partial z} A_v^o \dfrac{\partial \boldsymbol{u}_h}{\partial z}, & (1a) \\[4mm] A_v^o \dfrac{\partial \boldsymbol{u}_h}{\partial z}\bigg|_{z=\eta} = \dfrac{\boldsymbol{\tau}_{atm}}{\rho_w}. & (1b) \end{cases}$$

Here the subscript h identifies a 2D vector with components in the zonal ($\hat{\mathbf{x}}$) and meridional ($\hat{\mathbf{y}}$) directions, $\mathbf{u} = \boldsymbol{u}_h + w\hat{\mathbf{z}} = (u, v, w)$ represents the Eulerian velocity vector field of slowly evolving ocean currents (with $\hat{\mathbf{z}}$ the local upward vertical unit vector), f is the Coriolis parameter, t is time, p is pressure, $b = -g\rho/\rho_w$ is the buoyancy with ρ the ocean density, ρ_w a reference ocean density and g gravity, z is the height referenced to the geoid, η is the ocean free surface, $\boldsymbol{D}_h$ represents the parameterisation of sub-grid physics in the lateral direction and $\boldsymbol{\tau}_{atm}$ is the stress exerted by the atmospheric wind on the ocean surface.

The vertical eddy viscosity A_v^o is computed by AMM15-ocean using the two-equation GLS turbulent closure model with the following surface boundary conditions (see *Reffray et al.* [2015] for the details about the NEMO implementation):

- surface enhanced mixing due to wave-breaking according to *Craig and Banner* [1994] scheme

$$\frac{A_v^o}{\sigma_k} \frac{\partial k}{\partial z}\bigg|_{z=\eta} = C_w u_{*w}^3, \tag{2}$$

where k is the turbulent kinetic energy, σ_k is the constant Schmidt number for k, C_w is the Craig and Banner coefficient equal to 100 and $u_{*w} = (|\boldsymbol{\tau}_{atm}|\rho_w^{-1})^{1/2}$ is the water-side friction velocity;

- sea surface roughness z_0 as a function of the significant wave height H_s as proposed by *Rascle et al.* [2008]:

$$z_0 = \alpha H_s, \tag{3}$$

with $\alpha = 1.3$ and

$$H_s = \frac{665}{0.85\,g} u_{*w}^2 W_{age}^{\frac{3}{2}}, \tag{4}$$

$$W_{age} = 30\tanh\left(\frac{0.6}{28\,u_{*w}}\right), \tag{5}$$

where W_{age} is an estimate of the wave age as a function of the wind stress (the superscript o in the vertical eddy viscosity A_v^o emphasizes the fact that when ocean-wave coupling is switched off the H_s is estimated by the ocean model).

Equation 1b represents the surface boundary condition traditionally used in uncoupled ocean models, where it is assumed that at the air-sea interface the air-side momentum flux (i.e., the wind stress $\boldsymbol{\tau}_{atm}$) is completely transferred into the ocean. When FOAM-AMM15 system is uncoupled, the $\boldsymbol{\tau}_{atm}$ is computed by NEMO as

$$\boldsymbol{\tau}_{atm} = \rho_a C_D |\boldsymbol{U}_{10}|\boldsymbol{U}_{10}, \tag{6}$$

where ρ_a is the air density, $\boldsymbol{U}_{10}$ is the wind velocity at 10 m and C_D is the drag coefficient computed according to *Large and Yeager* [2009].

When ocean-coupling is activated, the momentum budget equation solved by the ocean model of the FOAM-AMM15 forecasting system is modified as follows:

$$\begin{cases} \dfrac{\partial \boldsymbol{u}_h}{\partial t} + [\boldsymbol{u}\cdot\nabla\boldsymbol{u}]_h + f\hat{\mathbf{z}}\times(\boldsymbol{u}+\boldsymbol{u}_s) = -\nabla\dfrac{p}{\rho_w} + b\hat{\mathbf{z}} + \boldsymbol{D}_h + \dfrac{\partial}{\partial z}A_v^w\dfrac{\partial \boldsymbol{u}_h}{\partial z}, & \text{(7a)} \\[4mm] A_v^w\dfrac{\partial \boldsymbol{u}_h}{\partial z}\bigg|_{z=\eta} = \dfrac{\boldsymbol{\tau}_{ocn}}{\rho_w}. & \text{(7b)} \end{cases}$$

Equation 7 is a wave-averaged momentum balance equation including three wave effects acting on the mean flow (see *Lewis et al.* [2019a,b] for the details):

1. *Coriolis-Stokes forcing*

Surface waves induce a mean Lagrangian drift $\boldsymbol{u}_s$ in their direction of propagation known as Stokes drift (e.g. *Stokes* [1847]; *Phillips* [1977]). When the wave-induced drift interacts with the planetary vorticity, an additional force named Coriolis-Stokes force (CSF) appears in the wave-averaged Eulerian momentum equation [*Hasselmann*, 1970]

$$CSF \equiv f\hat{\boldsymbol{z}} \times \boldsymbol{u}_s . \tag{8}$$

In the FOAM-AMM15 coupled system, the Stokes' Drift at the surface $\boldsymbol{u}_s^0 = \boldsymbol{u}_s(t,x,y,0)$ is computed by AMM15-wave model and exchanged with AMM15-ocean model together with the H_s and the mean wave period T_{01} . Then, the 3D Stokes drift $\boldsymbol{u}_s$ is estimated by AMM15-ocean according to *Breivik et al.* [2016]

$$\boldsymbol{u}_s = \boldsymbol{u}_s^0 \left[e^{2k_p z} - \beta \sqrt{-2k_p \pi z} \, \mathrm{erfc} \left(\sqrt{2k_p z} \right) \right], \tag{9}$$

where erfc is the complementary error function, $\beta = 1$ and $k_p = \frac{8u_s^0 T_{01}}{\gamma \pi H_s^2}$ with $\gamma = 5.97$.

2. *Sea-state dependent water-side momentum flux*

The blowing of the wind on the sea surface generates both ocean waves and currents (e.g. *Csanady and Gibson* [2001]). As a result, sheared ocean currents are directly forced by the total wind stress τ_{atm} only in the case of fully developed wind-waves [*Pierson and Moskowitz*, 1964]. Most of the time, the wave field is far from being in equilibrium with the local wind, and waves are either growing, with a net influx of momentum into the wave field, or decaying, with intensified wave-breaking and a net outflux of momentum from waves into the ocean (e.g. *Komen et al.* [1996]). Thus, when surface waves are considered the water-side momentum flux $\boldsymbol{\tau}_{ocn}$ (i.e. the stress that effectively forces the ocean at the surface) is given by (e.g. *Breivik et al.* [2015])

$$\boldsymbol{\tau}_{ocn} = \boldsymbol{\tau}_{atm} - \boldsymbol{\tau}_{atw} + \boldsymbol{\tau}_{woc} , \tag{10}$$

where $\boldsymbol{\tau}_{atw}$ is the momentum flux absorbed by the waves (aka the wave-supported stress) and $\boldsymbol{\tau}_{woc}$ is the momentum flux from the wave field to the mean flow.
In the FOAM-AMM15 coupled system $\boldsymbol{\tau}_{ocn}$ is computed by AMM15-wave and directly passed to the ocean model.

3. *Sea-state dependent sea surface roughness*

FOAM-AMM15 estimates the sea surface roughness z_0 from the significant wave height H_s. When run in coupled mode, H_s is computed by AMM15-wave and exchanged with AMM15-ocean that then uses Eq.3 to compute z_0 (as indicated by the superscript w in the vertical eddy viscosity A_v^w).

2.2 Numerical experiments

2.2.1 Lagrangian simulations

Drifter trajectories were simulated using the OpenDrift Lagrangian framework [*Dagestad et al.*, 2018; *Dagestad and Röhrs*, 2019]. We used a 4th order Runge-Kutta scheme and a timestep of 3600 s to integrate the following initial value problem for the drifter position $\boldsymbol{x}(t) = (x(t), y(t))$:

$$\begin{cases} \dfrac{d\boldsymbol{x}(t)}{dt} = \boldsymbol{u}(\boldsymbol{x}(t),t) + \boldsymbol{u}_s(\boldsymbol{x}(t),t) + \boldsymbol{u}_w(\boldsymbol{x}(t),t) + \boldsymbol{u}'(\boldsymbol{x}(t),t) , & \text{(11a)} \\ \boldsymbol{x}(t_0) = \boldsymbol{x}_0 , & \text{(11b)} \end{cases}$$

where $\boldsymbol{x}_0$ is the initial drifter position at time t_0.

Two different type of drifters are simulated in this study, iSphere and Surface Velocity Program (SVP) drifters. SVP drifters are drifting buoys used since the early 1980s to measure ocean currents at a nominal depth of 15 m. They are formed by a surface float connected to a subsurface 7-m-long holey sock drogue centred at 15 m depth [*Lumpkin and Pazos*, 2009]. Such a design allows to reduce the wind slippage to less than 0.1% in 10 $m\,s^{-1}$ wind speed [*Niller et al.*, 1987], so that drogued SVP drifters are mainly transported by ocean currents and the Stokes drift at 15 m depth [*Rio*, 2012]. Conversely, iSphere drifters are half submerged spherical drifting buoy where the drifting velocity results from the combination of surface ocean and wave-induced currents and direct wind leeway [*Röhrs et al.*, 2012; *De Dominicis et al.*, 2016].

In the case of iSphere drifters, $\boldsymbol{u}(\boldsymbol{x}(t),t)$ and $\boldsymbol{u}_s(\boldsymbol{x}(t),t)$ represent turbulent Eulerian ocean currents and the Stokes drift at 0.5 m (i.e. the depth of the upper ocean model level) respectively, while $\boldsymbol{u}_w(\boldsymbol{x}(t),t)$ is the wind drag velocity parameterised as

$$\boldsymbol{u}_w(\boldsymbol{x}(t),t) = \gamma\,\boldsymbol{U}_{10}(\boldsymbol{x}(t),t)\,, \tag{12}$$

where $\boldsymbol{U}_{10}(\boldsymbol{x}(t),t)$ is the wind velocity at 10 m and $\gamma = 0.01$ in agreement with *Röhrs et al.* [2012]; *De Dominicis et al.* [2016].

When simulating SVP drifters $\boldsymbol{u}(\boldsymbol{x}(t),t)$ and $\boldsymbol{u}_s(\boldsymbol{x}(t),t)$ represent Eulerian ocean currents and the Stokes drift at 15 m while $\boldsymbol{u}_w = 0$. The Stokes drift at 0.5 and 15 m was estimated from the Stokes drift at the surface applying *Breivik et al.* [2016] parameterisation (see Eq. 9).

The term $\boldsymbol{u}'(\boldsymbol{x}(t),t) = \alpha\,R$ with $R \in [-1,1]$ represents random fluctuations in the velocity field to simulate sub-grid turbulent diffusion. We use $\alpha = 0.04\,m\,s^{-1}$ which corresponds to a horizontal eddy diffusivity K_h of $\approx 1\,m^2\,s^{-1}$ when modelling sub-grid turbulence as a random walk diffusive process (e.g. *De Dominicis et al.* [2013]), in agreement with *Jones et al.* [2020].

Quantitative assessment of the accuracy of the simulated drifter trajectories has been carried out using the *Liu and Weisberg* [2011] skill score (*ss*). This metric compares modelled and observed drifter trajectories along their path evaluating the separation of the two trajectories normalized by their total length:

$$s = \frac{\sum_{i=0}^{N} d_i(\boldsymbol{x}_s(t_i),\boldsymbol{x}_o(t_i))}{\sum_{i=0}^{N} l_{oi}(\boldsymbol{x}_o(t_0),\boldsymbol{x}_o(t_i))}\,, \tag{13}$$

where N is the total number of observed drifter positions in a given trajectory, t_i is the time at which the ith drifter position has been recorded, t_0 is the time at which the drifter has been deployed, d_i are distances between simulated $\boldsymbol{x}_s(t_i)$ and observed $\boldsymbol{x}_o(t_i)$ drifter positions at time t_i and l_{oi} is the length of the observed trajectory at time t_i.

The skill score *ss* is then defined as

$$ss = \begin{cases} 1-s & , \text{ if } s \leq 1\,, \\ 0 & , \text{ if } s > 1\,, \end{cases} \tag{14}$$

so that $ss = 1$ indicates perfectly aligned observed and modelled trajectories while $ss = 0$ identifies model simulations with no skill. Besides taking account for the separation at the end of two trajectories, the *Liu and Weisberg* [2011] skill score also acknowledges some skill for trajectories that stay together during the beginning of their path, but separate towards the end.

For each drifter simulation, 100 particles were released at the same initial location and time: the skill score of each numerical track was computed considering the path of the barycentre of the spatial distribution of particles while the standard deviation of the *ss* computed for

Storm name	Days when storm crossed NWS	Description of the impacts	Lowest recorded atm. pres. [hPa]	Max. wind gust [$m\,s^{-1}$]	Highest signif. wave height [m]	References
GERTRUDE	29-30 Jan 2016	Strong winds across Scotland and northern England; 'red' (risk to life, widespread disruption) UK national severe weather warning for wind impacts issued by the Met Office for Shetland Islands	948	≈ 45	11	*Magnusson and Bidlot* [2016]; *Met Office* [2016a]; see also Fig.1a-e
HENRY	01-02 Feb 2016	Heavy rain and very strong wind across Scotland, northern England and northern Wales; strongest gusts recorded in the Outer Hebrides and larger waves affected the northern part of the NWS.	944	≈ 40	12	*Met Office* [2016b]; see also Fig.1b-f
IMOGEN	07-08 Feb 2016	Affected the south-west of England and the south of Wales with strong winds and large waves.	962	≈ 35	10-11	*Met Office* [2016c]; see also Fig.1i-j
JAKE	01-04 Mar 2016	Relatively moderate cyclone that affected large part of Ireland, Wales and south-west England	988.9	≈ 37	9-10	*Met Office* [2016c]; see also Fig.1m-n

Table 1. Summary of meteorological and wave conditions for the four storms considered in this study.

each of the 100 particles was used as a measure of the associated uncertainty. All the simulations showed a standard deviation < 0.02, proving the robustness of our results. Sensitivity tests using 1000 or 10000 particles showed no effect on the numerical solution. Results are presented in terms of average skill scores $\overline{ss}$ and standard deviation SD, similarly to the studies of *Amemou et al.* [2020]; *Tamtare et al.* [2021]; *Staneva et al.* [2021].

2.2.2 Experimental design

Four Atlantic wind-storms affecting the NWS during winter 2016 are considered in this study. They were named by the Met Office and Met Éireann as Gertrude, Henry, Imogen and Jake. A summary of meteorological and wave conditions for each storm is shown in Fig. 1, and further details are provided in Tab. 1.

Lagrangian experiments were forced using ocean currents and Stokes drift data from five different FOAM-AMM15 ocean-wave simulations as listed in Tab.2.

TRIAL NAME	CSF	Water-side mom. flux	H_s for z_0	Simulation period	Comments
CTR	no	$\boldsymbol{\tau}_{atm}$ (Eq.16)	estimated (Eq.4)	01-01-2016 07-03-2016	*Lewis et al.* [2019b] DA experiment
CPL	yes	$\boldsymbol{\tau}_{ocn}$ (Eq.10)	comput. by wave model	01-01-2016 07-03-2016	*Lewis et al.* [2019b] CPL_DA experiment
CSF	yes	$\boldsymbol{\tau}_{atm}$ (Eq.16)	estimated (Eq.4)	23-01-2016 06-02-2016	initial condition from CTR trial
TOC	no	$\boldsymbol{\tau}_{ocn}$ (Eq.10)	estimated (Eq.4)	23-01-2016 06-02-2016	initial condition from CTR trial
WSR	no	$\boldsymbol{\tau}_{atm}$ (Eq.16)	comput. by wave model	23-01-2016 06-02-2016	initial condition from CTR trial

Table 2. Characteristics of the five ocean-wave model trial datasets used to force the Lagrangian simulations (see the text for the details).

The control trial (CTR) used the ocean and wave models in uncoupled mode (Eq. 1) while the fully coupled experiment (CPL) used all the three wave feedbacks switched on (Eq. 7).
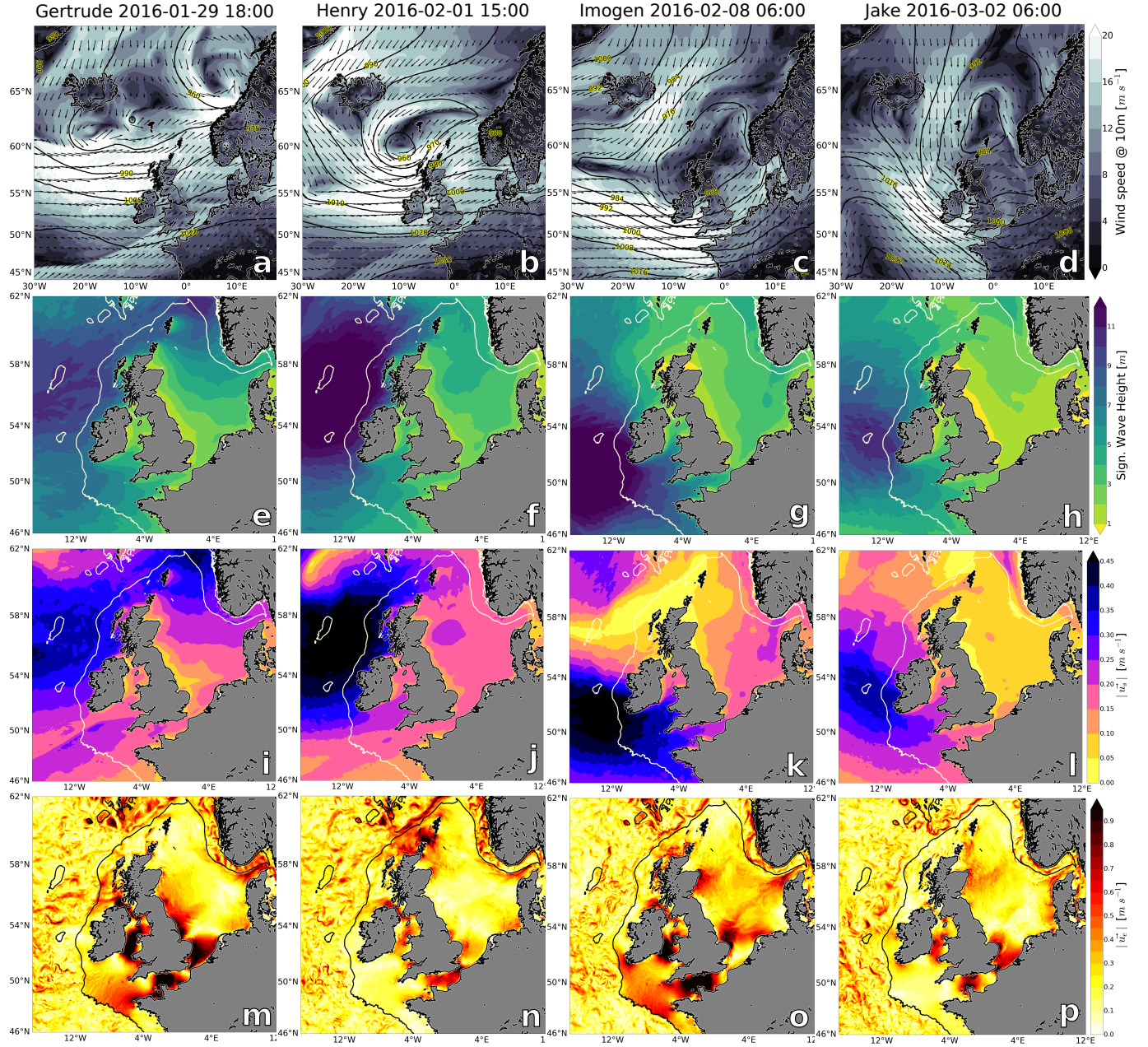
Figure 1. Snapshots of 10-m wind speed and direction and mean sea level pressure simulated by ECMWF global-scale atmosphere forecasts, used as meteorological forcing of the NWS ocean-wave system (upper row) and significant wave height (second row), Stokes drift speed (third row) and ocean currents speed (bottom row) simulated by the NWS ocean-wave forecasting system for storms Gertrude (leftmost column), Henry (second column), Imogen (third column) and Jake (rightmost column). Snapshots correspond to the H_s peak of each storm.

Both simulations were extensively validated and analysed by *Lewis et al.* [2019b] (in their work the CTR and CPL trials were named DA and CPL_DA, respectively).

Three more ocean-wave simulations were run specifically for this work to investigate the relative impact of the three wave effects considered in FOAM-AMM15 coupled system. All the three experiments used ocean and wave restarts from the CTR trial and covered the period from 23 January to 11 February 2016. The CSF trial used the coupled system with only the Coriolis-Stokes forcing activated (i.e., combining Eq.1 and Eq.8), while the TOC simulation switched on only the wave-dependent water-side momentum flux (i.e., Eq.1 replacing τ_{atm} with τ_{ocn} and using Eq.10). Finally, the WSR trial modified the stand-alone ocean momentum budget equation activating only the sea-state dependent sea surface roughness (i.e., using Eq.1 and Eq.3 with H_s computed by the wave model).

2.3 Ocean drifters observations

Drifter observations used to assess the skills of the Lagrangian simulations were retrieved from the CMEMS NWS in-situ product [*Wehde et al.*, 2021]. This dataset includes observed trajectories from i) SVP drifters equipped with a 15-m centred drogue and ii) SVP drifters which have lost their drogue. When SVP drifters lose their drogue, they become more susceptible to the wind generated slip, which increases to $\approx 1-3\%$ of the wind speed [*Pazan and Niiler*, 2001; *Rio*, 2012]. Therefore, undrogued SVP effectively behave as iSphere drifters.
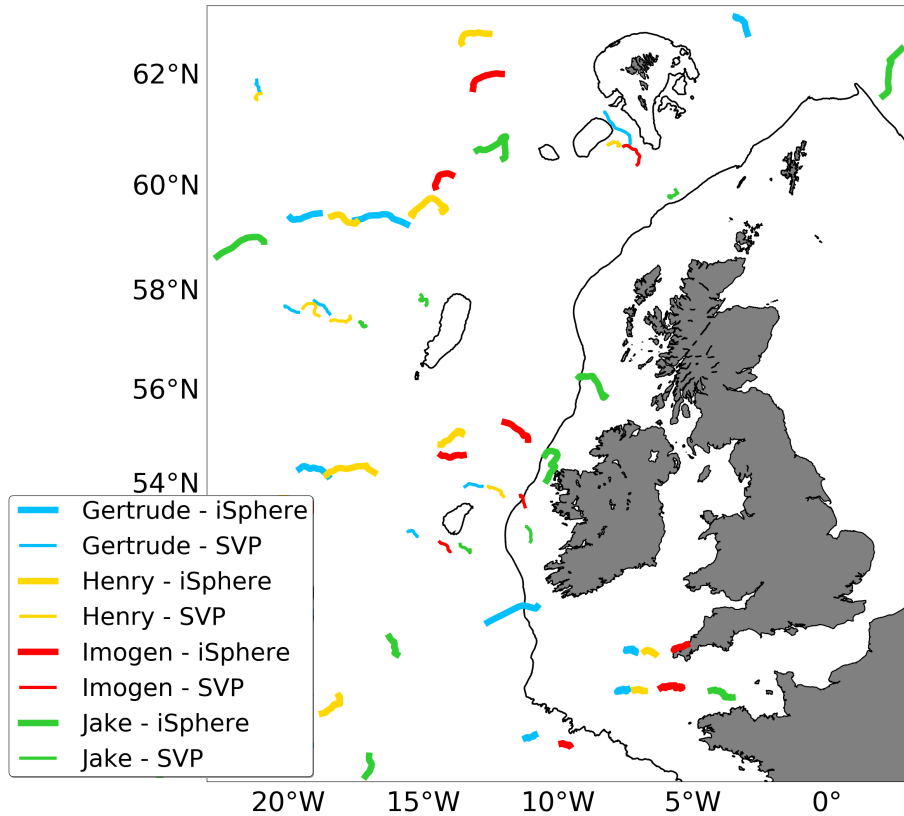

Figure 2. Drifters trajectories from the INSITU CMEMS dataset which were affected by the four winter 2016 storms considered in this study. Thick lines represent the tracks of SVP drifters which have lost their drogue (iSphere-like drifters) while thin lines identify SVP drifters with the drogue. The 200 *m* isobath is also shown in black. 14 tracks were recorded during storm Gertrude (light blue lines), 13 during storm Henry (yellow lines), 10 during storm Imogen (red lines) and 12 during storm Jake (green lines).

The CMEMS dataset is processed with the algorithm defined in Appendix A to identify the drifters trajectories which were affected by the four storms considered in this study. After processing, a total of 49 drifter trajectories are identified (see Fig.2): 18 tracks were recorded by drogued SVP drifters (hereafter SVP) while 31 belonged to undrogued SVP drifters (hereafter iSphere since they are effectively as surface iSphere drifters). In addition, 12 tracks were observed on the shelf and shelf-break (areas with depth $\leq 200\ m$) while 37 were in the open ocean. The algorithm described in Appendix A is designed to identify drifter tracks with maximum duration of 24-48 hours. This is done in order to maximise the usability of the available data set and to reduce the separation distance between observed and simulated track to an acceptable level (e.g., *De Dominicis et al.* [2014]; *Dagestad and Röhrs* [2019]).

3 The importance of coupling during extreme events

In this section we use the Ekman model [*Ekman*, 1905] to have some sense of the relative contributions of the three wave feedbacks included in the FOAM-AMM15 coupled system to the upper ocean dynamics in the presence of severe sea-states.

The Ekman model considers the simplified case of a constant vertical viscosity and therefore may not be suitable for exploring the impact of a wave dependent sea surface roughness. However, *Carniel et al.* [2009] extensively investigated the effect of the sea surface roughness and wave-breaking induced turbulence on modelling drifters trajectories during a wind storm event in the Adriatic sea. They used idealised and realistic numerical experiments to show that i) enhancing the surface roughness and/or including the injection of turbulent kinetic energy from breaking waves increases the vertical mixing of momentum reducing the shear and ultimately decreasing the upper ocean velocities; ii) drifters' trajectories in the presence of a storm are better simulated when wave breaking processes are taken into account and the sea surface roughness is enhanced.

Therefore, we consider the Ekman problem modified to include the Coriolis-Stokes forcing [*Huang*, 1979; *McWilliams et al.*, 1997; *Polton et al.*, 2005] and a sea-state dependent waterside momentum flux:

$$
\begin{cases}
f\hat{\boldsymbol{z}} \times (\boldsymbol{u}_h + \boldsymbol{u}_s) = \dfrac{\partial}{\partial z} A_v \dfrac{\partial \boldsymbol{u}_h}{\partial z}, & \text{(15a)} \\[2mm]
A_v \dfrac{\partial \boldsymbol{u}_h}{\partial z}\bigg|_{z=\eta} = \dfrac{\boldsymbol{\tau}_{ocn}}{\rho_w}, & \text{(15b)}
\end{cases}
$$

where A_v is a constant vertical viscosity coefficient and $\boldsymbol{u}_h$ becomes insignificant ($\boldsymbol{u}_h \to 0$) at great depths ($z \to -\infty$).

As shown by *Polton et al.* [2005], in this type of problem the analytical solution for the Eulerian currents results from the linear combination of three distinct terms:

$$\boldsymbol{u}_h = \boldsymbol{U}_E + \boldsymbol{U}_S + \boldsymbol{U}_{ES}, \tag{16}$$

where $\boldsymbol{U}_E$ is the wind-driven part acting on the whole Ekman depth $d_e = (2A_v/f)^{1/2}$ (i.e., the solution of the classical Ekman problem), $\boldsymbol{U}_S$ is the wave-driven Stokes component directly forced by the CSF term and decaying over the Stokes depth scale $d_s = (2k)^{-1}$ and $\boldsymbol{U}_{ES}$ is the Ekman-Stokes component which decays over the total Ekman depth scale. It is important to note that i) the Stokes component $\boldsymbol{U}_S$ is different from the Lagrangian Stokes drift $\boldsymbol{u}_s$ and ii) the Ekman-Stokes component $\boldsymbol{U}_{ES}$ arises to balance the stress exerted by the Stokes component and hence ensuring that the total velocity satisfies the wind stress surface boundary condition [*Polton et al.*, 2005].

Here, we assume a storm where the wind is blowing only in the zonal $\hat{\boldsymbol{x}}$ direction and monochromatic deep-water surface waves are propagating in the same direction. Monochromatic wave fields are chosen in order to approximate a dominant component in the wave spectrum (e.g. *McWilliams et al.* [1997]; *Sullivan et al.* [2007]). The associated Stokes drift is given
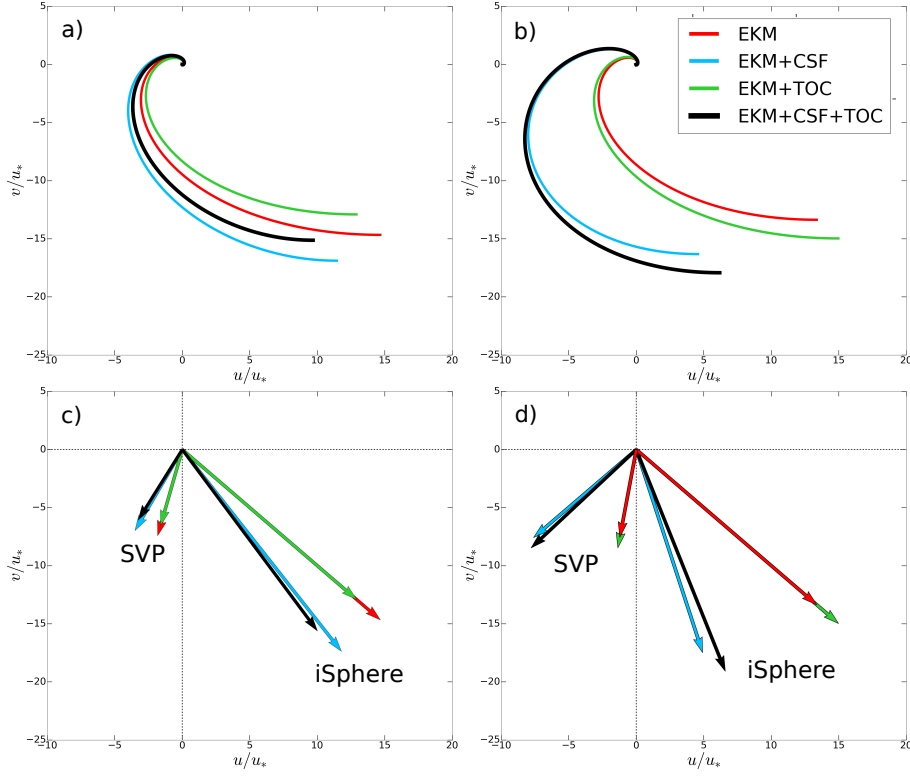
Figure 3. Solutions of the classical Ekman problem (in red) and the Ekman problem modified to include only the Coriolis-Stokes forcing (in light-blue), only a wave-dependent momentum flux (in green) and both wave feedbacks (in black). The idealised problem considers a zonal wind stress and monochromatic deep-water surface waves propagating in the same direction (see the text for the details) . The upper panels present hodographs for the growing waves (a) and the decaying waves scenario (b). Panels c) and d) present the total Eulerian transport an iSphere and a SVP drifter would experience (i.e. the Eulerian transport at the surface and in the depth-layer 10-20 m) for growing and decaying waves. All the velocities are normalised by the air-side friction velocity $\boldsymbol{u}_*$.

by $\boldsymbol{u}_s = \hat{\boldsymbol{x}}(ak)^2 c_p e^{2kz}$, where a is the wave amplitude, k the wavenumber and c_p the wave phase speed [*Phillips*, 1977]. We choose a wind speed U_{10} of 15 $m\,s^{-1}$, a Stokes drift at the surface of 0.3 $m\,s^{-1}$, $f = 10^{-4}\,s^{-1}$ and a constant vertical eddy viscosity $A_v = 1.16 \times 10^{-2}\,m^2\,s^{-1}$ [*McWilliams et al.*, 1997; *Polton et al.*, 2005], which corresponds to an Ekman depth scale d_e of $\approx 15\,m$. The drag coefficient C_D is computed according to *Smith and Banke* [1975], yielding a wind stress magnitude $\tau_{atm} = 0.43\,N\,m^{-2}$ and a water-side friction velocity u_{*w} of 0.02 $m\,s^{-1}$.

Two representative cases are explored: one for young fast growing waves and the second for more mature decaying waves. The growing waves scenario considers wind-waves with period $T = 5\,s$, inverse wave age $u_* c_p^{-1} = 0.08$ and ratio of the Ekman to the Stokes depth $d_s\, d_e^{-1}$ equal to 0.20. *Wu et al.* [2019] showed that during storm conditions the ratio $\tau_{ocn}\tau_{atm}^{-1}$ in the North Sea ranges between 0.8 and 1.8. Therefore, we parameterise the sea-state dependent water-side momentum flux during growing waves conditions as $\tau_{ocn} = 0.88 \times \tau_{atm}$. In the case of more mature decaying waves we choose $T = 11\,s$ and $u_* c_p^{-1} = 0.03$ corresponding to $d_s\, d_e^{-1} = 0.98$ and we use $\tau_{ocn} = 1.12 \times \tau_{atm}$.

Figure 3 compares the solutions for growing and decaying waves scenarios (left and right columns, respectively) of the classical Ekman problem (i.e. Eq.15 with $\boldsymbol{u}_s = 0$ and $\boldsymbol{\tau}_{ocn} = \boldsymbol{\tau}_{atm}$,

in red) against the ones of the Ekman problem modified to include i) only the CSF term (i.e. Eq.15 with $\boldsymbol{\tau}_{ocn} = \boldsymbol{\tau}_{atm}$, in light-blue), ii) only a sea-state dependent water-side momentum flux (i.e. Eq.15 with $\boldsymbol{u}_s = 0$, in green) and iii) both wave feedbacks (i.e. the complete Eq.15, in black).

In both scenarios, the CSF term changes the direction of the ageostrophic upper ocean current vectors adding an additional veering with respect to the pure Ekman solution (compare light-blue and red lines in Fig.3). However, in the case of mature decaying wind-waves the impact seems to be greater. This can be explained considering that during severe storms the wave period can grow up to $\approx 10-12\,s$ [*Toffoli and Bitner-Gregersen*, 2017], deepening the Stokes depth and resulting in $d_s\,d_e^{-1} \to 1$; in such a case, the Stokes component can have an exponentially decaying vertical contribution that is approximately of the same extent as the Ekman term. Conversely, when waves are growing and the Stokes depth is significantly shallower than the Ekman depth ($d_s\,d_e^{-1} \to 0$) the contribution of the Stokes component becomes less relevant: in this case, the Eulerian velocity results mainly from the balance between the wind-driven and the Ekman-Stokes components of the total solution (see *Polton et al.* [2005] for the details).

Using only a sea-state dependent surface stress has the effect of simply increasing (decreasing) the magnitude of the Eulerian transport with respect to the classical Ekman solution when considering decaying (growing) waves, with no effect on the ocean current directions (see red and green arrows in Fig.3).

When combining the two wave-induced effects, ageostrophic upper ocean currents of both scenarios appear to be mainly influenced by the Coriolis-Stokes acceleration and only slightly modulated by the wave-dependent surface momentum flux. In the case of growing waves, the reduced surface stress drives the weakening of the wind-driven part of the total solution while the Ekman-Stokes component is slightly enhanced, resulting in the CSF and wave-dependent surface stress acting in synergy to deflect the direction of upper ocean currents. To the contrary, when waves are decaying the increased surface stress enhances the wind-driven component of the solution while the Ekman-Stokes part is relatively weakened, with the two wave effects that in this case seems to compete.

While the wave-modified Ekman model can be a useful tool to investigate and isolate some of the mechanisms underpinning the interaction between wind-driven currents and surface wind-waves, it is an idealised model unable to give a detailed and realistic representation of the complex upper ocean dynamics, especially for regions where the tidal regime is a leading order process, as it is the case for the NWS.

4 Results

4.1 Assessment of the Lagrangian modelling approach

The motion of an object floating on the sea surface and not fully submerged can be importantly affected by the wind leeway [*Christensen et al.*, 2018]. However, it is not clear yet how to properly include this process when simulating drifter trajectories (e.g. *Breivik and Allen* [2008]; *Röhrs et al.* [2012]; *De Dominicis et al.* [2016]; *Callies et al.* [2017]; *Staneva et al.* [2021]). In addition, studies on modelling the trajectory of SVP drifters are scarce (e.g. *Kjellsson and Doos* [2012]; *Abascal et al.* [2012]; *Amemou et al.* [2020]), especially during storm conditions. Therefore the aim of this section is to assess the skills and the realism of our Lagrangian modelling approach.

The 49 drifter trajectories identified in Sec.2.3 were simulated forcing the Lagrangian model with ocean currents $\boldsymbol{u}$ and Stokes drift $\boldsymbol{u}_s$ data from the CTR and CPL trial datasets. Table 3 presents the average skill score $\overline{ss}$ and associated standard error of simulations of iSphere and SVP drifters located either on the shelf or in open ocean waters. Averaging was carried out including simulations forced with both CTR and CPL trial datasets.

DRIFTER TYPE	REGION	NUMB. OF DRIFTERS	$\overline{ss}\pm$SD no-wind	$\overline{ss}\pm$SD wind
iSphere	shelf & shelf-break	10	0.80 ± 0.09	0.42 ± 0.12
	open ocean	21	0.54 ± 0.20	0.60 ± 0.20
SVP	shelf & shelf-break	2	0.58 ± 0.14	–
	open ocean	16	0.44 ± 0.25	–

Table 3. Average skill score $\overline{ss}$ and associated standard deviation SD of numerical iSphere and SVP tracks located on the shelf and in the open ocean. In the case of iSpheres simulations the impact of using the wind leeway is also assessed. Averaging includes simulations forced with both CTR and CPL trial datasets.

The average skill score of SVP drifters is 0.46 ± 0.24, with open ocean simulations presenting a $\overline{ss}$ of 0.44 ± 0.25 and on-shelf tracks showing a $\overline{ss}$ equal to 0.58 ± 0.14. It is not clear whether this difference in skill score between deep and shallow areas might depend on the relatively low number of available drifters on the shelf - 2 against 16 in the open ocean. The visual inspection of model results might help to gain some more insights on this. Figure 4 a, b, c, d and Fig. 6 a, b, e, f present examples of open ocean and on-shelf SVP tracks simulated using $\boldsymbol{u}$ and $\boldsymbol{u}_s$ data from an uncoupled system (magenta and light-blue lines in Fig. 4 and Fig. 6, respectively) or an ocean-wave coupled run (violet and red lines in Fig. 4 and Fig. 6, respectively). Both on-shelf and open ocean numerical SVPs are consistently slower and generally deflected in comparison with the measured ones, an indication that the generally poor (< 0.5) $\overline{ss}$ of SVPs might depend on inaccuracies not directly related to the wave effects included in the coupling. For example, the systematic underestimation of SVP drifters velocity might suggest a lack of storm-related physical processes which may promote an enhanced drifter transport, such as the influence of strong storm-winds below the surface or SVP-drogued drifters surfing large storm-waves. Another possibility could be that the ocean model might underestimate the Ekman propagation of surface wind effects down into the water column (for example by overestimating the vertical shear), resulting in too slow sub-surface currents.

In the case of iSphere drifters, open ocean and on-shelf simulations present different sensitivity to the wind leeway. In deep water areas, including the wind drag velocity ($\boldsymbol{u}_w > 0$) in the Lagrangian transport equation 11a generally allows to reduce the underestimation of the observed trajectories (see Fig.4e,h), improving the average skill score from 0.54 ± 0.20 to 0.60 ± 0.20. On the other hand, including the wind leeway in coastal areas generates too large drifter velocities causing overshooting of the final observed locations (e.g. Fig.4f,g) while using $\boldsymbol{u}_w = 0$ (i.e. no wind drag velocity) significantly improves the simulations' skill increasing the $\overline{ss}$ from 0.42 ± 0.12 to 0.80 ± 0.09. However, iSphere simulations generally present a good ($>$ 0.5) average skill score (the $\overline{ss}$ with the wind leeway is 0.58 ± 0.22 while the one without is 0.61 ± 0.21), suggesting that ocean and wave-induced currents may represent the main forcing for the surface Lagrangian transport.

In order to better understand the reason behind the negative impact of the wind leeway in shelf areas, the accuracy of surface ocean currents, Stokes drift and wind velocities used to force the Lagrangian model was assessed against on-shelf independent observations.

Available wind speed measurements during the four storms were recorded by two wave buoys of the World Meteorological Organisation - International Oceanographic Commission (WMO-IOC) Joint Commission for Oceanography Marine Meteorology's operational Wave Forecast Verification Scheme (JCOMM-WFVS, *Bidlot et al.* [2007]), which includes quality controlled in-situ observations sampled on a 6-hourly basis. One buoy was located near the shelf-break off North Ireland coast while the other was off Land's End coast (respectively buoy A and B in Fig.5a). Figures 5b and 5c compare time-series of wind speed measurements during the four storms at buoy A and B, respectively, with time-series of 3-hourly ECMWF wind
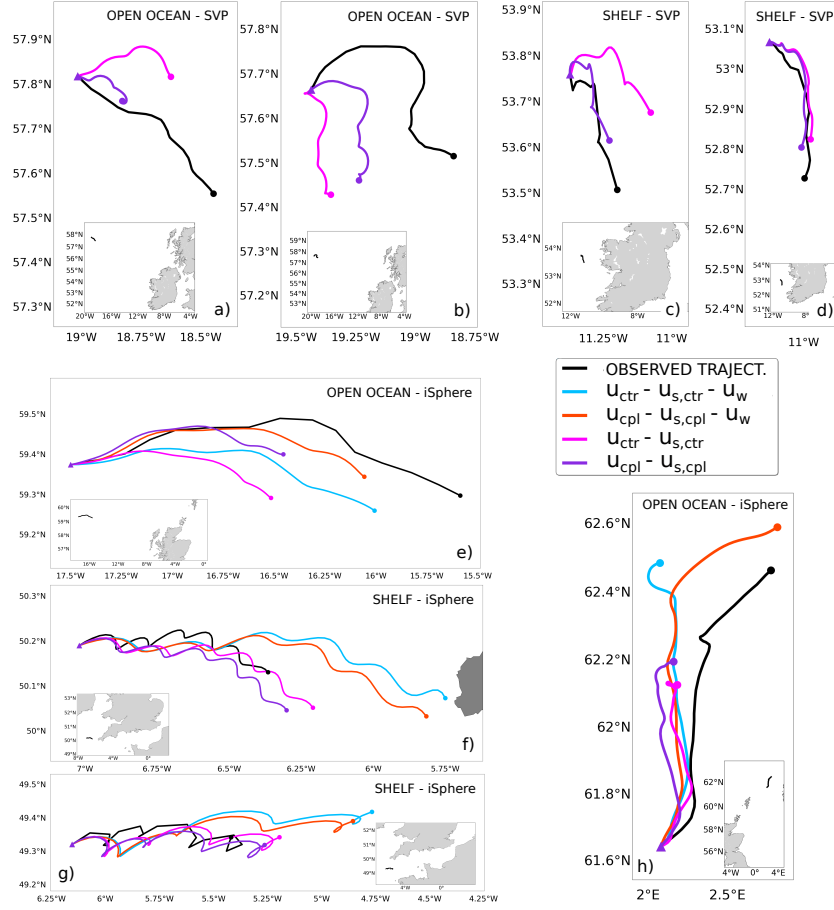
Figure 4. Examples of simulations of SVP and iSphere drifters located open ocean and on the shelf during the four storms considered in this study. Observed drifter tracks are shown in black. Drifter trajectories simulated forcing the Lagrangian model only with the ocean surface dynamics ($u + u_s$) from CTR and CPL trials are shown in magenta and violet, respectively. Tracks simulated using the wind leeway combined with surface currents and wave-induced transport ($u + u_s + u_w$) from CTR and CPL runs are presented in light-blue and red, respectively.

speed interpolated at the same locations. At buoy A, modelled wind speeds seem to overestimate the observations, with a BIAS of 1.49 $m\,s^{-1}$ and a RMSE of 2.38 $m\,s^{-1}$, while at buoy B ECMWF wind speeds are slower than the measured ones, with BIAS$= -1.32$ $m\,s^{-1}$ and RMSE$= 2.1$ $m\,s^{-1}$. It is worth noting that for both buoys there is no metadata to confirm whether or how these data are corrected to a 10 m wind speed. Consequently, quantitative errors may have significant uncertainties.

HF-radar currents measured in an area off the north coast of the south-west of England (see rectangle in Fig.5a) were used to assess the accuracy of on-shelf surface ocean currents and Stokes drift during the four storms. The Wave Hub HF radar system is a phased-array WEllen RAdar (WERA) system which has been measuring waves and currents off the north coast of Cornwall since 2011 [*Lopez and Conley*, 2019]. Comparisons between radar surface current measurements and ADCP derived near surface measurements typically exhibit a bias less than 0.03 $m\,s^{-1}$ and RMSE less than 0.10 $m\,s^{-1}$ [*Lopez*, 2017]. Whilst radar-derived currents are extensively used for oceanographic studies in coastal regions (e.g. *Paduan and Washburn* [2013]; *Lopez et al.* [2020]), whether they include either the entire wave-induced Stokes drift, part of it or none of it is still an open question (e.g. *Isern-Fontanet et al.* [2017]). After sensitivity tests,
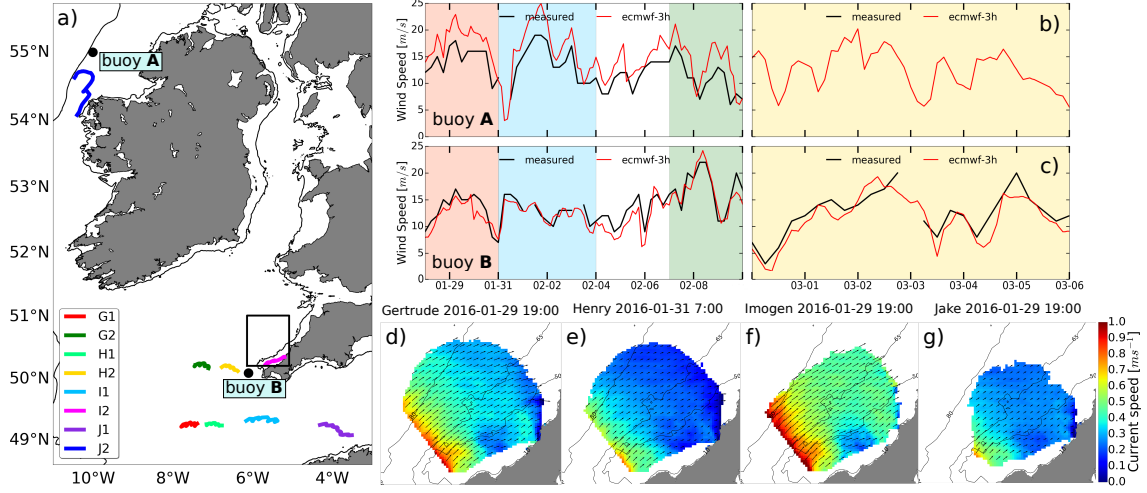
Figure 5. **a)** On-shelf iSphere drifter trajectories observed during storms Gertrude (G1, G2), Henry (H1, H2), Imogen (I1, I2) and Jake (J1, J2) together with the location of buoys A and B. The area covered by HF-radar measurements is also shown with the rectangle in black. **b-c)** Time-series of wind speed measured (black) during the four storms at buoy A and B, respectively, against time-series of 3-hourly ECMWF wind speed interpolated at the same locations (red). Storm-windows are identified by coloured shadows: pink is for Gertrude, light-blue for Henry, green for Imogen and yellow for Jake. **d-g)** Snapshots of HF-radar surface currents maps detected during the four storms. Only HF-radar measurements with an associated error < 0.09 $m\,s^{-1}$ are shown.

it was decided to compare HF-radar derived surface currents against the linear combination of model ocean currents and Stokes drift. The analysis considered only HF-radar currents with an associated error $< 0.09\ m\,s^{-1}$ (see Fig.5d,e,f,g for snapshots of radar derived surface currents during the four storms with such an accuracy) and included the computation of spatially averaged BIAS, RMSE and veering angles θ [*Kundu*, 1976] for each storm. Table 4 presents storm averaged metrics of surface ocean currents and Stokes drift from CTR and CPL trials. In general, the surface dynamics simulated by the CPL run presents improved accuracy (total metrics are BIAS $= -0.04\ m\,s^{-1}$, RMSE $= 0.10\ m\,s^{-1}$ and $\theta = -0.6°$) in comparison to the one of the CTR experiment (BIAS $= -0.09\ m\,s^{-1}$, RMSE $= 0.17\ m\,s^{-1}$ and $\theta = 3.35°$).

Metric	Gertrude CTR	Gertrude CPL	Henry CTR	Henry CPL	Imogen CTR	Imogen CPL	Jake CTR	Jake CPL
BIAS [$m\,s^{-1}$]	-0.09	-0.05	-0.09	-0.03	-0.10	-0.05	-0.07	-0.02
RMSE [$m\,s^{-1}$]	0.18	0.10	0.16	0.08	0.21	0.13	0.14	0.08
θ [°]	-0.60	-1.10	9.75	3.20	-1.62	-2.60	4.61	-1.80

Table 4. Spatially and storm averaged BIAS, RMSE and veering angles θ of linearly combined surface ocean currents and Stokes drift from CTR and CPL trials with respect to HF-radar detected surface currents. A positive θ means that the vector sum $\boldsymbol{u} + \boldsymbol{u}_s$ veers clockwise with respect to HF-radar currents.

Assessment against independent observations showed that modelled wind data might be affected by large inaccuracies in shelf and coastal areas. This is in agreement with other studies. For example, a recent work by *Christakos et al.* [2020] investigated the relationship between the quality of wind fields in the proximity of a coast with complex orography and the mesh size of the atmospheric model. They found that, especially during extreme wind events,

a finer grid can better capture local wind phenomena but leads to an overestimation of the wind speed while a coarser mesh systematically simulates weaker winds along the coast. Also, *Staneva et al.* [2021] noted that adding the contribution of windage in coastal areas might lead to over-parameterization. Therefore, in this study the trajectories of on-shelf iSphere drifters were simulated not taking into account the leeway of the wind (i.e. using $u_w = 0$).

4.2 The impact of ocean-wave coupling

In this section we evaluate and analyse the impact of the three wave feedbacks included in the FOAM-AMM15 coupled system on the upper ocean dynamics during storm conditions.

Four different Lagrangian experiments were conducted (see Tab.5) forcing OpenDrift model with ocean and wave data from CTR and CPL trial datasets to simulate the 49 drifter tracks identified in Sec.2.3. Two experiments used u and u_s data extracted from the same trial dataset and, consequently, they were named as $U_{ctr}S_{ctr}$ and $U_{cpl}S_{cpl}$, respectively. The other two experiments were named $U_{ctr}S_{cpl}$ and $U_{cpl}S_{ctr}$ since they forced the Lagrangian simulations combining u data from one dataset with u_s data from the other one. In the case of open ocean iSpheres, the Lagrangian simulations were forced using also the wind leeway.

DRIFTER TYPE	REGION	NUMB. OF DRIFTERS	$\overline{ss} \pm$ SD			
			$U_{ctr}S_{ctr}$	$U_{cpl}S_{cpl}$	$U_{ctr}S_{cpl}$	$U_{cpl}S_{ctr}$
iSphere	shelf & shelf-break	10	0.76 ± 0.09	0.82 ± 0.09	0.75 ± 0.10	0.81 ± 0.09
	open ocean	21	0.57 ± 0.21	0.60 ± 0.19	0.55 ± 0.21	0.59 ± 0.20
SVP	shelf & shelf-break	2	0.50 ± 0.16	0.66 ± 0.05	0.47 ± 0.16	0.69 ± 0.05
	open ocean	16	0.43 ± 0.23	0.46 ± 0.27	0.42 ± 0.23	0.46 ± 0.26

Table 5. Average skill score $\overline{ss}$ and standard deviation SD of open ocean and on-shelf iSphere and SVP drifters for the four Lagrangian experiments. $U_{ctr}S_{ctr}$ and $U_{cpl}S_{cpl}$ simulations use ocean currents and Stokes drift from CTR and CPL trials, respectively; $U_{ctr}S_{cpl}$ experiment uses currents from the CTR trial and the Stokes drift from the CPL dataset while $U_{cpl}S_{ctr}$ uses currents from the CPL dataset and the Stokes drift from the CTR trial.

Table 5 presents the average skill score $\overline{ss}$ and standard deviation SD of iSphere and SVP drifters on-shelf and in the open ocean for the four Lagrangian experiments. The comparison between the average skill scores of $U_{ctr}S_{ctr}$ and $U_{cpl}S_{cpl}$ experiments show that on average, during severe storm events, ocean-wave coupling is able to improve the accuracy of the predicted surface dynamics by 4% (from 0.56 ± 0.23 to 0.60 ± 0.24) . Improvements for specific drifters can reach values of $\approx 15 - 20\%$.

In addition, numerical results show that during storm events ocean-wave coupling seems to have a similar impact on both type of drifters, improving the $\overline{ss}$ of surface iSpheres from 0.63 ± 0.20 to 0.67 ± 0.19 and the one of 15 m drogued SVPs from 0.43 ± 0.22 to 0.48 ± 0.26. Generally, the three wave feedbacks included in the FOAM-AMM15 coupled system predominantly act at the sea surface and significantly decay with the depth. However, our results appear to indicate that during severe sea states their effect may propagate below the surface and affects also the sub-surface ocean dynamics.

In the following two sections we deepen our analysis investigating the relative impact of coupling on ocean currents and Stokes drift.
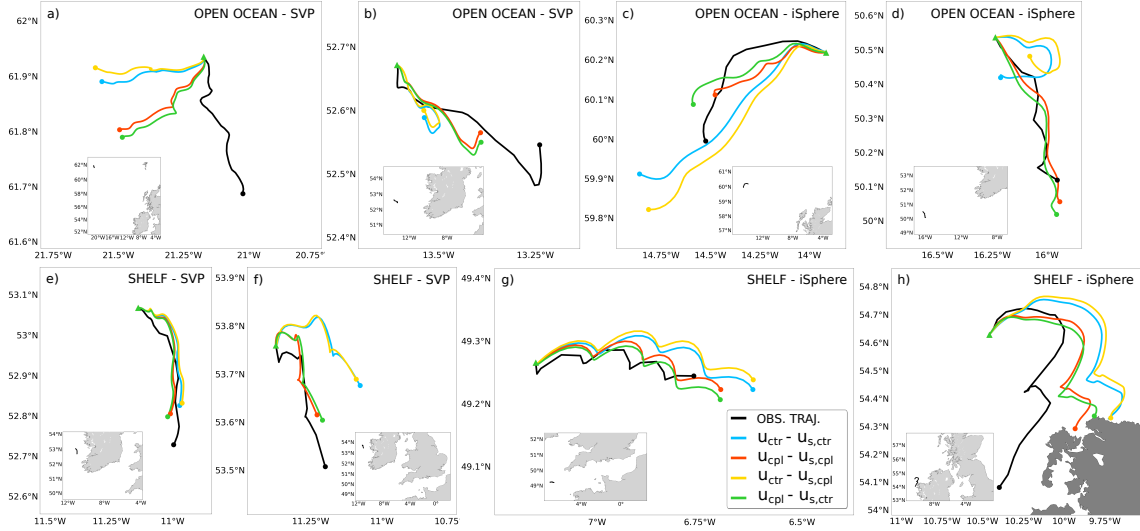
Figure 6. Examples of SVP and iSphere simulations located in the open ocean and on the shelf during the four storms considered in this study. Observed drifter tracks are shown in black. Drifter trajectories simulated forcing the Lagrangian model with the ocean surface dynamics (u and u_s) from CTR and CPL trials are shown in light-blue ($U_{ctr}S_{ctr}$) and red ($U_{cpl}S_{cpl}$), respectively. Tracks simulated using ocean currents from CTR trial and Stokes drift from CPL dataset are shown in yellow ($U_{ctr}S_{cpl}$); simulations using ocean currents from CPL trial and Stokes drift from CTR dataset are shown in yellow ($U_{cpl}S_{ctr}$). Open ocean iSphere simulations use also the wind leeway $u_w > 0$.

4.2.1 *The effect of coupling on the ocean currents*

The impact of ocean-wave coupling on the accuracy of the upper ocean currents can be evaluated and quantified considering Lagrangian experiments applying the same Stokes drift forcing but using different data for the currents, i.e. comparing $U_{ctr}S_{ctr}$ against $U_{cpl}S_{ctr}$ and $U_{ctr}S_{cpl}$ against $U_{cpl}S_{cpl}$, respectively.

Figure 6 shows that, as expected, ocean-wave coupling has the larger impact on the ocean currents (compare light-blue against green and yellow against red trajectories). In addition, results reported in Table 5 reveal that using currents from a coupled system allows the improvement of the $\overline{ss}$ by 8% in shelf areas (from 0.71 ± 0.14 to 0.79 ± 0.09) and 4% in the open ocean (from 0.50 ± 0.23 to 0.54 ± 0.24). The greater improvement on the shelf is probably the consequence of multiple factors. Firstly, there is an under-sampling affecting on-shelf regions - 12 tracks against 37. Then, including the wind leeway in the forcing of off-shelf simulations could result in masking the effect of ocean-wave coupling, making improvements less notable. Finally, the interaction between waves, tides, and wind-driven circulation is a leading order process on the shelf, where ocean waves increase their amplitude to conserve energy flux and tidal currents are larger than in the open ocean (e.g. *Huthnance* [1981]; *Simpson* [1998]; *Valiente et al.* [2019]).

In order to better understand the mechanisms behind the difference in skill score between shelf and open ocean simulations, we continue our analysis computing a number of simulated diagnostics along the 49 observed trajectories using model outputs from CTR and CPL trial datasets.

Figure 7a compares the track-averaged magnitude of current velocities $\langle u \rangle$ and Stokes drift $\langle u_s \rangle$ at the surface (iSpheres) or 15 m (SVPs). In the case of SVP drifters, ocean currents are consistently larger than the Stokes drift, with values from ≈ 2 to ≈ 10 times larger, in agree-
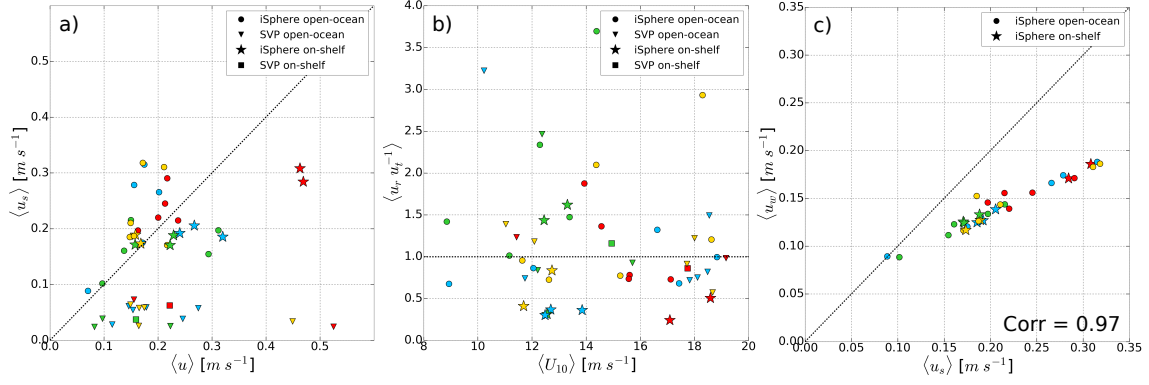
Figure 7. Track-averaged magnitude of a) current velocities $\langle u \rangle$ and Stokes drift $\langle u_s \rangle$, b) ratio between residual and tidal currents $\langle u_r \tilde{u}^{-1} \rangle$ and wind speed $\langle U_{10} \rangle$, c) surface Stokes drift and wind leeway for open ocean and on-shelf surface (iSpheres) or 15 m (SVPs) drifters.

ment with the strong vertical shear characterising the Stokes drift (e.g. *Breivik et al.* [2014, 2016]). However, results suggest that in the presence of wind-storms the contribution of the wave-induced transport to the total drift below the surface might be important. In the case of iSpheres, 70% of on-shelf drifters present track-averaged ocean currents generally larger than the Stokes drift while in the open ocean the majority of the trajectories (81%) are affected by larger wave-induced velocities $\langle u_s \rangle$. This seems to support the idea that one of the reasons for the larger improvements on the shelf relative to off-shelf might be the stronger ocean currents characterising shallow areas.

In order to understand the physical mechanism behind the differences in the currents forcing our drifters, we apply the Doodson filter [*Parker*, 2007] to the hourly ocean currents model outputs to remove diurnal and sub-diurnal signals and compute the residual flow $\boldsymbol{u}_r$. Figure 8 presents the frequency spectrum of the high-frequency oceanic flow $\tilde{\boldsymbol{u}} = \boldsymbol{u} - \boldsymbol{u}_r$ at the surface computed for three stations located in deep waters (stations S1 and S2 in the map in Fig. 8) and on the shelf (station S3). In our domain of study, the inertial period ranges between ≈ 13.5 and ≈ 17.2 hours. Figures 8a and b show clear inertial and M_2 maxima, indicating that in the open ocean $\tilde{\boldsymbol{u}}$ includes both tidal and mesoscale currents with modest amplitudes of comparable magnitude ($\approx 0.02 - 0.05 \ m \, s^{-1}$). Conversely, inertial oscillations are not present on the shelf and the strong high-frequency flow $\tilde{\boldsymbol{u}}$ is largely tidal with amplitude of $\approx 0.3 \ m \, s^{-1}$ as shown in Fig. 8c. This is probably a consequence of the strong dissipative processes characterising shallow areas which suppress the development of inertial waves [*Stanev and Ricker*, 2020]. Since barotropic tidal currents are generally more predictable than the fully baroclinic mesoscale circulation, these results may help also to explain why, on average, Lagrangian simulations (with or without coupling) are more skilful on the shelf than in the open ocean. In addition, velocity spectra reveals that ocean-wave coupling affects mesoscale currents while it has practically no effect on the M_2 tidal component .

Figure 7b presents the track-averaged ratio $\langle u_r \tilde{u}^{-1} \rangle$ as a function of the track-averaged wind speed $\langle U_{10} \rangle$. On the shelf, 25% of the drifters' trajectories are characterised by a ratio $\langle u_r \tilde{u}^{-1} \rangle > 1$, while in the deep ocean this happens for the 54% of the tracks. In addition, the track-averaged wind speed is larger than 14 $m \, s^{-1}$ for 56% of the drifters' tracks in the open ocean while the large majority of on-shelf trajectories (77%) are affected by a $\langle U_{10} \rangle < 14 \ m \, s^{-1}$. These results show that, during our four storms, the on-shelf upper ocean flow is generally tidally dominated whereas in the open ocean the residual component seems to lead the dynamics.

Figure 7c compares the track-averaged magnitude of the surface Stokes drift and the wind leeway in the case of iSphere drifters. For all the trajectories, the wind leeway is less relevant
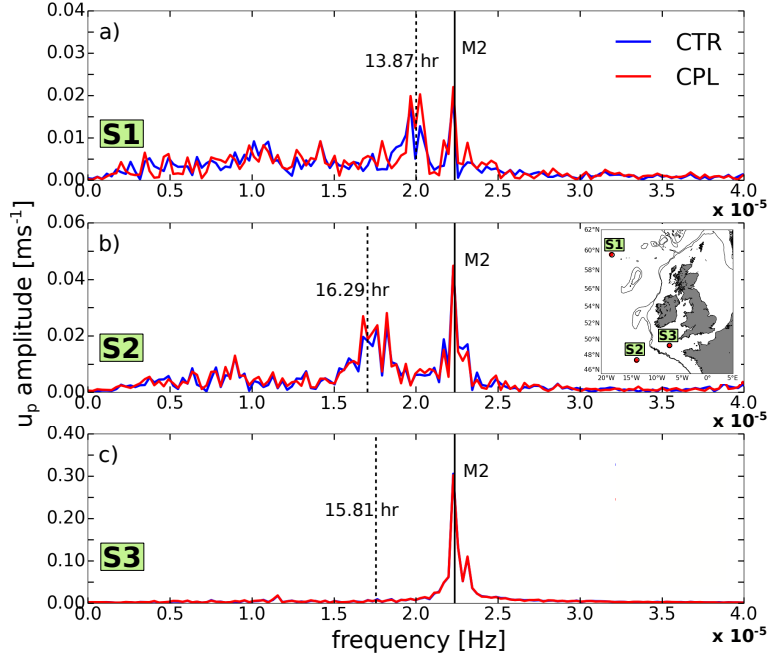
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Figure 8. Frequency spectrum of the zonal component of $\tilde{\boldsymbol{u}} = \boldsymbol{u} - \boldsymbol{u}_r$ velocity at the surface computed for three stations located in the open ocean (stations S1 and S2 in the inset) and on the shelf (station S3) for the period from 01-01-2016 to 10-02-2016.

than the Stokes drift, indicating that tidal, wind- and wave-driven currents represent the main forcing for both off- and on-shelf drifters. The high correlation ($r = 0.97$) between the wind leeway and the Stokes drift might suggest that iSphere trajectories are generally forced by locally generated wind-waves. This conclusion seems to be supported also by the high Stokes drift values found in Fig.7a, since the surface Stokes drift is mainly driven by shorter high-frequency waves while the contribution of lower wavenumbers (i.e., swell) is generally much smaller (e.g. *Breivik et al.* [2014]; *Pizzo et al.* [2019]; *Lenain and Pizzo* [2020]). Both results might also indicate that in the case of severe sea-states the wave-induced transport at the surface might be parameterised quite accurately as a function of the wind speed (e.g. *Breivik and Allen* [2008]).

Figure 9a presents the track-averaged ratio $\langle \tau_{ocn} \tau_{atm}^{-1} \rangle$ as a function of the average inverse wave age $\langle u_* c_p^{-1} \rangle$, where c_p is the phase velocity of waves at the peak of the wind-sea spectrum [*Melville et al.*, 2004], u_* is the air friction speed and $u_* c_p^{-1} \to 0.1$ in the case of younger waves while for older waves $u_* c_p^{-1} \to 0$. As expected, all the drifters are affected by relatively developed waves. This is a consequence of the algorithm used to identify the drifter trajectories affected by the storms. However, in the open ocean 59% of the drifters are affected by waves with $u_* c_p^{-1}$ larger than the median value of the data while on the shelf this is true for only 16% of the tracks. In addition, 76% of open ocean trajectories present $\langle \tau_{ocn} \tau_{atm}^{-1} \rangle <$ 1 and an average ratio of 0.99 while on the shelf for 58% of the tracks τ_{ocn} is larger than τ_{atm} and the average ratio is 1.03. Generally, both results seem to indicate that the open ocean might be affected by younger growing waves while on the shelf we might be in the presence of more developed decaying waves.

In the FOAM-AMM15 system, the sea surface roughness z_0 is computed as a function of the significant wave height H_s: when the ocean model is run in standalone mode H_s is parameterised from the wind speed following *Rascle et al.* [2008] while in coupled mode the H_s is computed by the wave model (see Sec.2.1.3 for the details). Figure 9b compares the track-
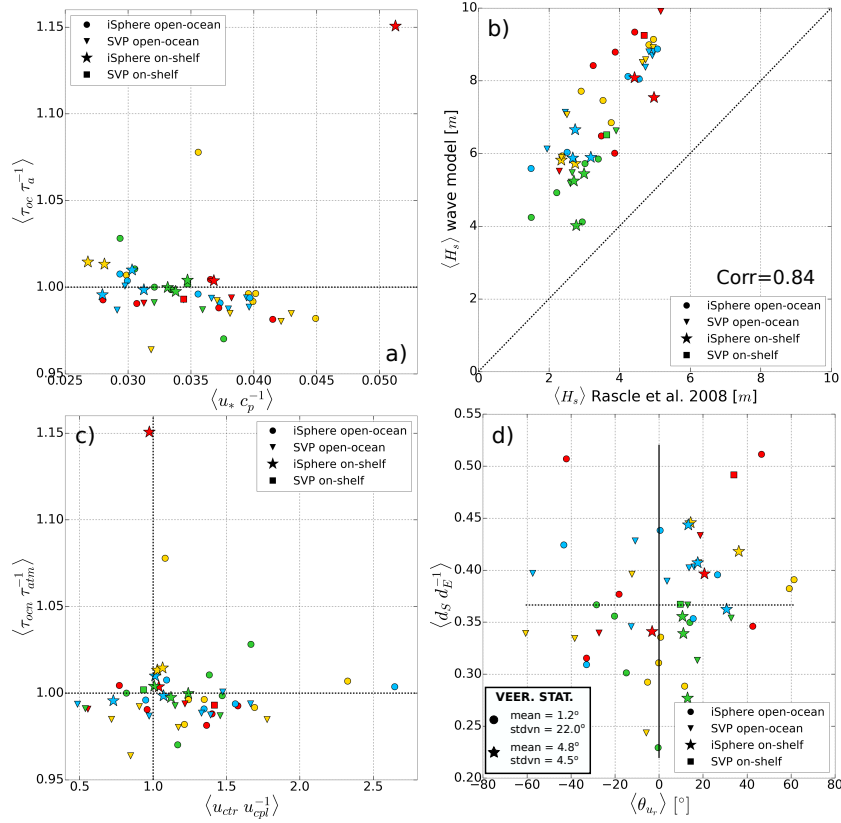
Figure 9. Track-averaged a) $\langle \tau_{ocn} \tau_{atm}^{-1} \rangle$ ratio as a function of the average inverse wave age $\langle u_* c_p^{-1} \rangle$, b) $\langle H_s \rangle$ estimated by the standalone ocean model against the $\langle H_s \rangle$ computed by the spectral wave model, c) $\langle \tau_{ocn} \tau_{atm}^{-1} \rangle$ ratio as a function of the ratio $\langle u_{ctr} u_{cpl}^{-1} \rangle$, d) ratio $\langle d_s d_e^{-1} \rangle$ and the veering θ_{u_r} of CPL residual currents with respect to the CTR residual flow computed according to *Kundu* [1976]) for open ocean and on-shelf surface (iSpheres) or 15 m (SVPs) drifters.

averaged $\langle H_s \rangle$ estimated according to *Rascle et al.* [2008] (i.e. Eq. 4) against the $\langle H_s \rangle$ computed by the spectral wave model. *Rascle et al.* [2008] found that estimating the significant wave height H_s from the wind speed might be a good approximation in the case of young wind-seas without swell, while it could lead to an underestimation of $10-20\%$ in the case of fully developed waves. The high correlation ($r = 0.84$) between the estimated and computed H_s of our results seem to support those conclusions. However, our results also indicate that, during severe storm conditions, the parameterisation used by the uncoupled ocean model might underestimate the H_s computed by the spectral wave model by $30-50\%$.

When modifying the water-side momentum flux or the sea surface roughness z_0, the result is that the speed of the upper ocean flow u is changed. In order to understand the impact of both wave feedbacks on the magnitude of ocean currents, we continue our analysis computing the track-averaged ratio $\langle u_{ctr} u_{cpl}^{-1} \rangle$, where u_{ctr} are ocean currents from the CTR trial while u_{cpl} are the ones from the CPL run. Figure 9c shows that, in the open ocean, for 80% of iSphere and 56% of SVP tracks u_{ctr} currents are larger than u_{cpl}, with a mean ratio of 1.50 and 1.40, respectively. On the shelf, 80% of the iSpheres show $\langle u_{ctr} u_{cpl}^{-1} \rangle > 1$, although with much smaller values - the mean ratio is equal to 1.07. 50% of the tracks of the on-shelf SVPs present u_{cpl} larger than u_{ctr} with a ratio of 0.94.

The simplified analysis of Sec. 3 indicated that the magnitude of the Coriolis-Stokes veering might depend on the ratio between the Stokes' depth d_s and the Ekman scale d_e. In or-

der to verify whether this is the case also in a realistic scenario, we compute the track-averaged ratio $\langle d_s\, d_e^{-1} \rangle$ and $\langle \theta_{u_r} \rangle$, where θ_{u_r} is the veering of CPL residual currents with respect to the CTR residual flow computed according to *Kundu* [1976] - a positive θ_{u_r} signifies that the vector $\boldsymbol{u}_{r,cpl}$ veers clockwise with respect to $\boldsymbol{u}_{r,ctr}$. The Stokes' depth d_s is calculated using the peak period of the wind-sea spectrum and the *Fenton and McKee* [1990] approximation. The length scale of neutrally stratified Ekman layers is usually estimated as $d_e = \gamma u_{*w}\, f^{-1}$, with γ derived from observations (e.g., *Stigebrandt* [1985]; *Perlin et al.* [2007]). In this work we use $\gamma = 0.25$ [*Coleman et al.*, 1990; *McWilliams et al.*, 1997; *Polton et al.*, 2005]. Assuming constant vertical viscosity will always result in overestimating d_e, since stratification acts to inhibit turbulent mixing of momentum reducing the Ekman layer thickness (e.g., *Cushman-Roisin and Beckers* [2011]). Figure 9d shows that 58% of on-shelf tracks present $\langle d_s\, d_e^{-1} \rangle$ greater than the median value of the data (0.37) while in the open ocean this is true for 45% of the drifter trajectories. At the same time, on-shelf tracks present a mean $\langle \theta_{u_r} \rangle$ of 17.32° with a standard deviation of 10.93° while in the open ocean the mean $\langle \theta_{u_r} \rangle$ is -1.42° and the standard deviation is 29.59°.

4.2.2 The effect of coupling on the Stokes drift

The impact of ocean-wave coupling on the Stokes drift can be assessed comparing Lagrangian simulations using the same data for the ocean currents but different forcing for the Stokes drift, i.e. contrasting $U_{ctr}S_{ctr}$ against $U_{ctr}S_{cpl}$ and $U_{cpl}S_{ctr}$ against $U_{cpl}S_{cpl}$, respectively.

Table 5 reveals that ocean-wave coupling has, on average, a small (or negligible) impact on the wave-induced currents, with a difference in the average skill score between off- and on-shelf simulations of ±1%. This result is in line with our expectations, since formally the FOAM-AMM15 coupled system does not include any new ocean currents effect to the action density balance equation solved by the spectral wave model.
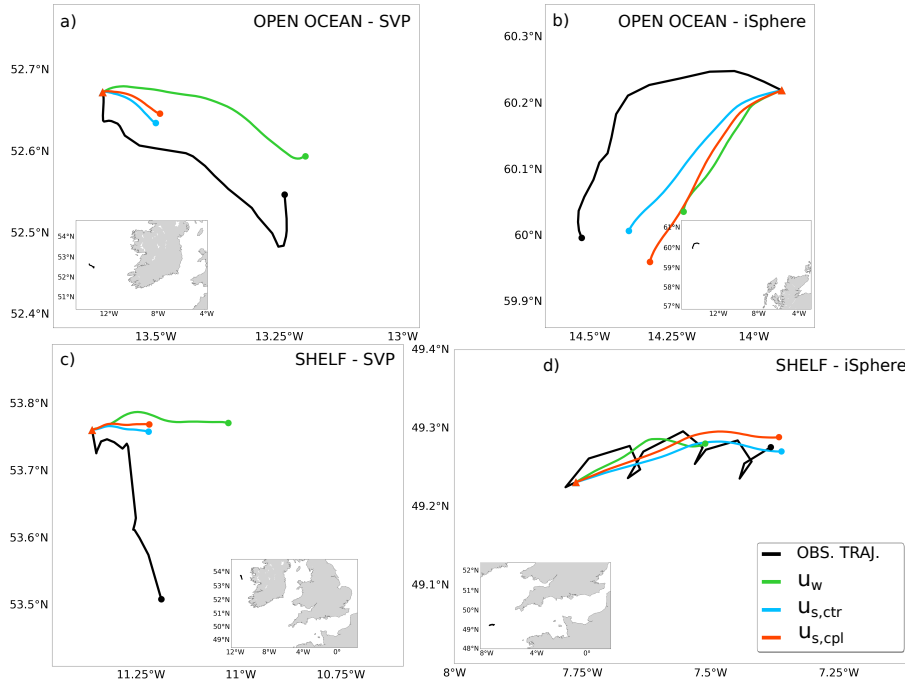

Figure 10. Examples of open ocean and on-shelf iSphere and SVP drifter simulations obtained forcing the Lagrangian model only with wind leeway ($\boldsymbol{u}_w$, green trajectories) or only with the Stokes drift from either the CTR ($\boldsymbol{u}_{s,ctr}$, light-blue lines) or the CPL ($\boldsymbol{u}_{s,cpl}$, red tracks) trial runs.

However, Fig.6 seems to indicate that the tracks simulated forcing the Lagrangian model with the CPL Stokes drift are consistently deflected in comparison to the ones using the Stokes drift from the uncoupled system, especially at the surface (compare light-blue against yellow lines and/or green against red lines).

The direction of the Stokes drift at the surface usually correlates relatively well with the wind direction, since it is more sensitive to the high-frequency part of the wave spectra (e.g., *Webb and Fox-Kemper* [2015]; *Tuomi et al.* [2018]). In order to investigate whether differences in the Stokes drift direction may be related to the wind direction, we conducted three additional Lagrangian experiments: in the first one virtual drifters where forced only with the wind leeway ($\boldsymbol{u}_w$) while in the other two we applied only the Stokes drift forcing from either the CTR ($\boldsymbol{u}_{s,ctr}$) or the CPL ($\boldsymbol{u}_{s,cpl}$) trials, respectively.

Figure 10 shows some examples of the results from this last set of simulations. The virtual trajectories obtained forcing the Lagrangian model with the CPL Stokes drift are more closely aligned with the ones using only the wind leeway, suggesting that switching on the three wave feedbacks in the FOAM-AMM15 momentum balance equation may have a control also on the direction of the Stokes drift computed by the wave model.

In order to quantify this effect, Tab.6 presents the mean track-averaged veering $\langle \theta_{u_s} \rangle$ of CTR and CPL Stokes drift vectors with respect to the wind leeway direction computed according to *Kundu* [1976]. Results shows that the Stokes drift from the coupled run reduce the veering from the wind direction by more than 50% in comparison with the one of the Stokes drift from the uncoupled system, in agreement with observations (e.g., *Clarke and Van Gorder* [2018]).

DRIFTER TYPE	REGION	NUMB. OF DRIFTERS	Mean $\langle \theta_{u_s} \rangle$ [°] CTR	CPL
iSphere	shelf & shelf-break	10	5.50	1.52
	open ocean	21	5.46	-3.50
SVP	shelf & shelf-break	2	6.19	-0.80
	open ocean	16	6.09	-3.44

Table 6. Mean track-averaged veering $\langle \theta_{u_s} \rangle$ of Stokes drift vectors from CTR and CPL trial datasets with respect to the wind leeway direction. The veering is computed according to *Kundu* [1976].

4.3 The relative impact of each single ocean-wave interaction

The aim of this section is to quantify which one of the three wave-current interactions included in the FOAM-AMM15 coupled system has the larger impact on the accuracy of the solution for the surface dynamics.

Five different Lagrangian experiments are compared (see Tab.7). Two of them forced the Lagrangian model with ocean and wave data from CTR and CPL trials. The other three experiments used forcing data from FOAM-AMM15 simulations where only one wave-current interaction was switched on: CSF used only the Coriolis-Stokes forcing, TOC only the wave-dependent water-side stress while WSR only the sea-state modulated sea surface roughness (see Sec.2.2.2 for the details). In the case of open ocean iSpheres, the Lagrangian simulations were forced using also the wind leeway. Since CSF, TOC and WSR ocean-wave simulations covered only the storms occurred in January-February (i.e., Gertrude, Henry and Imogen), only 37 drifter trajectories were simulated in this set of Lagrangian experiments.

Numerical results presented in Tab.7 indicate that the best skill score is obtained when the three wave-current interactions are considered. The Coriolis-Stokes forcing seems to be the dominant wave-current interaction for both iSphere (0.64 ± 0.20) and SVP (0.48 ± 0.23)

DRIFTER TYPE	REGION	NUMB. OF DRIFTERS	$\overline{ss}\pm$SD				
			CTR	CPL	CSF	TOC	WSR
iSphere	shelf & shelf-break	7	0.74 ± 0.08	0.81 ± 0.09	0.79 ± 0.09	0.75 ± 0.07	0.80 ± 0.09
	open ocean	16	0.54 ± 0.22	0.58 ± 0.17	0.58 ± 0.19	0.55 ± 0.21	0.57 ± 0.18
SVP	shelf & shelf-break	1	0.34	0.61	0.53	0.47	0.32
	open ocean	13	0.42 ± 0.25	0.49 ± 0.25	0.47 ± 0.24	0.45 ± 0.22	0.45 ± 0.22

Table 7. Average skill score $\overline{ss}$ and standard deviation SD of iSphere and SVP drifters on the shelf and in the open ocean for the following five Lagrangian experiments: CTR and CPL simulations used ocean currents and Stokes drift from an uncoupled and a fully coupled FOAM-AMM15 system, respectively; the CSF experiment used ocean and wave data from an ocean-wave simulation where only the Coriolis-Stokes wave effect was activated; the TOC Lagrangian simulations used forcing data produced by the FOAM-AMM15 system using only the wave-dependent momentum flux; the WSR experiments forced the Lagrangian model with data from an ocean-wave simulation activating only the sea-state dependent sea surface roughness.

drifters, in agreement with the results of the simplified wave-modified Ekman model of Sec. 3. In the case of iSpheres, the second most important wave effect seems to be the wave-dependent sea surface roughness z_0 (0.63 ± 0.19) while for SVPs is the wave-dependent momentum flux (0.46 ± 0.22), especially on the shelf.

The visual inspection of the simulated trajectories may help to better understand the dynamical impact of each wave-current interaction. Figure 11 presents four examples of drifter tracks simulations from CTR (in light-blue), CPL (in red), CSF (in green), TOC (in yellow) and WSR (in violet) Lagrangian experiments representative of iSpheres and SVPs in open ocean and on-shelf conditions.

In the case of the on-shelf iSphere (see Fig.11a), the TOC trajectory is slightly faster than the CTR one, indicating that $\boldsymbol{\tau}_{ocn}$ is generally larger than $\boldsymbol{\tau}_{atm}$ but to a small extent. At the same time, the WSR virtual drifter is significantly slower than the CTR: in the uncoupled simulation H_s is underestimated (see Fig.8b), resulting in a smaller z_0, reduced vertical shear and consequently increased surface currents, in agreement with the findings of *Carniel et al.* [2009]. The CPL and CSF trajectories are very similar, confirming the supremacy of the Coriolis-Stokes force.

Conversely, in the open ocean iSphere case (see Fig.11c) both TOC and WSR drifters are slower than the CTR one, indicating that $\boldsymbol{\tau}_{ocn} < \boldsymbol{\tau}_{atm}$ and z_0 is larger when computed by the wave model, respectively. However, the CPL trajectory seems to be an hybrid between both CSF and WSR tracks, confirming the leading role of both wave effects in the open ocean as found in Tab.7.

SVP drifters seem to be affected by the same dynamics of surface drifting buoys, although with some differences. In the case of the on-shelf SVP drifter (see Fig.11b), the wave-modulated water-side stress $\boldsymbol{\tau}_{ocn}$ seems to dominate the wave-dependent z_0 (CPL and TOC virtual drifters show very similar velocity) while for the open ocean SVP (see Fig.11d) the CPL drifter seems to follow a path very similar to the CSF one but with slightly slower speed as in the TOC simulation. As one can expect, SVPs simulations are less impacted by the sea-state modulated z_0, indicating that this wave-related process might be less important for the sub-surface circulations.

Numerical results show that the wave-dependent momentum flux might have quite an important impact on the accuracy of numerical SVP trajectories. The resolution of the vertical grid near the surface plays an important role in the propagation of the momentum from the atmosphere down into the water column (e.g., *Carniel et al.* [2009]). If the model verti-
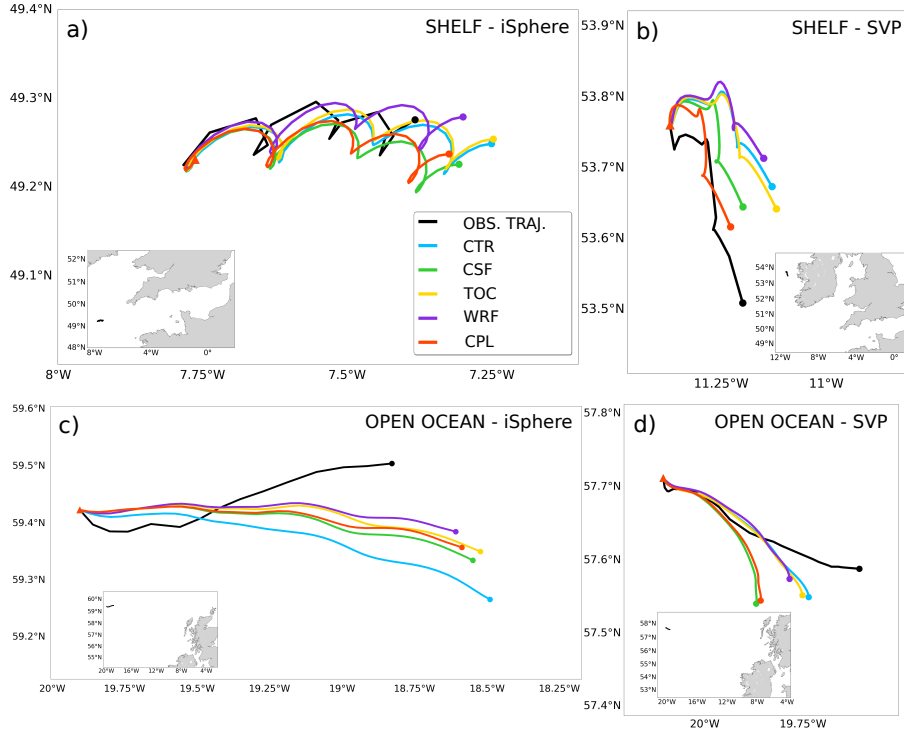
Figure 11. Simulated trajectories from CTR (in light-blue), CPL (in red), CSF (in green), TOC (in yellow) and WSR (in violet) Lagrangian experiments representative of open ocean and on-shelf iSphere and SVP drifters.

cal grid is too coarse, the shear of the Ekman current might be overestimated, resulting in a too weak modelled sub-surface circulation. Assuming that AMM15 vertical discretization is lacking the required resolution near the surface could explain why SVP simulations have generally lower skill score (< 0.5). AMM15-ocean uses 51 s-levels with a constant thickness of 1m for the uppermost grid cell in areas where the depth is larger than 50 m [*Siddorn and Furner*, 2013]. Research activities are ongoing for improving the vertical resolution of this model, taking into consideration also this aspect [*Bruciaferri et al.*, 2021]. However, the type of vertical discretization impacts the accuracy of a wide range of physical processes reproduced by an ocean model and the choice of the vertical grid is not an easy task and must be pursued very carefully (e.g. *Siddorn and Furner* [2013]; *Bruciaferri et al.* [2018, 2020]).

4.4 Physical processes driving surface drifters during storms

The aim of this Section is to obtain further insights about some of the details underpinning the physical mechanisms driving the transport of open ocean and on-shelf drifters during the storms. We explore and discuss the time-series of a number of diagnostics computed along the observed track of a couple of iSpheres chosen to represent open ocean and on-shelf conditions. The analysis is conducted only for surface drifters since the results of Sec.4.1 indicated that SVPs simulation might be affected by inaccuracies not related with ocean-wave coupling.

The open ocean case considers the iSphere trajectory presented in Fig.11c. During the storm, the drifter is primarily transported by the Stokes drift, as showed by the time-series of the along-track ocean and wave-induced currents speed from CTR and CPL trials presented in Fig.12a. In addition, Fig.12b reveals that residual currents are the second most important forcing while the high frequency flow $\tilde{u}$ represents the minor transport process.
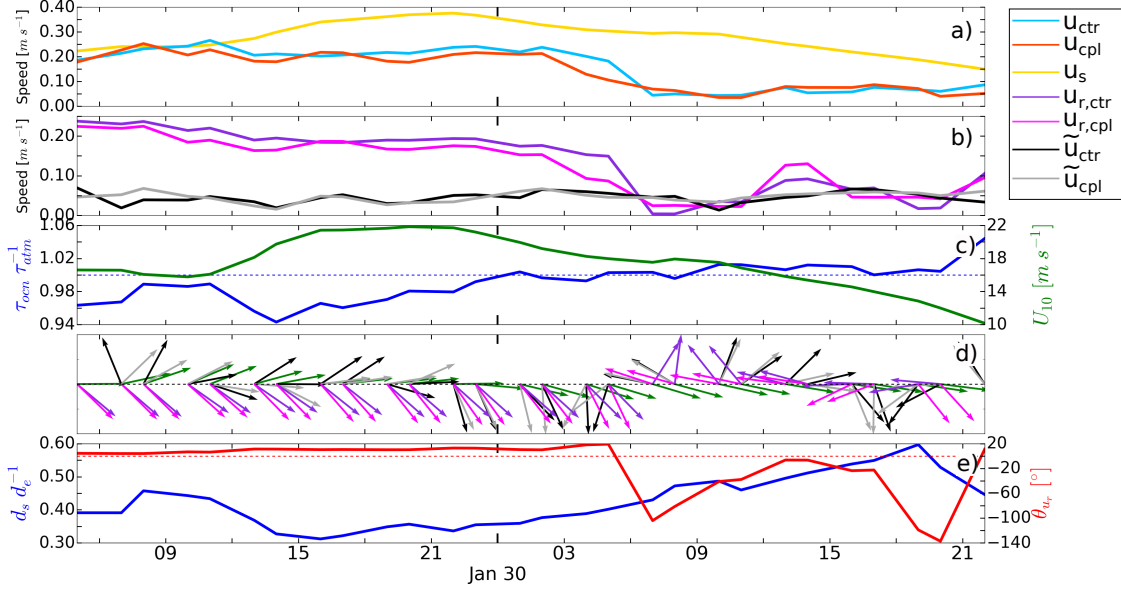
Figure 12. Diagnostics computed along the observed iSphere track shown in Fig.11c representing deep water conditions. Time-series of a) CTR (light-blue) and CPL(red) ocean currents and Stokes drift (yellow) speed; b) CTR and CPL $u_{t,ctr}$ (black) and $u_{t,cpl}$ (grey) tidal currents and $u_{r,ctr}$ (violet) and $u_{r,cpl}$ (magenta) residual currents; c) 3 hourly ECMWF wind speed (green) and $\tau_{ocn}\tau_{atm}^{-1}$ ratio (blue); d) wind (green), high frequency $\tilde{u}_{ctr}$ (black) and $\tilde{u}_{cpl}$ (grey) and residual $u_{r,ctr}$ (violet) and $u_{r,cpl}$ (magenta) vector directions; veering θ_{u_r} of $u_{r,cpl}$ with respect to $u_{r,ctr}$ (red) and $d_s\,d_e^{-1}$ ratio (blue).

Time-series of along-track CTR and CPL residual currents speed (Fig.12b, violet and magenta lines respectively) seems to correlate quite well with the along-track wind speed time-series (Fig.12c, green line), indicating that wind-driven currents might represent the dominant component of the residual circulation. The time evolution of the differences between $u_{r,ctr}$ and $u_{r,cpl}$ signals and the time-series of $\tau_{ocn}\tau_{atm}^{-1}$ ratio (Fig.12c, blue line) seem to confirm this: from 29 January, $\approx 10{:}00$am to 30 January, $\approx 6{:}00$am the drifter track is affected by high wind speeds ($U_{10} > 16\ m\,s^{-1}$), $\tau_{ocn} < \tau_{atm}$ and consequently $u_{r,ctr} > u_{r,cpl}$. After, the wind speed decreases to values below $12\ m\,s^{-1}$, $\tau_{ocn} \approx \tau_{atm}$ and the differences between $u_{r,ctr}$ and $u_{r,cpl}$ seem less related to the wind dynamics, suggesting the weakening of the wind-driven component of the residual circulation.

Figure 12d presents time-series of wind, residual and high frequency currents vector directions. During the high-wind period, residual vectors are consistently to the right of the wind direction (see violet and magenta vectors with respect to green arrows), as from the classical Ekman theory for the wind-driven circulation. In addition, CPL residual currents present a consistent clockwise additional veering of $5-15°$ with respect to CTR currents (see red line of Fig.12e), in agreement with the storm modified Ekman model of Sec.3. When the wind decreases, the wind-driven circulation weakens, as shown by the high variability of the veering θ_{u_r} (see violet and magenta vectors in Fig.12d and red line in Fig.12e). In the open ocean, the high frequency flow $\tilde{\boldsymbol{u}}$ includes both tidal and inertial currents, as shown in Fig. 8 (note that the location of the open ocean drifter trajectory analysed in this section is very close to the S1 station of Fig. 8). Therefore, differences in direction between CTR and CPL $\tilde{\boldsymbol{u}}$ (grey and black vectors in Fig.12d) are probably due to the effects of coupling on the mesoscale dynamics. During the high-wind phase the ratio $d_s\,d_e^{-1}$ oscillates around 0.35 while in the low-wind phase grows up to 0.60 (see blue line in Fig.12e): in this case the diagnostic $d_s\,d_e^{-1}$ seems to be controlled more by the dynamics of the wind-driven circulation (i.e., the Ekman scale) than the Coriolis-Stokes force (i.e., the Stokes depth).
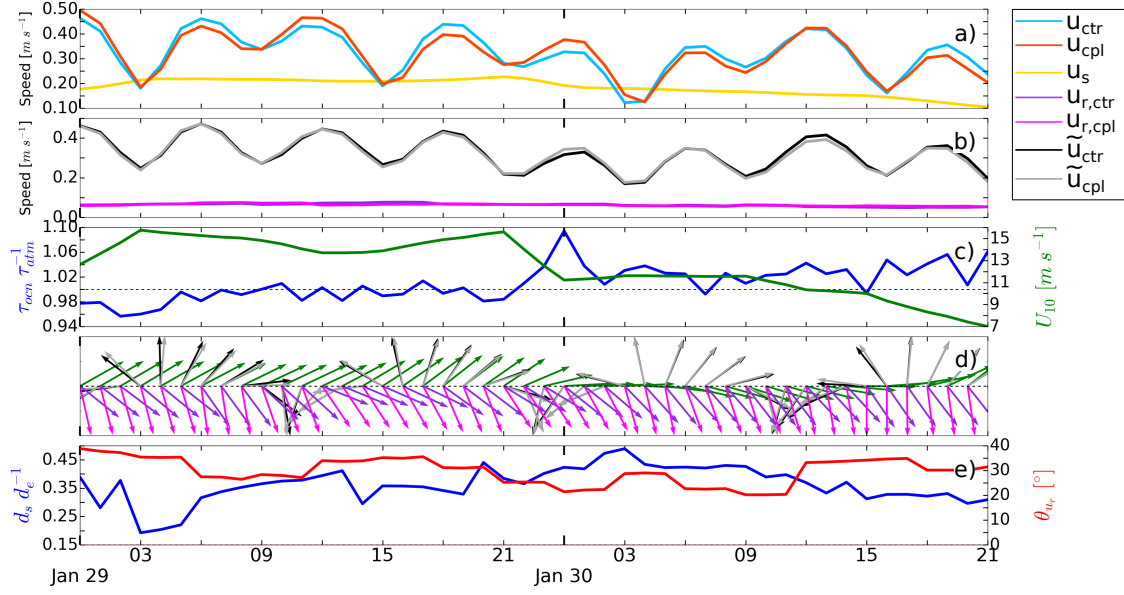
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Figure 13. Diagnostics computed along the observed iSphere track shown in Fig.11a representing on-shelf conditions. Time-series of a) CTR (light-blue) and CPL(red) ocean currents and Stokes drift (yellow) speed; b) CTR and CPL $u_{t,ctr}$ (black) and $u_{t,cpl}$ (grey) tidal currents and $u_{r,ctr}$ (violet) and $u_{r,cpl}$ (magenta) residual currents; c) 3 hourly ECMWF wind speed (green) and $\tau_{ocn}\tau_{atm}^{-1}$ ratio (blue); d) wind (green), high frequency $\tilde{u}_{ctr}$ (black) and $\tilde{u}_{cpl}$ (grey) and residual $u_{r,ctr}$ (violet) and $u_{r,cpl}$ (magenta) vector directions; veering θ_{u_r} of $u_{r,cpl}$ with respect to $u_{r,ctr}$ (red) and $d_s\,d_e^{-1}$ ratio (blue).

For the on-shelf scenario we chose the iSphere track presented in Fig.11a. On the shelf, the high frequency flow $\tilde{\boldsymbol{u}}$ includes mainly tidal currents (see Fig. 8). Figures 13a,b show that the on-shelf drifter is prevalently transported by tidal currents while the Stokes drift and the residual flow represent the second and third forcing, respectively. High wind speeds ($U_{10} > 13\ m\,s^{-1}$) affect the on-shelf track on 29 January from $\approx 3\!:\!00$am to $\approx 9\!:\!00$pm, while wind speeds drop to less than $\approx 10\ m\,s^{-1}$ during the second part of the trajectory (see green line in Fig.13c). Differences between CPL and CTR total currents speed time-series (Fig.13a, red and light-blue lines, respectively) show a periodic pattern which suggests an interplay between tides and wave feedbacks on the ocean currents. Figure 13d reveals the details of this interaction: CPL residual currents present an additional clockwise veering relative to the CTR field due to the Coriolis-Stokes acceleration which affects the vector sum with the tidal circulation, with the final result of modulating the magnitude of total currents.

The additional veering θ_{u_r} of CPL residual currents is consistently positive along the entire track, with values around $20-30°$ (see red line in Fig.13e): during the low-wind phase the Coriolis-Stokes force is probably acting on wind-driven inertial oscillations triggered by the wind drop at the end of 29 January. The time-series of $d_s d_e^{-1}$ (blue line of Fig.13e) shows slightly larger values during the low-wind wave-decaying phase.

5 Discussion

The results of Sec. 4 indicated that improvements in the average skill score of iSphere and SVP Lagrangian simulations due to wave feedbacks on the ocean currents are larger on the shelf than in the open ocean. Our analysis indicates that several physical mechanism related to the contrasting dynamical regime of deep ocean and shallow marine environments might contribute to this result (see for example *Bruciaferri* [2020] and references therein for a review of physical and numerical challenges characterising shelf seas dynamics).
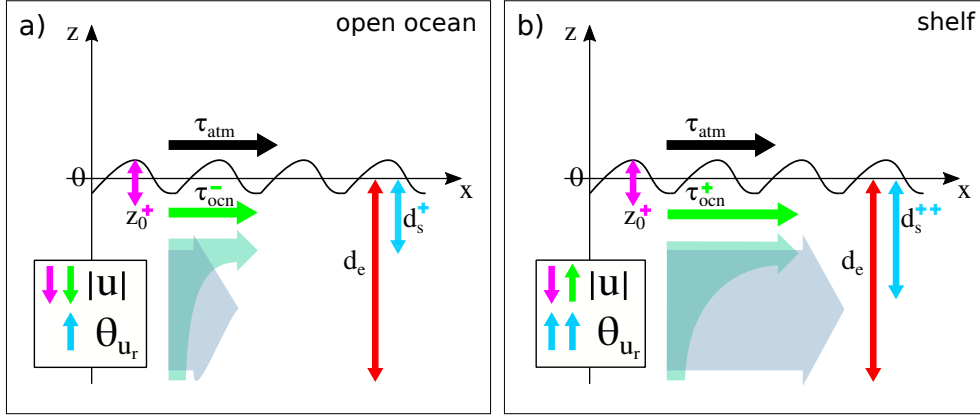
Figure 14. Sketch describing the main mechanisms relating wind-driven circulation, tidal currents and wave feedbacks on the ocean momentum budget in the open ocean (a) and on the shelf (b). The grey-blue thick arrows represent tides, while the green-blue curved arrows describe sheared wind-driven currents. Wave feedbacks are indicated with a plus or minus, while their final effect on the ocean currents (magnitude $|\boldsymbol{u}|$ or direction θ_{u_r}) is explained by the vertical arrows in the boxes. Also, z_0 is the roughness length, d_s the Stokes' depth, d_e the Ekman scale while $\boldsymbol{\tau}_{atm}$ and $\boldsymbol{\tau}_{ocn}$ are the air- and water-side stresses, respectively. See the text for a detail description of the processes.

For example, Fig. 7 and 9a indicate that, during our storms, deep ocean and shelf areas might be affected by wind-waves at different stages of wave-growth: in the open ocean, we might be in the presence of younger growing waves where part of the atmospheric stress is transferred to the rapidly developing wave field reducing the water-side momentum flux while in shelf areas more developed decaying waves may tend to release momentum into the ocean increasing the water-side stress.

In addition, Fig. 9b clearly shows that in the presence of severe sea-states the H_s calculated by the wave model is consistently larger than the one estimated from the wind speed, resulting always in a larger z_0 both off- and on-shelf.

Combining the findings of Fig. 9a, 9b and 9c suggest that off-shelf the sea state controlled $\boldsymbol{\tau}_{ocn}$ and z_0 might cooperate to reduce the strength of the ocean currents $\boldsymbol{u}$ while on the shelf they might counteract each other resulting in a u_{cpl} more similar to u_{ctr}. The same mechanism seem to be confirmed by the simulations of Sec. 4.3. In the case of the on-shelf drifter (Fig.11a), the virtual drifter is slower in the CPL simulation than in the CTR one, indicating that the sea-state controlled z_0 prevails on the wave-dependent stress $\boldsymbol{\tau}_{ocn}$. Conversely, in the open ocean case (Fig.11c), both $\boldsymbol{\tau}_{ocn}$ and z_0 wave feedbacks cooperate to reduce the magnitude of the surface currents. Similarly, the analysis of Fig. 13 shows that while $\tau_{ocn}\tau_{atm}^{-1}$ time-series correlates quite well with the wind speed signal − i.e., $\tau_{ocn} \leq \tau_{atm}$ ($\tau_{ocn} > \tau_{atm}$) during the high-wind (low-wind) phase − CTR and CPL residual currents present very small differences in magnitude during the entire track. This is probably an indication of the competition between the wave-dependent τ_{ocn} and z_0, especially during the low-wind phase.

The results of Fig. 9d seem to indicate that the findings of the simplified storm-modified Ekman model presented in Sec. 3 might apply also to our more realistic scenario: in shallow areas, the Coriolis-Stokes forcing appears to affect a larger portion of the Ekman depth with CPL residual currents presenting a consistent positive veering with respect to the CTR residual flow; conversely, in the open ocean d_s tend to be shallower and $\langle\theta_{u_r}\rangle$ shows larger variability, suggesting a weaker impact of the CSF term.

Finally, the analysis presented in Fig. 8 and Sec. 4.4 showed that the three wave feedbacks included in the FOAM-AMM15 coupled system mainly impact the wind-driven mesoscale circulation while it has practically not direct effect on the tidal dynamics, especially on the shelf. However, Fig. 13 revealed also that net on-shelf circulation is importantly modulated by the interaction between the strong tidal flow and the wave-modified wind-induced currents.

Figure 14 summarises the main mechanisms involving wind-driven circulation, tidal currents and wave feedbacks on the ocean momentum budget in the open ocean (a) and on the shelf (b) during the storms considered in our study.

In general, the open ocean is impacted by younger shorter waves (see Fig.14a). Two main consequences follow from this: i) part of the atmospheric stress is extracted by the rapidly growing wave field, reducing on average the momentum flux into the ocean $\boldsymbol{\tau}_{ocn}$; ii) the importance of the Stokes' depth scale d_s with respect to the Ekman depth d_e is generally decreased, making the Coriolis-Stokes veering θ_{u_r} less pronounced than on the shelf. When the reduced $\boldsymbol{\tau}_{ocn}$ combines with the constantly larger z_0, the result is that both wave effects generally act in synergy to slow down ocean currents. In addition, tidal currents are also weak off-shelf, making the interactions between waves, tides and residual circulation less important as well.

On the shelf (see Fig.14b), wind-waves are generally more mature than in the open ocean, resulting in i) net outflux of momentum from waves into the ocean (i.e., $\boldsymbol{\tau}_{ocn} > \boldsymbol{\tau}_{atm}$, and ii) relatively larger $d_s\, d_e^{-1}$ ratio with increased and more consistent Coriolis-Stokes veering θ_{u_r}. In this case, the increased momentum flux into the ocean $\boldsymbol{\tau}_{ocn}$ and the larger roughness length z_0 seem to compete one against another, resulting in almost vanishing their mutual impacts on the ocean currents strength. Shallow areas are affected also by very strong tidal currents, making the interactions between waves, tides and residual circulation a leading order process.

6 Conclusions

In this study, we assess and analyse the impact of including three wave-dependent processes in the momentum equation solved by the ocean model of the Met Office ocean-wave forecasting system of the NWS. Our focus is on the accuracy of the simulated upper ocean circulation in the presence of severe sea-states. The analysis is conducted using upper ocean velocities produced by various versions of the NWS forecasting system differing only in the level of ocean-wave coupling to simulate the trajectories of a number of drifters affected by four Atlantic storms occurred in winter 2016.

Sensitivity experiments showed that, regardless the level of coupling, including the wind drag velocity in the Lagrangian transport equation allows the improvement of numerical tracks' accuracy in the open ocean while significantly degrades the results in shallow areas. Assessment against independent observations indicated that one reason that improvements are not evident on the shelf might be the inaccuracies affecting wind model data in shelf and coastal areas, in agreement with other studies (e.g. *Christakos et al.* [2020]).

Lagrangian experiments to assess the benefit of ocean-wave coupling showed that, in the presence of extreme events, using forcing data from a fully coupled system allows to improve the skill of the numerical drifter trajectories by $\approx 4\%$. In addition, results showed that improvements are comparable for both iSphere and SVP drifters, suggesting that, during storms, the three wave-related processes included in the NWS coupled system might extend below the surface and impact a larger part of the upper ocean.

Ocean-wave coupling primarily impacts ocean currents, improving the accuracy of the predicted surface dynamics by $\approx 4\%$ in the open ocean and $\approx 8\%$ on the shelf. Our analysis showed that this is probably a consequence of the contrasting dynamical regimes characterizing deep and shallow marine environments, with stronger tidal currents, a more vigorous

wind-driven circulation and a more pronounced Coriolis-Stokes veering on the shelf than in the open ocean.

Numerical results indicated that the Coriolis-Stokes force is the dominant wave-current interaction during storm events, both off- and on-shelf. In addition, we found that in the case of surface iSpheres, the second most important wave effect is the wave-dependent sea surface roughness while for 15 m drogued SVP drifters is the wave modified water-side stress.

The impact of ocean-wave coupling on the Stokes drift seems to be not relevant in terms of skill score improvements. However, a more in depth analysis showed that the Stokes drift from a fully coupled system is deflected to be more aligned with the wind direction in comparison with the one from the uncoupled system, in agreement with observations (e.g., *Clarke and Van Gorder* [2018]).

All our ocean simulations parameterised the input of turbulence at the surface due to wave-breaking according to *Craig and Banner* [1994], with no sea-state feedback. Similarly, wave effects on the bottom friction were not considered. However, our experiments showed that, during extreme events, the sea surface roughness simulated by the coupled system is consistently enhanced with respect to the one parameterised by the stand-alone ocean model. This might indicate that including the input of wave-induced turbulence in the coupling strategy (both at the surface and the bottom, e.g. *Staneva et al.* [2016a]) may help to further improve the accuracy of the simulated upper ocean dynamics, especially in shallow areas.

In the case of SVPs we found that, independently from ocean-wave coupling, simulated drifter trajectories are generally slower than the observed ones. This might be due to the inability of the ocean-wave modelling system to properly represent some storm-related physical processes which may promote enhanced transport (e.g., drifters surfing large waves). Alternatively, slower wind-induced currents below the surface could also indicate that the ocean model is overestimating the vertical shear of Ekman circulation, for example due to a vertical grid which may discretize the upper ocean with not enough details.

One possible limitation of this study is the number of observations: while with 49 satellite-tracked trajectories we are able to cover quite extensively the open ocean, drifters on the shelf are more scarce, especially in the North Sea.

This study shows that coupled circulation-wave models may be fundamental for improving our ability of predicting the transport and fate of particles and objects floating on the sea surface, with important practical implications for example for search and rescue activities or oil spill and plastic dispersal monitoring and control operations.

A: Algorithm to identify storm-affected trajectories

In order to identify the drifters trajectories which were affected by the four storms considered in this study, drifter observations from the CMEMS NWS in-situ product [*Wehde et al.*, 2021] dataset were pre-processed with the following algorithm.

For each drifter trajectories:

1. Consider the time window when each storm was recorded as active in winter 2016 on the NWS (GERTRUDE: 29-30 January; HENRY: 1-2 February; IMOGEN: 8 February; JAKE: 1-4 March);
2. Extend the identified time-window by adding the day after and before its limits;
3. Interpolate AMM15-wave H_s fields along the observed drifter trajectory during the identified time-window.

The result is a time-series of the H_s along each drifter trajectory during each storm. Then, for each H_s time-series:

1. Compute the peak as the record of the time-series where $H_s > H_{s99}$ [*Masselink et al.*, 2016], where H_{s99} is the 1% exceedance H_s (i.e. the H_s with a value which is exceeded in the time-series only 1% of the time);

2. Discard all the time-series presenting a H_s peak less than 6 m;

3. Compute the beginning (end) of the along-drifter storm as the record of the H_s time-series occurred before (after) the peak of the storm which is nearest in time to the occurrence of the peak and with $H_s < H_{s30}$ (i.e. the H_s with a value which is exceeded in the timeseries 70% of the time).

As an example, Fig. A.1 presents the H_s time-series along the trajectories of those drifters identified by the algorithm for storm Henry.

Figure A.1. Time-series of along-track H_s for those drifters identified by our algorithm during storm Henry

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