

Martian Highlands Differentiation Concomitant to Dichotomy Formation

Valentin Bonnet Gibet¹, Chloe Michaut², Thomas Bodin³, Mark A. Wieczorek⁴, and Fabien Dubuffet⁵

¹DLR

²Ecole Normale Supérieure de Lyon

³CNRS, ENS Lyon, Université de Lyon-1

⁴Université Paris Cité

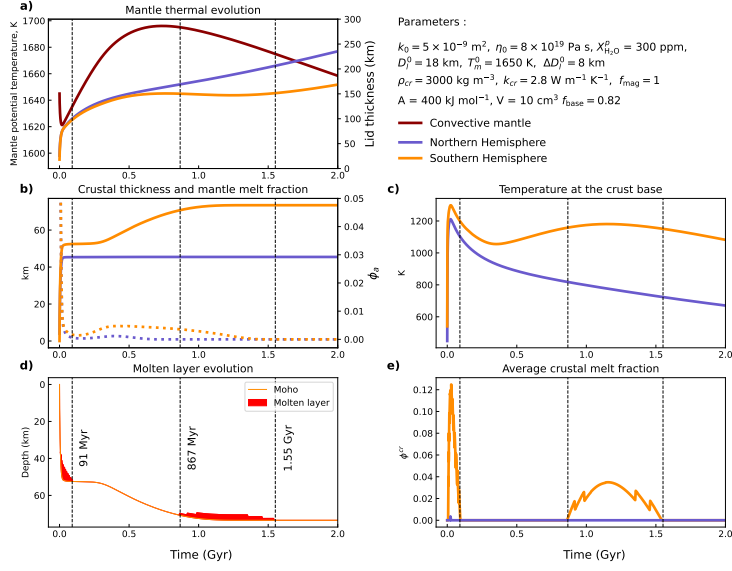
⁵ENS Lyon, France

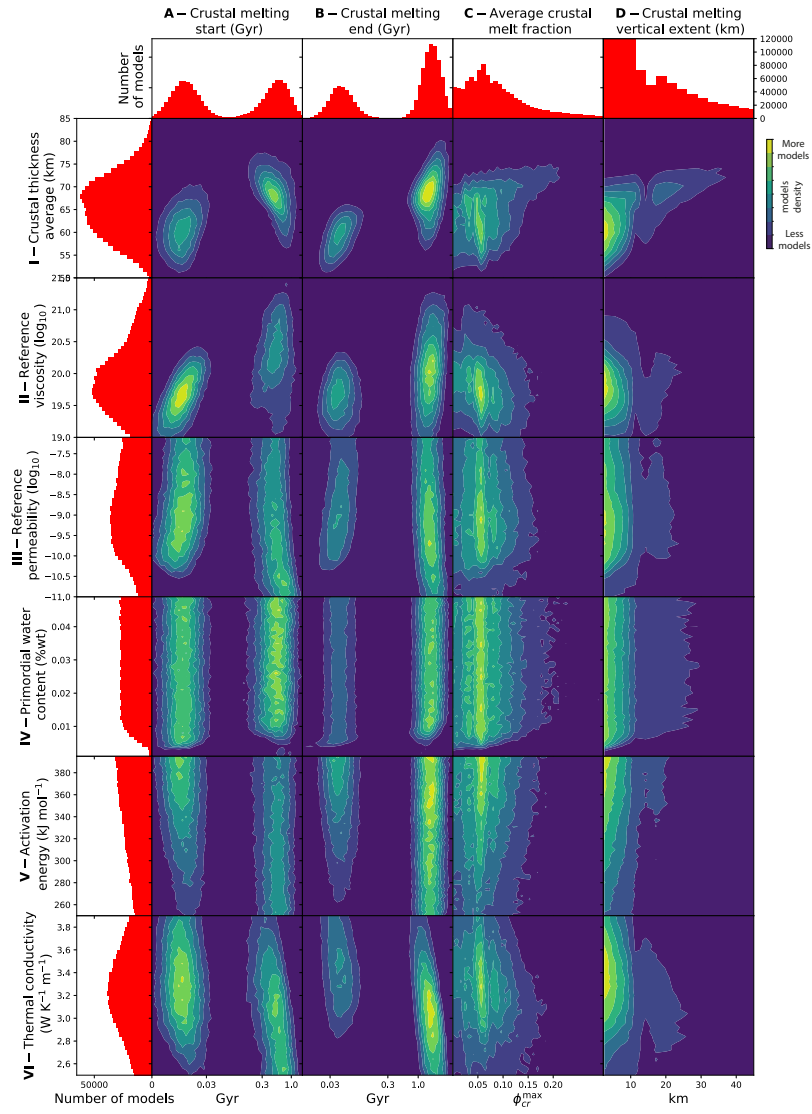
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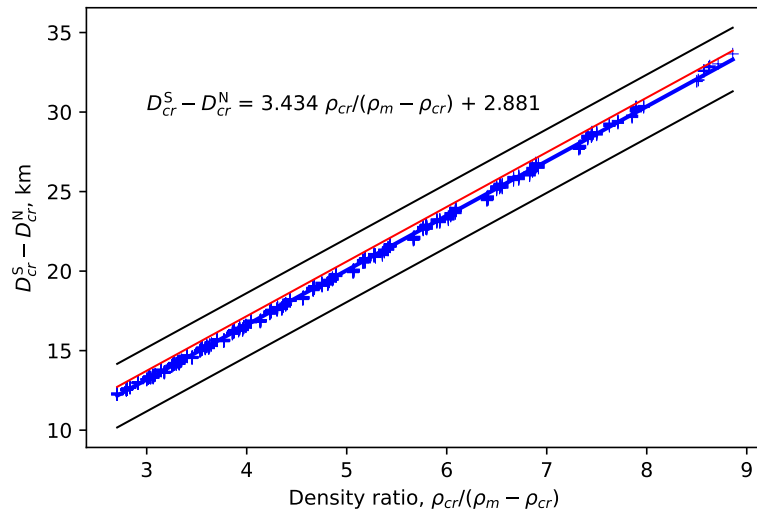
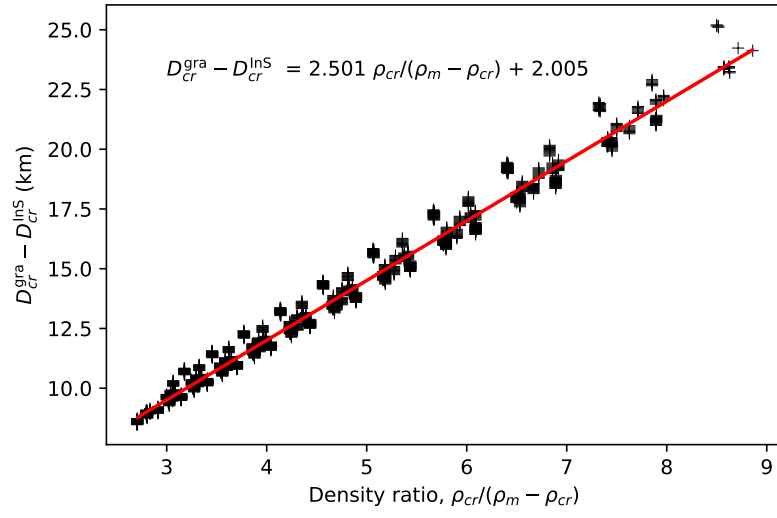
Abstract

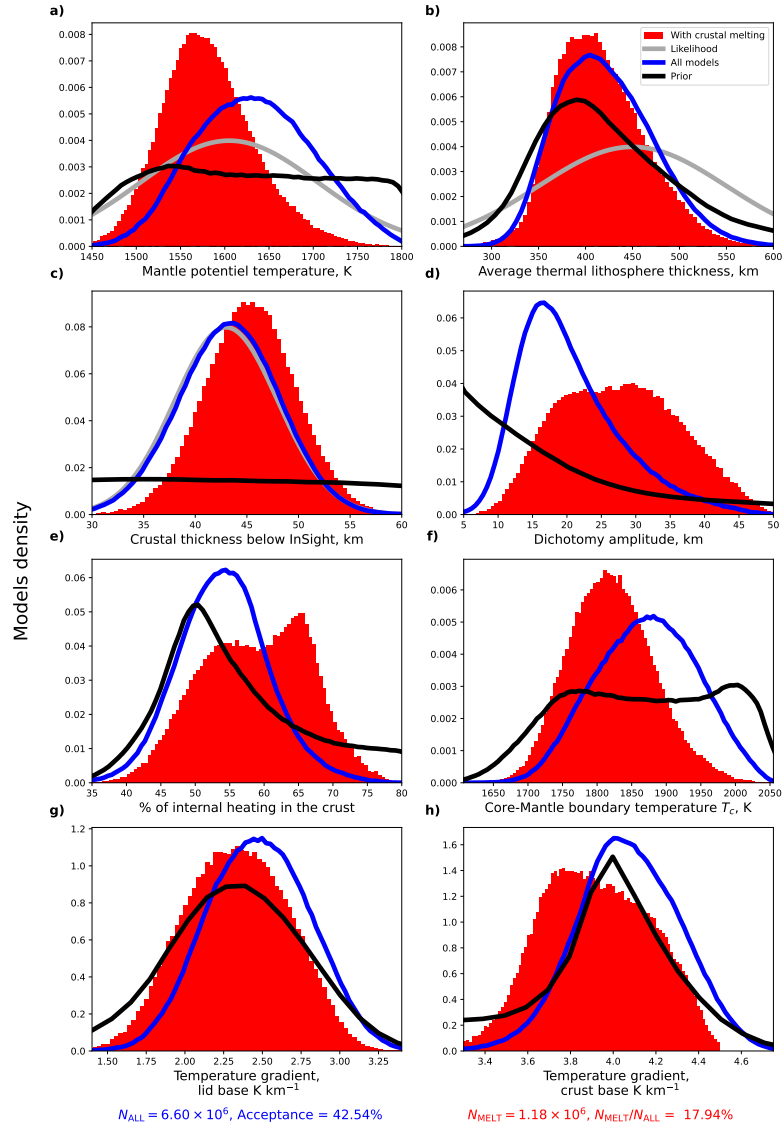
The Martian surface composition appears mainly mafic but recent observations have revealed the presence of differentiated rocks, only in the Highlands. Here, we demonstrate that differentiated melts can form during the construction of thick crustal regions on Mars by fractional crystallisation of a mafic protolith, without plate tectonics. On a stagnant-lid planet, regions of thicker crusts contain more heat-producing elements and are associated to thinner lithospheres and to higher mantle melt fractions. This induces larger crustal extraction rates where the crust is thicker. This positive feedback mechanism is favoured at large wavelengths and can explain the formation of the Martian dichotomy. We further develop an asymmetric parameterised thermal evolution model accounting for crustal extraction, where the well-mixed convective mantle is topped by two lithospheres (North/South) characterised by specific thermal and crustal structures. We use this model in a Bayesian inversion to investigate the conditions that allow crustal temperatures to be maintained above the basalt solidus during crustal growth, resulting in the formation of evolved melts.

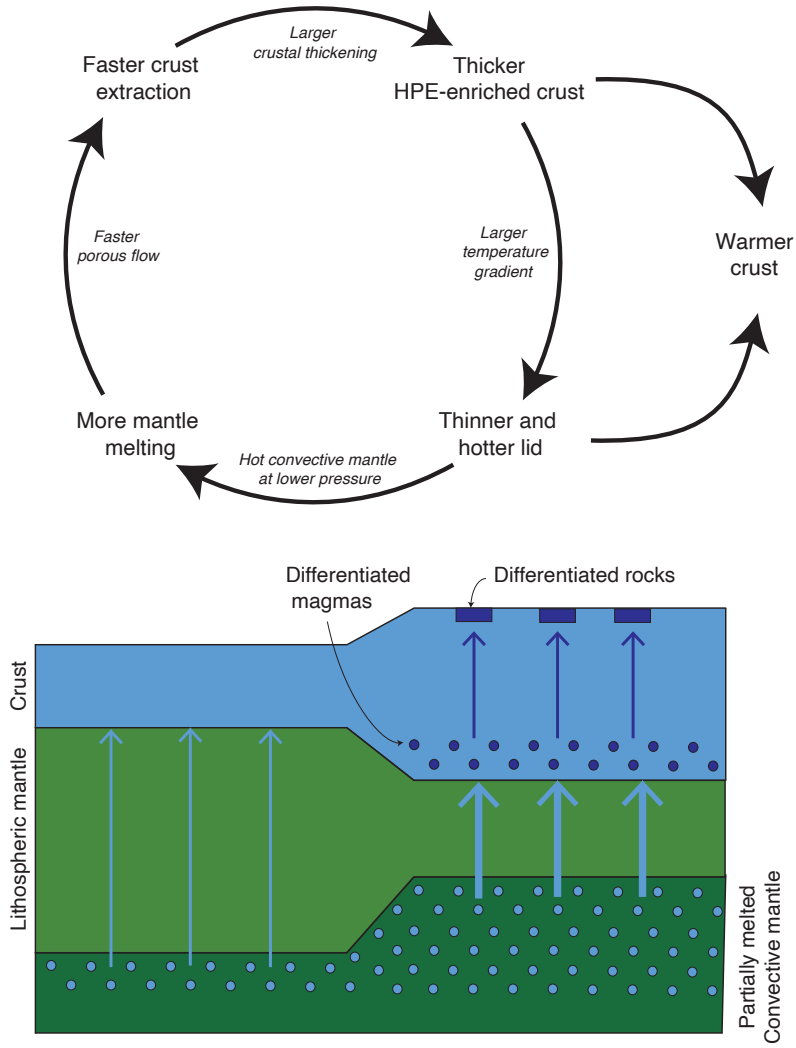
Among the thermal evolution models matching constraints on the structure of the Martian crust and mantle provided by the InSight NASA mission, a non-negligible fraction allows partial melting and differentiation of the crust in the south, which can occur very early (<100 Myr) as well as during the Hesperian ; partial melting in the north appears unlikely. Although crustal differentiation may occur on a hemispheric scale on Mars, its vertical extent is limited to less than a third of the crustal thickness.

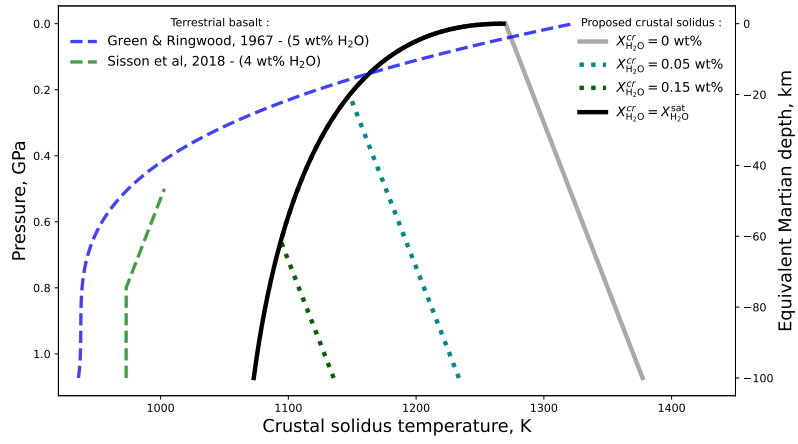












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Valentin Bonnet Gibet ¹, Chloé Michaut ^{1,2}, Thomas Bodin ¹, Mark
Wieczorek ³, Fabien Dubuffet ¹

¹Ecole Normale Supérieure de Lyon, Université de Lyon, Université Claude Bernard Lyon 1, Université
Jean Monet, CNRS, Laboratoire de Géologie de Lyon, Terre, Planètes, Environnement, F-69007 Lyon,
France.

²Institut Universitaire de France, Paris, France.

³Institut de Physique du Globe de Paris: Paris, France

Key Points:

- The Martian crust can partially melt at its base during its formation in the presence of a low amount of water and without plate tectonics.
- Partial melting of the crust occurs in regions of thick crust as the Highlands, where differentiated rocks are found.
- A non-negligible fraction of thermal evolution scenarios fitting InSight constraints show one or two episodes of crustal melting only in the Highlands.

Corresponding author: Valentin Bonnet Gibet, =valentin.bonnetgibet@proton.me=

Abstract

The Martian surface composition appears mainly mafic but recent observations have revealed the presence of differentiated rocks, only in the Highlands. Here, we demonstrate that differentiated melts can form during the construction of thick crustal regions on Mars by fractional crystallisation of a mafic protolith, without plate tectonics. On a stagnant-lid planet, regions of thicker crusts contain more heat-producing elements and are associated to thinner lithospheres and to higher mantle melt fractions. This induces larger crustal extraction rates where the crust is thicker. This positive feedback mechanism is favoured at large wavelengths and can explain the formation of the Martian dichotomy. We further develop an asymmetric parameterised thermal evolution model accounting for crustal extraction, where the well-mixed convective mantle is topped by two lithospheres (North/South) characterised by specific thermal and crustal structures. We use this model in a Bayesian inversion to investigate the conditions that allow crustal temperatures to be maintained above the basalt solidus during crustal growth, resulting in the formation of evolved melts. Among the thermal evolution models matching constraints on the structure of the Martian crust and mantle provided by the InSight NASA mission, a non-negligible fraction allows partial melting and differentiation of the crust in the south, which can occur very early (<100 Myr) as well as during the Hesperian; partial melting in the north appears unlikely. Although crustal differentiation may occur on a hemispheric scale on Mars, its vertical extent is limited to less than a third of the crustal thickness.

Plain Language Summary

While the surface of Mars appears mostly mafic, recent observations of differentiated rocks in the Highlands of Mars have questioned their origins and significance. Our study proposes that these rocks can form concomitantly to the growth of the crust, by fractional crystallisation of a mafic protolith in thick crustal regions. Thicker crusts contain more heat-producing elements, and are associated to hotter lithospheres and increased partial melt fractions in the mantle beneath and hence to larger crustal thickening rates. Temperatures in thicker crustal regions are thus more likely to reach the basalt solidus. By modeling the thermal evolution of Mars, we show that temperatures larger than the basalt solidus can be maintained during the growth of the Martian crust, but only in thick crustal regions, allowing the formation and extraction of differentiated melts. Among the thermal evolution models that are in agreement with the present-day thermal structure of Mars, as revealed by the NASA InSight mission, a significant number allows partial melting in the southern crust, in the very early history of Mars or during the Hesperian. Partial melting of the crust in the North does not seem likely.

1 Introduction

The composition of the Martian crust appears globally basaltic (G. J. Taylor, 2013). Martian meteorites have mafic to ultra-mafic compositions, as do a large proportion of the rocks observed in-situ by rovers. The grain density estimated from their petrology and from surface concentrations in Fe, Al, Ca, Si, and K measured by GRS data is rather high, between 3100 and 3300 kg m^{-3} , with potentially lower values in the Highlands (Baratoux et al., 2014). Topography and gravity data, on the other hand, suggest lower crustal density values. Pauer and Breuer (2008) constrained the average crustal density of the Highlands to values <3020 kg m^{-3} and Goossens et al. (2017) estimated an average density of 2582 ± 209 kg m^{-3} for the crust. Significant lateral density variations may exist between the Highlands, where the density could be as low as 1800 - 2000 kg m^{-3} , the northern plains, which seems on average denser than the South, and the recent volcanic massifs (Tharsis and Elysium), where the bulk density may reach 3000 - 3200 kg m^{-3} (Goossens et al., 2017). Variations in pyroxene Calcium content between Hesperian and Noachian

67 volcanic rocks cannot explain such large density differences (Mangold et al., 2010; Bara-
 68 toux et al., 2014). The presence of a mega-regolith with a high porosity ($\sim 10\%$) over a
 69 non-negligible portion of the crust, or of sedimentary rocks made of clays and sulfate (Wieczorek
 70 et al., 2022), may partly explain the low density values found in the Highlands. But, given
 71 their low contribution to the bulk crust, their effects are probably insufficient. It has thus
 72 been proposed that a large felsic component may be buried beneath the surface in the
 73 Highlands (Baratoux et al., 2014; Sautter et al., 2015).

74 Orbital observations have identified outcrops rich in silica (Christensen et al., 2005;
 75 Bandfield, 2006) or in iron-rich feldspar (Figure 1, red triangles, Carter & Poulet, 2013;
 76 Wray et al., 2013; Phillips et al., 2022; Payré et al., 2022) in the Highlands, that could
 77 represent felsic rocks, but their degree of differentiation is still debated (Phillips et al.,
 78 2022; Flahaut et al., 2023; Barthez et al., 2023). In parallel, a large diversity of igneous
 79 rocks has been detected in the Gale crater, from mafic rocks, typical of the Martian sur-
 80 face, to intermediate and evolved rocks, such as trachytes, dated to the Noachian/late
 81 Hesperian (Sautter et al., 2015; Cousin et al., 2017). A pair of meteorites, NWA 7034
 82 & NWA 7533, breccia fragments of the same parent meteorite, contain differentiated clasts
 83 ranging from intermediate to monazite in composition, mixed with larger basaltic and
 84 gabbroic clasts (Agee et al., 2013). The formation of this breccia occurred only 225 Myr
 85 ago, but felsic clasts are as old as 4.35 to 4.49 Gyr (Costa et al., 2020; Cassata et al., 2018),
 86 indicating that felsic rocks were present on early Mars. Unlike other Martian meteorites,
 87 this breccia appears to be representative of the Martian Highlands, because of its high
 88 concentration in Fe, K and Th, its strong magnetic signature and the ancient crystalli-
 89 sation ages of its minerals. The crater Khujirt, located in the north-east of the Terra Cimmeria-
 90 Sirenum province, in the Southern Hemisphere of Mars, was identified as the possible
 91 ejection site (Lagain et al., 2022). In addition, several feldspar-rich outcrops of poten-
 92 tially evolved composition have been detected by visible/near-infrared spectroscopy in
 93 this province (Payré et al., 2022), which concentrates many evidence for the presence of
 94 felsic rocks.

95 Observations of differentiated rocks are all located in the Highlands (Figure 1), which
 96 present a high topography and ancient terrains contrasting with the low topography and
 97 younger terrains of the North. Assuming a uniform crustal density, the hemispheric dif-
 98 ference in topography would be caused by a difference in crustal thickness. But if the
 99 Highlands contain a buried felsic component, its bulk density could be lower than that
 100 of the Northern crust, which would explain at least part of the dichotomy in topogra-
 101 phy (Knappmeyer-Endrun et al., 2021; Wieczorek et al., 2022). With a North-South crustal
 102 density contrast of $200\text{-}300\text{ kg m}^{-3}$, a prominent difference in average crustal thickness
 103 between the north and south would no longer exists. It is therefore important to under-
 104 stand the mechanism behind the formation of these differentiated rocks to constrain the
 105 bulk crustal density of these geological provinces and the nature of the dichotomy.

106 A primary origin for the remotely-detected feldspar-rich rocks has been proposed,
 107 in particular because the remote detection of plagioclase is difficult and may require an
 108 enrichment of over 90% in anorthite, as in the lunar Highlands (Wieczorek et al., 2022;
 109 Carter & Poulet, 2013; Wray et al., 2013). But the formation of an anorthosite flotation
 110 crust seems more difficult on Mars than on the Moon (Elkins-Tanton et al., 2003; Elkins-
 111 Tanton, 2012; Collinet et al., 2015): anorthite crystals are stable at pressures below ~ 1
 112 GPa, i.e. only over the first hundred of kilometers on Mars, and the presence of water
 113 also reduces the stability of plagioclase (Lin et al., 2017). Alternatively, large Ca-rich
 114 plagioclase crystals may be more easily detected by remote-sensing (Barthez et al., 2023),
 115 which would require anorthite concentration of only $\sim 30\text{-}80\%$. Nyquist et al. (2016) also
 116 proposed that the evolved clasts of NWA 7034 formed similarly to lunar KREEP-enriched
 117 rocks, that is, by extraction of residual melts enriched in incompatible elements from the
 118 crystallising magma ocean. But crystallisation experiments have shown that the melt
 119 composition remains predominantly basaltic until the end of crystallisation of the Mar-

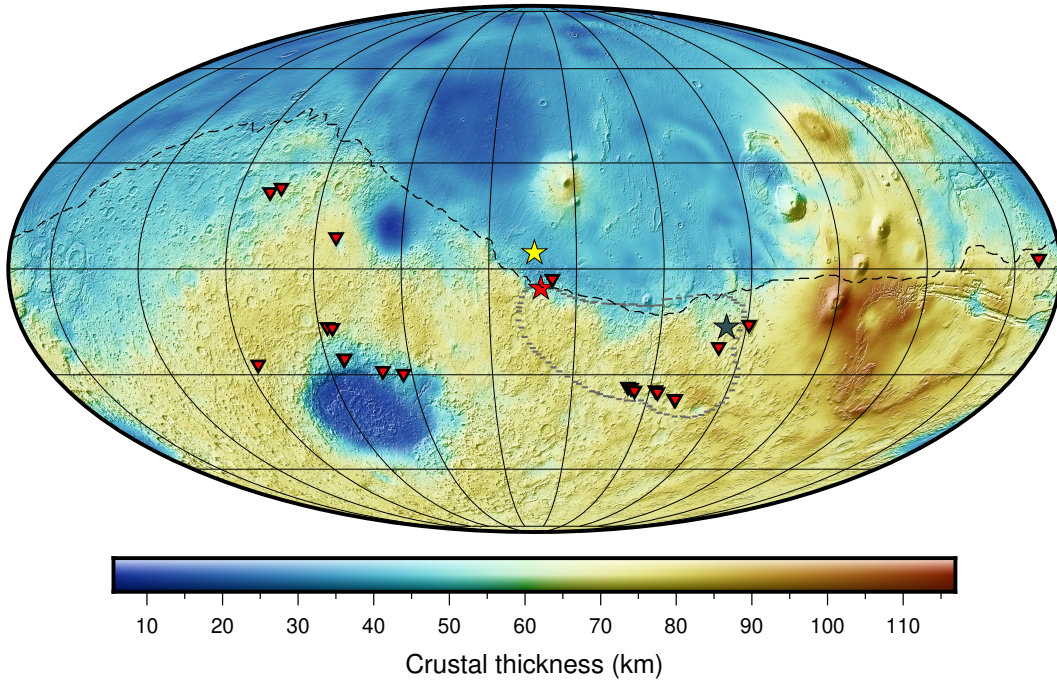


Figure 1. Locations of feldspar-rich and evolved rocks superposed on a crustal thickness map of Mars. This crustal thickness map was built considering a uniform crustal density of 2900 kg m^{-3} , the mantle density model of Khan et al. (2021) and a crustal thickness at the InSight landing site (yellow star) of 39 km (Wieczorek et al., 2022; Knapmeyer-Endrun et al., 2021). This map is presented on a Mollweide projection with a central meridian of 136°E longitude. Black dashed line: dichotomy boundary of Andrews-Hanna et al. (2008), dotted grey line: boundary of the Terra Cimmeria-Sirenum province (Bouley et al., 2020), red star: location of the Gale crater (Cousin et al., 2017), grey star: location of the Khujirt crater (Lagain et al., 2022), red triangles: locations of feldspar-rich outcrops revealed by orbital spectroscopy (Carter & Poulet, 2013; Wray et al., 2013; Phillips et al., 2022; Payré et al., 2022).

120 tian mantle (Collinet et al., 2015). Impacts may also bring felsic material to Mars (Payré
 121 et al., 2022), or generate partial melt of evolved composition (Black & Marchi, 2024).
 122 However, the rocks found at Gale crater form a magmatic series from a basaltic protolith
 123 (Sautter et al., 2015), which argues in favour of their secondary origin. Their chemistry
 124 and mineralogy appear similar to those of differentiated terrestrial intraplate volcanic
 125 rocks (Udry et al., 2018), suggesting that they formed by fractional crystallisation, in
 126 presence of water, of an ultramafic or mafic melts similar in composition to the Martian
 127 crust.

128 On one-plate planets like Mars, the crustal thickness exerts a positive feedback on
 129 the extraction of mantle melts. As the crust concentrates heat-producing elements, the
 130 lithosphere is hotter in regions of thicker crusts (Thiriet et al., 2018). The mantle melt
 131 fraction is, in turn, higher and the rates of melt extraction and crustal thickening are
 132 thus higher where the crust is thicker. This mechanism enables the formation of geolog-
 133 ical provinces of thick crust at large wavelengths, in particular at the hemispheric scale,
 134 as the effectiveness of conductive cooling is increased at smaller wavelengths ; this mech-
 135 anism can thus explain the Martian dichotomy (Figure 2, Bonnet Gibet et al., 2022). This
 136 mechanism further implies that regions of thicker crusts are characterized by an increased
 137 magmatism and are marked by higher temperatures. Here, we investigate whether crustal
 138 temperatures may be maintained above the basalt solidus temperature during crust con-
 139 struction, i.e. if partial melting can be sustained in the deep part of the crust, in par-
 140 ticular in regions of thick crust. If such a layer is stable over time, secondary evolved melts
 141 could be extracted and form differentiated rocks, enriched in water and silica. In this sce-
 142 nario, felsic rocks would form concomitantly to the crust and dichotomy on Mars. This
 143 could explain the observed spatial correlation between outcrops of differentiated rocks
 144 and thick crustal provinces on Mars (Figure 2).

145 To explore this scenario, we use and develop further the asymmetric 1D thermal
 146 evolution model described in Bonnet Gibet et al. (2022) to estimate the amount of par-
 147 tial melting in the crust over time. We first describe the modifications brought to our
 148 physical model and illustrate a specific thermal evolution that shows two episodes of par-
 149 tial melting in the Southern crust. To estimate the probability of Martian crust differ-
 150 entiation given our current knowledge on the thermal state of Mars, we use our thermal
 151 model in a Bayesian inversion based on the recent constraints on Mars’ structure (crustal
 152 thickness and mantle thermal state) provided by the NASA InSight mission. This in-
 153 version gives a set of thermal evolutions, each defined by an ensemble of parameters, that
 154 reproduce the observations from InSight. We study the subset of inverted thermal evo-
 155 lutions that are able to sustain partial melting and differentiation of the crust in the South.
 156 We finally discuss the differences between the two sets of evolutions.

157 2 Thermal evolution modelling

158 For this work, we use the thermal modelling developed in Bonnet Gibet et al. (2022)
 159 incorporating some previously neglected physics that seems important to consider for
 160 this study. This thermal model assumes a well-mixed convective mantle, with a temper-
 161 ature T_m at its top, overlaid by a conductive lid split in two different hemispheres (North
 162 and South) evolving independently. Each hemisphere has its own crustal thickness $D_{cr}^{N/S}$,
 163 lid thickness $D_l^{N/S}$ and temperature profile in the lid $T(r)^{N/S}$, where superscript N/S
 164 stands for North and South respectively. Bonnet Gibet et al. (2022) provided a complete
 165 description of this model, but its essential ingredients are recalled in Appendix A. To
 166 obtain a better resolution of the temperature profile in the lid, the heat source term due
 167 to magmatism is better specified. We also consider the cooling caused by the downward
 168 advection of material in the lid associated to magma eruption and intrusion in the crust,
 169 which was previously neglected. Finally, we parameterise a basalt solidus for the crust
 170 of Mars and calculate the melt fraction in the crust as a function of depth. We neglect

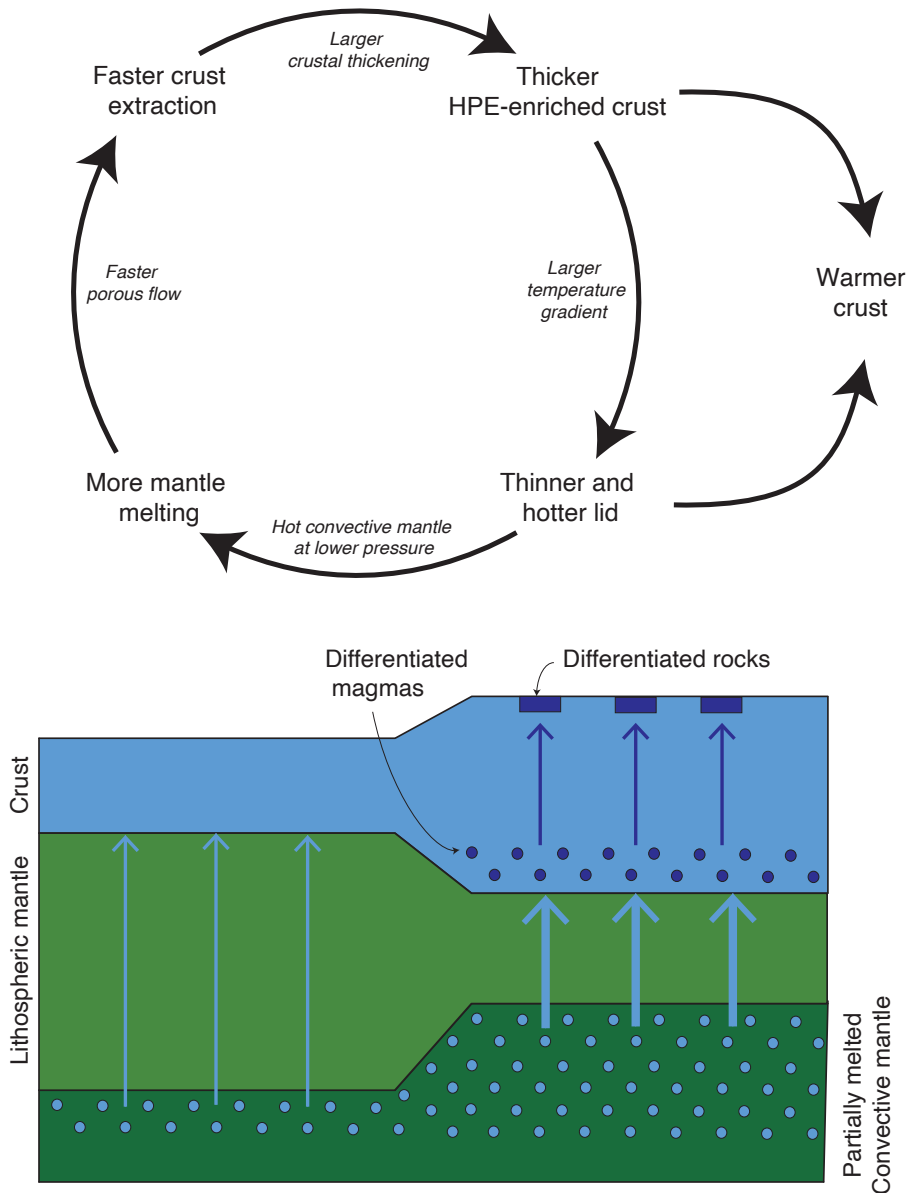


Figure 2. Conceptual diagram showing the positive feedback of the crust thickness on melt extraction. The crust is enriched in heat-producing elements leading to larger lithospheric temperatures where the crust is thicker. The rheological temperature marking the boundary between the convective mantle and the lid is reached at shallower depths, i.e. the lid is thinner, below a thicker crust. The well-mixed convective mantle rises to lower pressures and mantle melt fractions are higher below thinner lids because of the pressure-dependence of the solidus. By Darcy’s law, the extraction rate is higher where the melt fraction is more important. Therefore, larger thickening rates are expected where the crust is thicker. This mechanism also implies that the base of the crust is hotter, and partial melting more likely, where the crust is thicker. Extraction of evolved partial melts could lead to differentiated rocks at shallower depths.

171 the thermal effects induced by extraction and eruption of differentiated crustal melts that
 172 may form.

173 2.1 Heat equation

174 In each hemisphere, we solve for the diffusion equation in spherical geometry over
 175 the lid thickness accounting for the heat brought by magmatism H^{mag} , downward ad-
 176 vection of lithospheric material at velocity $u(r)$ caused by crust growth as well as crustal
 177 melting:

$$\rho(r)c(r) \left[\left(1 + a(r) \frac{L(r)}{c(r)\Delta T^{\text{ls}}(r)} \right) \frac{\partial T}{\partial t} + u(r) \left(\frac{\partial T}{\partial r} + \frac{L(r)}{c(r)} \frac{\partial \phi}{\partial r} \right) \right] = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 k(r) \frac{\partial T}{\partial r} \right) + H^{\text{rad}}(r, t) + H^{\text{mag}}(r, T, t), \quad (1)$$

178 where $k(r)$ is the thermal conductivity, equal to k_{cr} in the crust and k_m in the mantle,
 179 $c(r)$ is the heat capacity, equal to c_m in the mantle and c_{cr} in the crust, $L(r)$ is the la-
 180 tent heat of melting (J kg^{-1}) equal to L_m in the mantle and L_{cr} in the crust and $\rho(r)$
 181 is the density, equal to ρ_{cr} in the crust and ρ_m in the mantle. Magmatism induces a heat-
 182 ing term noted $H^{\text{mag}}(r, T, t)$ that depends on crustal temperatures and the fraction of
 183 basal and bulk intrusive magmatism (see Section 2.2.1); it is assumed equal to zero in
 184 the lithospheric mantle. Downward advection of colder material and hence heat occurs
 185 at velocity $u(r)$, which depends on the crustal growth rate (see Section 2.2.2) and on the
 186 temperature and melt fraction gradients. We neglect changes in the thermodynamic pa-
 187 rameters of the crust caused by melting, as melt fractions in the crust remain low. Crustal
 188 melting is added as a heat source/sink term, function of the secular cooling term, the
 189 Stefan number for the crust $St(r) = c(r)\Delta T^{1-s}(r)/L(r)$, and a parameter $a(r)$, where
 190 $a(r) = 1$ if the melt fraction $\phi(r)$ is larger than 0, $a(r) = 0$ if $\phi(r) = 0$ or 1. $\Delta T_r^{\text{ls}} =$
 191 $T_{\text{liq}}(r) - T_{\text{sol}}(r)$ is the difference between the liquidus and solidus of the crust (See Sec-
 192 tion 2.3, Equations 6 & 12).

193 2.2 Magma emplacement

194 2.2.1 Magma heating

195 We neglect heat loss during magma ascent from the base of the lid to the crust and
 196 assume that magma intrudes the crust at the temperature of the lid base T_l . The heat
 197 source term caused by magma cooling in the crust depends on how the magma is dis-
 198 tributed within the crust. We consider that a fraction of magma f_{mag} intrudes the crust
 199 while a fraction $1 - f_{\text{mag}}$ erupts at the surface. The intrusive fraction is itself divided
 200 into a basal component noted as "basal magmatism" f_{base} , deposited at the crust base,
 201 while the fraction $1 - f_{\text{base}}$ distributes uniformly in the crust as "crustal intrusions". We
 202 consider that the heat released by volcanism at the surface is instantaneously evacuated.
 203 The heat source term caused by magmatism depends thus on the crustal temperature
 204 and radius and writes:

$$H^{\text{mag}}(r > R_{\text{cr}}) = w \frac{A_{\text{cm}}}{V_{\text{cr}}^{\text{N/S}}} \rho_{\text{cr}} \left[L_{\text{cr}} (1 - \phi(r)) + c_{\text{cr}} (T_l - T(r)) \right] f_{\text{mag}} (1 - f_{\text{base}}), \quad (2)$$

$$H^{\text{mag}}(R_{\text{cr}}) = w A_{\text{cm}} \rho_{\text{cr}} \left[L_{\text{cr}} (1 - \phi(R_{\text{cr}})) + c_{\text{cr}} (T_l - T_{\text{cr}}) \right] f_{\text{mag}} \left(\frac{(1 - f_{\text{base}})}{V_{\text{cr}}^{\text{N/S}}} + \frac{f_{\text{base}}}{dV_{\text{cr}}} \right), \quad (3)$$

where the crust-mantle boundary is at radius R_{cr} and temperature T_{cr} , w is the melt percolation velocity at the interface between the lid and mantle, of radius R_l , and area A_{cm} . dV_{cr} is the volume element heated by basal magmatism.

2.2.2 Downward advection due to crustal growth

Magma intrusion and crustal thickening lead to the downward displacement of underlying crustal and lid materials. This acts to cool down the lid as it brings colder material downward, which limits heating by magmatism. This effect is generally neglected in parameterised thermal evolution studies (Breuer & Spohn, 2006; Morschhauser et al., 2011), in particular because the Péclet number ($\frac{D_l w}{\kappa}$) is less than one (Foley & Smye, 2018). In the new version of our model, we account for this effect, as it can limit the rise in crustal temperatures associated to magmatism.

The distribution of magma intrusions and extrusions determines the downward advection: extrusive volcanism causes downward displacement of the entire crust and lid, while basal magmatism leads to the downward advection of the lithospheric mantle only. The downward displacement velocity $u(r)$ in the crust ($r > R_{cm}$) and in the lithospheric mantle ($r \leq R_{cm}$) due to volcanism and magmatism is obtained by volume conservation:

$$u(r > R_{cr}) = -(1 - f_{\text{mag}}) \times w \left(\frac{R_l}{r} \right)^2 - (1 - f_{\text{base}}) \times f_{\text{mag}} \times w \frac{R_l^2}{r^2} \frac{R_p^3 - r^3}{R_p^3 - R_{cr}^3}, \quad (4)$$

$$u(r \leq R_{cr}) = -w \times \left(\frac{R_l}{r} \right)^2, \quad (5)$$

where R_p is the radius of Mars.

2.3 Partial melting of the crust

A characteristic solidus for the Martian crust has not yet been proposed. We thus rely on existing experiments on terrestrial basaltic analogues to propose an approximate solidus for Mars that depends on pressure and crust water content, as the solidus of mafic rocks is strongly modified by addition of water. For the Earth, the solidus of rocks with basaltic compositions has been determined for subduction settings where the rocks are often altered and/or enriched in water (Green & Ringwood, 1967; Peacock et al., 1994; Sisson & Kelemen, 2018). The water composition of the Martian primordial mantle is estimated between 1 and 1000 ppm (Mysen et al., 1998; Johnson et al., 1991) which is not sufficient to significantly affect the melting temperature of the Martian mantle. Still, as water behaves as an incompatible element, the Martian crust may be enriched in water compared to the mantle. As water and heat-producing elements share similar partition coefficients (Aubaud et al., 2004), the crust of Mars may be similarly enriched in water and heat-producing elements, i.e. 10 to 15 times more enriched than the primitive mantle (Thiriet et al., 2018). But, even considering the highest possible enrichment of 1.5 wt %, the Martian crust water enrichment still seems much lower than that of terrestrial basalt ($\simeq 2-5\%$ Green & Ringwood, 1967; Peacock et al., 1994; Sisson & Kelemen, 2018). Such a water concentration is however close to that for a terrestrial mantle enriched in water (Katz et al., 2003). Basaltic rocks being chemically and mineralogically relatively similar to mantle rocks, we parameterise our crustal solidus similarly to Katz et al. (2003), as a function of the melt fraction water content X_{H_2O} and pressure P , in GPa, with a classical slope of 100 K GPa^{-1} :

$$T_{\text{sol}}^{\text{cr}}(P, X_{H_2O}) = T_{\text{sol}}^{\text{cr},0} + 100P - \Delta T(X_{H_2O}), \quad (6)$$

245 where $T_{\text{sol}}^{\text{cr}}$ is in Kelvin. $T_{\text{sol}}^{\text{cr},0}$ is the Martian crustal solidus temperature in K at zero pressure,
 246 defined as $T_{\text{sol}}^{\text{cr},0} = T_{\text{sol}}^{\text{Earth},0} - \Delta T_{\text{Fe}}$, where $T_{\text{sol}}^{\text{Earth},0}$ is the typical solidus temper-
 247 ature at zero pressure for a terrestrial basalt (1323 K, Peacock et al., 1994) and ΔT_{Fe}
 248 is a correction accounting for different #Mg between the bulk silicate part of the Earth
 249 and that of Mars. We use a temperature difference of 50 K as estimated by Collinet et
 250 al. (2015) for the difference in solidus between the Martian mantle and that of the Earth.
 251 $\Delta T(X_{\text{H}_2\text{O}})$ is the decrease in the solidus temperature caused by addition of water in the
 252 melt, which we express as a power law, function of the water content in the melt in wt%:

$$\Delta T(X_{\text{H}_2\text{O}}) = K X_{\text{H}_2\text{O}}^\gamma, \quad (7)$$

253 where we use $K = 43$ and $\gamma = 0.75$ K wt% $^{-\gamma}$ as in Katz et al. (2003) for the terres-
 254 trial mantle solidus. The water content in the melt at the solidus ($\phi_{\text{cr}} = 0$) is obtained
 255 assuming chemical equilibrium:

$$X_{\text{H}_2\text{O}} = \frac{X_{\text{H}_2\text{O}}^{\text{cr}}}{\phi + (1 - \phi_{\text{cr}})D_i} = \frac{\Lambda_{\text{cr}} X_{\text{H}_2\text{O}}^{\text{p}}}{D_i}, \quad (8)$$

256 with $X_{\text{H}_2\text{O}}^{\text{p}}$ the water content of the bulk silicate part of Mars, Λ_{cr} the crustal enrich-
 257 ment in water relative to the primitive mantle. We assume the same partition coefficient
 258 D_i for water and heat-producing elements (Aubaud et al., 2004) ; the crustal enrichment
 259 in water is thus the same as that of heat-producing elements.

260 The decrease in solidus temperature associated to the addition of dissolved water
 261 in the melt is limited by water saturation:

$$\Delta T(X_{\text{H}_2\text{O}} > X_{\text{H}_2\text{O}}^{\text{sat}}) = \Delta T(X_{\text{H}_2\text{O}}^{\text{sat}}), \quad (9)$$

262 where $X_{\text{H}_2\text{O}}^{\text{sat}}$ is the maximum water content in the melt, which depends on pressure fol-
 263 lowing:

$$X_{\text{H}_2\text{O}}^{\text{sat}} = 12P^{0.6} + P, \quad (10)$$

264 where P is expressed in GPa and $X_{\text{H}_2\text{O}}^{\text{sat}}$ is in wt% (Katz et al., 2003). A water content
 265 similar to that of the primitive mantle as proposed by G. J. Taylor (2013) (i.e. $300 \pm$
 266 150 ppm) is sufficient to significantly decrease the crustal solidus temperature compared
 267 to the anhydrous one (Figure 6).

268 The crustal melt fraction is then assumed to be a linear function of temperature
 269 over the melting interval:

$$\phi^{\text{cr}}(r) = \frac{T(r) - T_{\text{sol}}^{\text{cr}}(r)}{T_{\text{liq}}^{\text{cr}}(r) - T_{\text{sol}}^{\text{cr}}(r)}, \quad (11)$$

270 where $T_{\text{liq}}^{\text{cr}}(r)$ is the crustal liquidus in Kelvins, equal to the anhydrous solidus plus a con-
 271 stant:

$$T_{\text{liq}}^{\text{cr}}(P) = T_{\text{sol}}^{\text{cr},0} + 100P + 330. \quad (12)$$

272 With this parameterisation, we establish a saturation solidus (Figure 3, black curve) where
 273 the melt water content consistently equals saturation, maximizing the impact of water.
 274 At zero pressure, this solidus is similar to the anhydrous case ; it progresses to lower tem-

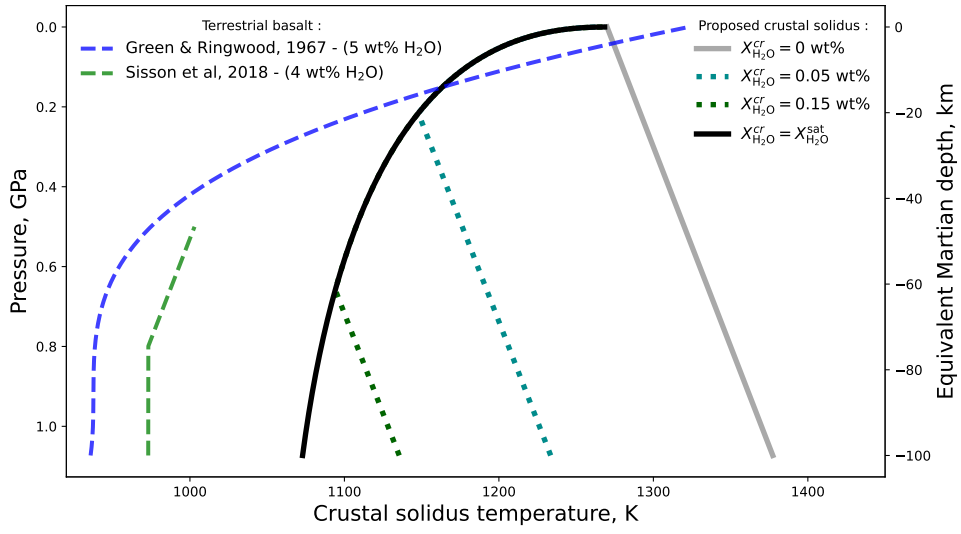


Figure 3. Crustal solidus temperature $T_{\text{sol}}^{\text{cr}}$ as a function of pressure (in GPa) and equivalent Martian depth (in km) assuming a crustal density of 2900 kg m^{-3} and a gravity of $3.7 \text{ m}^2 \text{ s}^{-1}$. The solid and dotted curves represent the Martian crustal solidus for increasing values of water content in the crust $X_{\text{H}_2\text{O}}^{\text{cr}}$ from 0 to 1500 ppm with 500 ppm increments. The black solidus curve is the solidus at water saturation ($X_{\text{H}_2\text{O}} = X_{\text{H}_2\text{O}}^{\text{sat}}$). The grey solid curve is the anhydrous solidus. Different water-saturated solidus for terrestrial basalts are plotted for comparison in dashed lines as a function of pressure.

275 peratures for increasing pressures and depths. Our saturated solidus behaviour aligns
 276 with that proposed by Green and Ringwood (1967) or Sisson and Kelemen (2018) for
 277 terrestrial basalts in subduction zones (dashed curves on Figure 3), although terrestrial
 278 basalts show a steeper slope caused by a higher water content. If the melt becomes un-
 279 dersaturated at some depth, the crustal solidus slope transitions to the anhydrous slope
 280 (Figure 3, dotted coloured curves). The solidus curves are similar to those described in
 281 Peacock et al. (1994).

282 **3 An example of thermal evolution with crustal melting**

283 Our model is numerically solved to determine the thermal evolution of Mars and
 284 the extraction of the crust over 4.5 Gyr from a given initial state (see Bonnet Gibet et
 285 al., 2022, for details on the numerical resolution). The example shown in Figure 4 illus-
 286 trates a classical thermal evolution for commonly used parameters (Table A1) ; it fea-
 287 tures two typical episodes of partial melting in the crust. As shown in Bonnet Gibet et
 288 al. (2022), two stages of crustal extraction can occur: an early and a late one (Figure 4b).
 289 An episode of crustal melting may occur towards the end of each crustal extraction stage
 290 if those stages are important and rapid enough (Figure 4d-e).

291 During the first phase of crustal extraction, a thick crust rapidly forms in both hemi-
 292 spheres, within a timescale typically less than ~ 100 Myr (~ 40 Myr for the example
 293 of Figure 4). The early rapid thickening of the crust is caused by the initially large man-
 294 tle melt fraction ($\sim 18\%$ at 0 Gyr). Temperatures at the base of the crust then rise rapidly
 295 and can reach the solidus in the South, as in this example (Figure 4c), where crustal melt-
 296 ing occurs between 6 and 91 Myr (Figure 4e). As the mantle cools and its melt fraction
 297 decreases, it becomes smaller than the critical value for melt extraction, which impedes
 298 crustal thickening during ~ 200 Myr (Figure 4b). The crustal temperature decreases
 299 and passes below the crustal solidus (Figure 4c-e). Meanwhile, the convective mantle tem-
 300 perature increases because of radiogenic heating, while the lid slowly thickens in the North
 301 and stabilises around 150 km in the South (Figure 4a). As a result, the mantle melt frac-
 302 tion increases, and crustal extraction can start again, but only in the South, where the
 303 lid is thinner and the melt fraction higher (Figure 4b). During this second phase of crustal
 304 thickening in the South, the temperature at the base of the crust starts to rise again at
 305 $\simeq 300$ Myr (Figure 4b); it exceeds the solidus after ~ 867 Myr (Figure 4e). This sec-
 306 ond crustal melting event takes place in the South at the end of crust formation and is
 307 sustained for more than 500 Myrs (Figure 4d-e).

308 During the first episode of crustal melting, the average crustal melt fraction reaches
 309 12% in the south over a maximum vertical extent of 8 km but partial melting lasts only
 310 for a short duration (<90 Myr). During the second episode, the amplitude of the melt-
 311 ing is less important, as the average crustal melt fraction reaches 4% over 3 km, but the
 312 episode lasts much longer, ~ 688 Myr in this case (Figure 4d-e). The base of the crust
 313 remains partially molten until $\simeq 1.55$ Gyr, more than 300 million years after the end of
 314 crust formation (Figure 4d-e). After this last phase of extraction, the thickness of the
 315 crust remains constant (Figure 4a), the temperature of the convective mantle decreases
 316 and the stagnant lid thickens (Figure 4c) which impedes further crustal melting.

317 **4 Inversion with a Monte Carlo Markov chain algorithm**

318 Our thermal evolution example shows that it is possible to reach the conditions for
 319 partial melting at the base of the southern crust during crustal extraction for a given set
 320 of parameters. However, this direct approach does not tell us how likely such an episode
 321 is. To infer its significance, we first need to define a set of thermal evolution scenarios
 322 that are plausible given our current knowledge on the structure and thermal state of Mars.
 323 To that aim, an inverse problem is formulated in a Bayesian framework, to estimate the
 324 probability of different thermal evolution scenarios, given observations and results of the

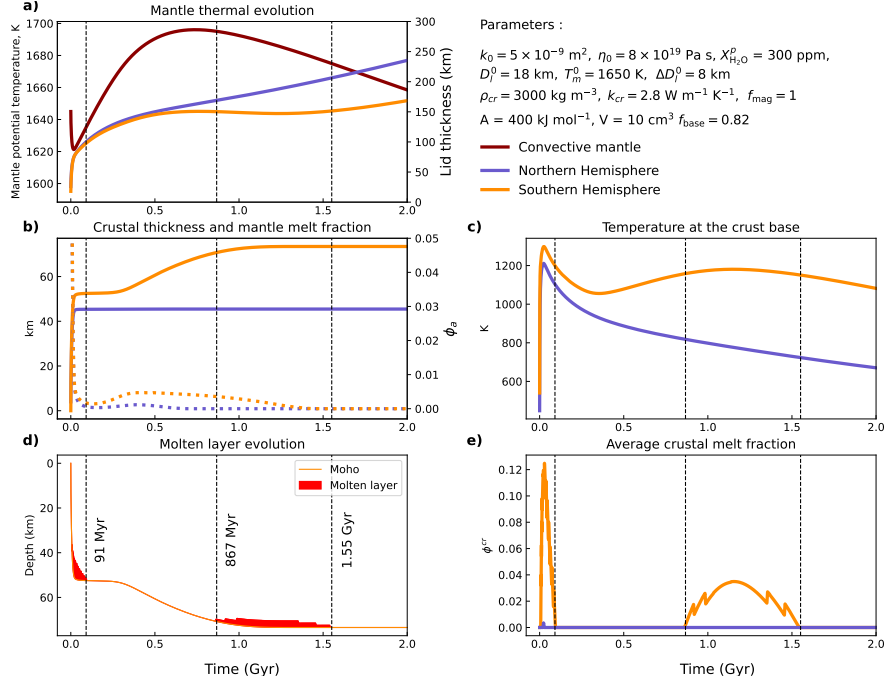


Figure 4. Thermal evolution for a specific case with crustal melting. Evolution of **a)** the lid thickness D_l , (left y-axis) and potential mantle temperature T_p (red line, right y-axis), **b)** crustal thickness D_{cr} and average mantle melt fraction ϕ_a (dotted lines) **c)** the temperature at the base of the crust, **d)** thickness and depth of the molten layer (in red) in the crust in the South and **e)** average crustal melt fraction ϕ_{cr}^{avg} . We define the average crustal melt fraction as the volumetric average of the melt fraction over the partially molten crustal volume. Dotted black lines indicate the different stages of crustal melting.

325 NASA InSight mission. The inversion is based on a Markov Chain Monte Carlo sampling
 326 algorithm, which, through a random walk in our parameter space, defines a collection
 327 of models (each model being defined by a set of parameters) that approximates the prob-
 328 ability function of our model parameters given the observational constraints.

329 4.1 Formulation of the Bayesian inverse problem

A Bayesian inference is used to formulate our inverse problem following the formal-
 ism proposed by Gallagher et al. (2009) and based on Bayes' equation (Bayes, 1763):

$$p(\mathbf{m}|\mathbf{d}) \propto p(\mathbf{d}|\mathbf{m}) p(\mathbf{m}), \quad (13)$$

330 where \mathbf{m} represents the parameters of our thermal evolution model and \mathbf{d} represents our
 331 "data", which consist in observational constraints on the structure and thermal state of
 332 Mars from the InSight mission. $p(\mathbf{m})$ is the prior probability of these parameters and
 333 therefore of the associated thermal evolution model. $p(\mathbf{d}|\mathbf{m})$ is the likelihood of our ob-
 334 servational data, i.e. the probability of \mathbf{d} conditional on our model parameters. $p(\mathbf{m}|\mathbf{d})$
 335 is the posterior probability of the model parameters which we want to reconstruct us-
 336 ing an inversion.

337 4.2 Prior distribution

338 The prior probability $p(\mathbf{m})$ summarises what we know about our model paramete-
 339 rs. Here, we invert 11 parameters, listed in Table 1 ; the other parameters, held con-
 340 stant, are listed in Table A1. Since we have no specific prior information on these inverted
 341 parameters, except for a possible range of values, a uniform probability law is assumed.
 342 Thus, the prior probability is 1 for a model whose set of parameters lies within the space
 343 defined in Table 1 ; its prior probability is 0 if it lies outside this space. In addition, we
 344 set to 0 the prior probability of models that encounter the situation where the crust be-
 345 comes as thick as the lithosphere, as it is not entirely clear whether the buoyancy of the
 346 crust allows its survival and further growth despite thermal convection (Bonnet Gibet
 347 et al., 2022; Batra & Foley, 2021). Furthermore, these scenarios differ significantly from
 348 the solutions we are looking for, as they result in too-thick crusts and/or excessively large
 349 dichotomies (Bonnet Gibet et al., 2022) ; in addition they require very long calculation
 350 times.

351 4.3 Likelihood function

352 A thermal evolution scenario generate outputs, obtained during or at the end of
 353 the evolution. Some of these outputs can be compared to observations on Mars, thus pro-
 354 viding predictions ; they are called forecasts. We use four different observational con-
 355 straints from InSight, described in Section 4.4, which consist in the "data". The data vec-
 356 tor \mathbf{d} is composed of the crustal thickness below InSight $D_{\text{InS}}^{\text{calc}}$, the amplitude of the di-
 357 chotomy in crustal thickness $\Delta D_{\text{cr}}^{\text{calc}}$, the mantle potential temperature T_p^{calc} and the av-
 358 erage thickness of the thermal lithosphere D_L^{calc} . To evaluate the likelihood of the data,
 359 we use a Gaussian probability distribution in its general form (Gallagher et al., 2009):

$$p(\mathbf{d}|\mathbf{m}) = \frac{1}{(2\pi)^{N/2} |\mathbf{V}|^{N/2}} \exp \left\{ -\frac{1}{2} ((\mathbf{d} - g(\mathbf{m}))^t |\mathbf{V}|^{-1} (\mathbf{d} - g(\mathbf{m}))) \right\}, \quad (14)$$

360 where $N = 4$ is the number of observations, $g(\mathbf{m})$ is the vector containing the model
 361 forecasts and \mathbf{V} is the covariance matrix of data errors, which describes the statistics of
 362 both prediction errors and errors in our observational constraints. The covariance ma-
 363 trix is a square of size N^2 composed of the error covariances of each pair of observations.
 364 In our case, the observations have no covariance, so the matrix is diagonal and made up

Parameters	Minimum	Maximum	σ_{perturb}	Unit
$\log_{10} k_0$	-12	-7	0.25	$\log_{10} \text{m}^2$
$\log_{10} \eta_0$	19	22	0.13	$\log_{10} \text{Pa s}$
f_{mag}	0	1	0.03	
f_{base}	0	1	0.03	
A	250	400	6	kJ mol^{-1}
V	0	10	0.3	cm^3
ρ_{cr}	2550	3150	30	kg m^{-3}
k_{cr}	2.0	4.0	0.06	$\text{W m}^{-1} \cdot \text{K}^{-1}$
$X_{\text{H}_2\text{O}}^p$	0.0	0.05	0.005	%wt H_2O
T_m^0	1625	1750	6	K
ΔD_l^0	0.5	12	0.4	km

Table 1.

Parameters of our sampling algorithm with k_0 , the reference permeability, η_0 the reference viscosity, f_{mag} the intrusive fraction, f_{base} the fraction of basal magmatism, A the activation energy, V the activation volume, ρ_{cr} the crust density, k_{cr} the crust thermal conductivity, $X_{\text{H}_2\text{O}}$ the water concentration of the primitive mantle, T_m^0 the initial mantle temperature, ΔT_c^0 the initial overheating of the core, ΔD_l^0 the initial hemispheric perturbation in lid thickness.

365 of the error variances associated to each observation. In the case of a diagonal covari-
366 ance matrix, Equation 14 can be written as the product of four probabilities following
367 a Gaussian distribution:

$$p(\mathbf{d}|\mathbf{m}) = p(\Delta D_{\text{cr}}|\mathbf{m}) \times p(D_{\text{InS}}|\mathbf{m}) \times p(T_p|\mathbf{m}) \times p(D_L|\mathbf{m}). \quad (15)$$

368 The probability of $p(X|\mathbf{m})$ follows then a Gaussian law:

$$p(X|\mathbf{m}) = \frac{1}{\sigma_X \sqrt{2\pi}} \exp \left\{ -\frac{1}{2} \left(\frac{\bar{X} - X(\mathbf{m})}{\sigma_X} \right)^2 \right\}, \quad (16)$$

369 with σ_X the standard deviation of the data and \bar{X} the mean value of the data.

370 4.4 Observational data

371 Observations from the InSight mission have better constrained the structure of the
372 Martian crust and the present-day mantle thermal state. Here, we describe our obser-
373 vational data, their mean values and standard deviations.

374 4.4.1 Crustal thickness and dichotomy amplitude

375 The present-day average thickness of the crust and amplitude of the dichotomy are
376 two important forecasts, i.e. model outputs that can be compared to observations from
377 InSight.

378 *Data set* Crustal thickness maps can be constructed by joint analysis of the grav-
379 ity and topography (Knapmeyer-Endrun et al., 2021; Wiczorek et al., 2022). Relative
380 variations of the crustal thickness are obtained by assuming that the Bouguer anomaly
381 comes from undulations of the crust-mantle interface (Wiczorek, 2015). The crust thick-
382 ness at a given location, estimated from an independent method, then serves as an an-
383 chor point to obtain absolute crustal thickness maps. Martian crustal thickness maps

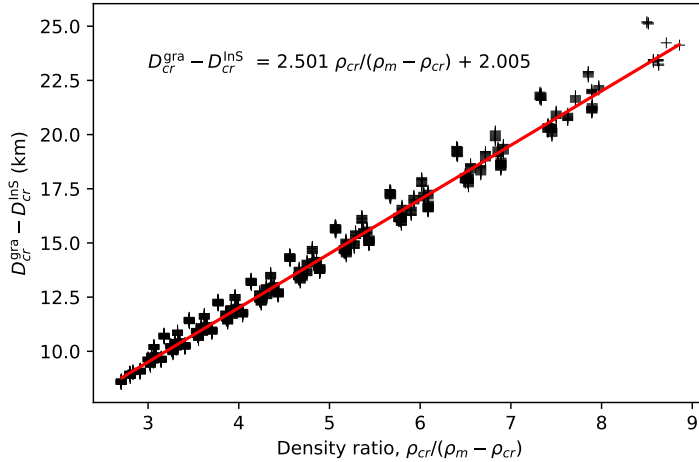


Figure 5. Difference between the global average crustal thickness calculated from Bouguer anomaly inversions and the assumed local crustal thickness at the InSight location as a function of the density ratio between the crustal density and the mantle-crust density contrast for a variety of crustal thickness maps obtained by inversion of gravity and topography data. A linear regression on all data points give the red line whose expression is shown in the graph.

384 have been anchored at the location of the InSight seismic station, where estimates of the
385 local crustal thickness has been deduced from receiver function analysis (Knapmeyer-
386 Endrun et al., 2021; Durán et al., 2022; Joshi et al., 2023). The crustal density ρ_{cr} is con-
387 sidered uniform. We use the results of 1833 crustal thickness models built from differ-
388 ent combinations of three parameters: the crustal density ρ_{cr} , varying between 2550 and
389 3150 kg m⁻³, the mantle density ρ_m , that is between 3350 and 3500 kg m⁻³ and cor-
390 responds to different types of mineralogical models detailed in Wieczorek et al. (2022)
391 and the crustal thickness below InSight, estimated between 38 and 48 km. From each
392 modelled crustal thickness map, we extract the global average thickness of the crust D_{cr}^{gra}
393 and the difference in average thickness between the Lowlands and the Highlands ΔD_{cr}^{gra} ,
394 where we use the dichotomy boundary proposed by Andrews-Hanna et al. (2008).

395 *Average crustal thickness* The average crustal thickness predicted from a crustal
396 thickness map D_{cr}^{gra} mainly depends on the values of two parameters used to construct
397 the map: the crustal thickness below InSight D_{InS}^{gra} and the ratio between the crustal den-
398 sity and the mantle-crust density contrast $\frac{\rho_{cr}}{\rho_m - \rho_{cr}}$. The difference between the average
399 crustal thickness D_{cr}^{gra} extracted from crustal thickness maps and the crustal thickness
400 below InSight D_{InS}^{gra} is linearly correlated to the ratio between the crustal density and the
401 mantle-crust density contrast (Figure 5). A linear regression on all data points gives:

$$D_{cr}^{gra} - D_{InS}^{gra} = a_{\text{thick}} \left(\frac{\rho_{cr}}{\rho_m - \rho_{cr}} \right) + b_{\text{thick}}, \quad (17)$$

402 with a slope $a_{\text{thick}} = 2.501$ km and a y-intercept $b_{\text{thick}} = 2.005$ km ; the correlation
403 coefficient (r^2), equal to 0.998, confirms the strong linear correlation (Figure 5).

404 The crustal density is a parameter of the thermal evolution model and the man-
405 tle density is an output as it increases very slightly with time (from 3493 to at most 3500
406 kg m⁻³) by mass conservation as the crust is extracted (Bonnet Gibet et al., 2022). Equa-

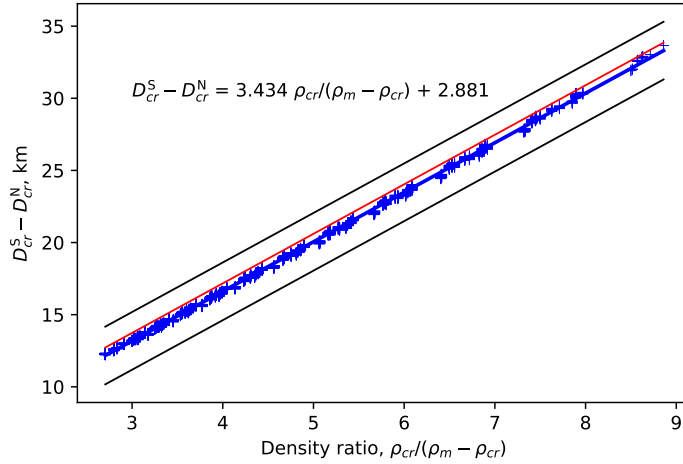


Figure 6. North-South difference in crustal thickness calculated from Bouguer anomaly inversions as a function of the ratio between the crustal density and the density contrast between mantle and crust, where we consider the North-South boundary of Andrews-Hanna et al. (2008). The blue line corresponds to a linear regression on all data points, its expression is shown on the graph. The black lines correspond to a deviation of 2 km from this linear fit. The red curve shows the difference in crustal thickness assuming Airy isostasy and a Highland topography of $h = 3.434$ km.

407 tion 17 is used to predict a theoretical thickness below InSight $D_{\text{InS}}^{\text{calc}}$ from the outputs
408 and parameters (final average crustal thickness and density ratio) of a given thermal evolu-
409 tion model, to be compared with observations from InSight:

$$D_{\text{InS}}^{\text{calc}} = D_{\text{cr}}^{\text{calc}} - a_{\text{thick}} \left(\frac{\rho_{\text{cr}}}{\rho_{\text{m}} - \rho_{\text{cr}}} \right) - b_{\text{thick}}. \quad (18)$$

410 The local crustal thickness below the InSight lander has indeed been estimated using re-
411 ceiver function analysis applied to P and S waves. The most recent works of Durán et
412 al. (2022) and Joshi et al. (2023) give the following estimate:

$$D_{\text{InS}}^{\text{SEIS}} = 43 \pm 5 \text{ km}. \quad (19)$$

413 The mantle density in our thermal evolution model is an average over the whole man-
414 tle volume, but in Bouguer anomaly inversions, it corresponds to the mantle density at
415 the crust-mantle interface. The difference between the density at the top of the man-
416 tle and the average mantle density depends on the mineralogical model and ranges be-
417 tween 50 and 200 kg m^{-3} . For simplicity, the density at the top of the mantle is con-
418 sidered to be the average mantle density minus 100 kg m^{-3} .

419 *Dichotomy amplitude* The difference in north-south crustal thickness obtained
420 from Bouguer anomaly inversions is plotted for each inversion as a function of the same
421 density ratio (Figure 6). We recall that a uniform crustal density is assumed for the crust.
422 A linear regression between the dichotomy amplitude and the density ratio shows a very
423 strong linear correlation with a correlation coefficient of $r^2 = 0.999$. We thus express the
424 expected north-south crustal thickness difference as follows:

$$\Delta D_{cr}^{\text{gra}} = D_{cr}^S - D_{cr}^N = a_{\text{dich}} \left(\frac{\rho_{cr}}{\rho_m - \rho_{cr}} \right) + b_{\text{dich}}, \quad (20)$$

425 with a slope $a_{\text{dich}} = 3.447$ km and a y-intercept $b_{\text{dich}} = 2.858$ km. The mean of the
 426 dichotomy is given by Equation 20. As for the standard deviation, we could use the stan-
 427 dard deviation calculated from the linear regression, which is ± 0.1 km. This value is very
 428 small, and leaves little margin for our thermal model. We therefore use a standard de-
 429 viation of ± 2 km, which is close to the numerical step used for the resolution of the tem-
 430 perature profile in the lid.

431 **4.4.2 Average Thermal Lithosphere thickness**

432 The total conductive layer thickness is the sum of the lid thickness D_l and the thick-
 433 ness of the thermal boundary layer at the top of the convective mantle δ_u , ($D_L^{\text{calc}} = D_l +$
 434 δ_u); we define it as the thermal lithosphere thickness. This lithosphere thickness is not
 435 a lithological boundary but a thermal boundary and is thus not easy to detect with seis-
 436 mological data. The conductive layer thickness is defined by the change in slope in the
 437 temperature profile between a conductive gradient and an isentropic gradient. On Mars,
 438 because of the low Martian gravity, the large temperature increase in the conductive litho-
 439 sphere tends to decrease seismic waves velocities and may dominate over the effect of pres-
 440 sure, in particular for S-waves, more sensitive to temperature. The base of the thermal
 441 lithosphere on Mars may thus also correspond to the base of a low-velocity zone for seis-
 442 mic waves. Arrival-time analysis of different seismic phases from a set of low-frequency
 443 marsquakes suggests a seismic velocity structure for the upper mantle that is compat-
 444 ible with the presence of a weak low-velocity zone corresponding to a thick lithosphere
 445 of 400 to 600 km (Khan et al., 2021). The more recent study of Durán et al. (2022) pro-
 446 poses a mean value of 450 km, with no associated standard deviation. We thus use a mean
 447 lithosphere thickness value of 450 km with a standard deviation of ± 100 km, as suggested
 448 by the range 400 – 600 km obtained in Khan et al. (2021):

$$D_L^{\text{avg}} = 450 \pm 100 \text{ km.} \quad (21)$$

449 In our thermal evolution model, the present-day average thickness of the lid is cal-
 450 culated from a volume-weighted average of both hemispheres.

451 **4.4.3 Present-day thermal state of the Martian mantle**

452 The mantle potential temperature is the projection to the planet’s surface of the
 453 temperature at the top of the convective mantle T_m along the isentropic temperature
 454 gradient across the conductive layer thickness :

$$T_p^{\text{calc}} = T_m - \frac{\alpha g T_m}{c_m} D_L. \quad (22)$$

455 The olivine to wadsleyite phase transition causes a seismic discontinuity associated to
 456 a travel-time triplication. Huang et al. (2022) constrained the depth of this triplication
 457 to 1006 ± 40 km in the Martian mantle. The associated mantle temperature is estimated
 458 between 1670 and 1892 K at the depth of the phase transition, accounting for uncertain-
 459 ties in the mantle composition. This temperature, projected along the isentropic gradi-
 460 ent up to the Martian surface, provides a range for the present-day mantle potential tem-
 461 perature:

$$T_p = 1605 \pm 100 \text{ K,} \quad (23)$$

462 where the standard deviation includes uncertainties in depth and mantle mineralogy. Our
 463 model forecast is calculated from Equation 22 using the average thermal lithosphere thick-
 464 ness.

465 **4.5 Monte Carlo - Markov chain (MCMC) algorithm**

466 To approximate the posterior distribution, we implement a Markov chain and a Monte
 467 Carlo sampling algorithm (Sambridge et al., 2013). This sampling method performs a
 468 random walk through the parameter space, starting with a model \mathbf{m}_1 with N_p param-
 469 eters to which we apply a small, random, perturbation to obtain a model \mathbf{m}_2 :

$$\mathbf{m}_2 = \mathbf{r}_a^{\text{gauss}}(\mathbf{m}_1, \boldsymbol{\sigma}_{\text{pertub}}), \quad (24)$$

470 where $\mathbf{r}_a^{\text{gauss}}$ is a vector of N_p random numbers following a Gaussian distribution cen-
 471 tred around the \mathbf{m}_1 -parameters with a standard deviation $\boldsymbol{\sigma}_{\text{pertub}}$, where a given value
 472 for the standard deviation is defined for each parameter of our model (Table 1). We cal-
 473 culate the prior probability $p(\mathbf{m}_2)$ following the guidelines defined in Section 4.2. We then
 474 calculate the posterior probability of our two sets of model parameters which depends
 475 on the likelihood and the prior. We accept the new model \mathbf{m}_2 in our Markov chain if the
 476 following condition is verified:

$$\frac{p(\mathbf{m}_2|\mathbf{d})}{p(\mathbf{m}_1|\mathbf{d})} > r_b \equiv \frac{p(\mathbf{d}|\mathbf{m}_2)p(\mathbf{m}_2)}{p(\mathbf{d}|\mathbf{m}_1)p(\mathbf{m}_1)} > r_b, \quad (25)$$

477 where r_b is a random number chosen uniformly between 0 and 1. If this condition is met,
 478 the model \mathbf{m}_2 is accepted, otherwise the model \mathbf{m}_1 is accepted again. The algorithm then
 479 restarts from the accepted model (\mathbf{m}_1 or \mathbf{m}_2), now called \mathbf{m}_1 to which we again apply
 480 a perturbation. This operation is repeated a sufficient number of times to sample the
 481 entire parameter space. The accepted models form a Markov chain which have the fol-
 482 lowing properties: the distribution of the sampled model in this chain is equivalent to
 483 the model posterior distribution $p(\mathbf{m}|\mathbf{d})$. We can then approximate the posterior prob-
 484 ability function of our model in the parameter space by calculating the density function
 485 of this collection of models. The acceptance rate measures the ratio of accepted over pro-
 486 posed models. This rate increases if we reduce the amplitude of the perturbations and
 487 decreases if we increase them. The optimal acceptance rate defined by statistics is around
 488 44% (G. O. Roberts & Rosenthal, 2009).

489 **4.6 Initial thermal state**

490 The temperature at the top of the convective mantle T_m^0 and the lithosphere thick-
 491 ness D_l^0 are set initially. Both are chosen such that the mantle is at the rheological tran-
 492 sition to a solid-like convection 4.5 billion years ago, which allows the extraction of buoy-
 493 ant melts to form the crust (Lejeune & Richet, 1995; Scott & Kohlstedt, 2006). We de-
 494 fine the rheological transition such that the maximum melt fraction within the mantle
 495 is equal to 0.35, which corresponds to an average melt fraction over the partially molten
 496 layer $\phi_a^{\text{N/S}}$ of ~ 0.16 . This initial condition on the melt fraction was not considered in
 497 Bonnet Gibet et al. (2022) where the initial mantle temperature and the initial viscos-
 498 ity evolved independently. For the crust, we start with an initial thickness of 4 km, for
 499 numerical reasons, and a classical crustal enrichment in heat-producing elements of 10
 500 (Thiriet et al., 2018). We impose a small initial thermal perturbation to the symmet-
 501 rical base state to trigger the instability in crustal growth ; it consists in a small north-
 502 south difference in lid thickness ΔD_l^0 (Table 1), equivalent to a small north-south dif-
 503 ference in heat flux.

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4.7 Initial Phase

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A preliminary exploration phase is necessary to the inversion. A series of inversions are first carried out with different perturbation values for each of the parameters (vector σ_{perturb} , Table 1) to find the perturbation amplitudes leading to an acceptance as close as possible to the optimal value of 44%. Once the parameters of the random walk are defined, we need to determine the necessary number of accepted models, i.e. the length of the Markov chain, to ensure a good coverage of the parameter space. One way to determine the length of the chain is to perform an inversion without constraints on the data, i.e. an inversion where the probability of the data likelihood $p(\mathbf{d}|\mathbf{m})$ is equal to 1 ; the posterior distribution should then be equal to the prior distribution. From a Markov chain with 1 million models, uniform distributions are reached, so this is the minimum number of models to gather for our inversions. The second purpose of this inversion with no observational constraints is to provide the prior distributions of the outputs of our thermal evolution model, including the forecasts. It is then possible to compare them to the posterior distributions of the outputs obtained when constraints on the data are accounted for in the inversion to evaluate whether observational data brings valuable constraints.

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5 Results of the inversion on crustal melting

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5.1 Model sets

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Following this preliminary phase, an inversion is performed based on our 4 forecasts. 960 independent Markov chains are run in parallel starting from an identical model. The first 500 models collected for each channel are not accounted for in the final distribution, a phase known as burn-in: the algorithm takes a certain number of iterations to find the high-probability parameter space it has to sample. The ensemble of models obtained from each chain are summed to obtain a final ensemble solution with a total number of $N_{\text{asym}} = 6.60 \times 10^6$ models whose acceptance rate is 42.54%, i.e. close to the optimal value of 44%. We are interested in the proportion of models that are able to sustain partial melting at the base of the crust, which corresponds to thermal evolutions where the average maximum crustal melt fraction is non-zero. The proportion of models with a non-zero maximum melt fraction in the Southern crust is 19.14% ; it is 1.20% in the Northern one. Partial melting of the Southern crust is thus significant and an order of magnitude more likely than in the North. The proportion of models with crustal melting in the South but not in the North is 17.94%, which is exactly the difference between the two previous percentages. Hence, crustal melting in the north is only possible if the southern crust partially melts as well. We define a subset of models showing sustained crustal melting in the Southern Hemisphere but not in the North, i.e. a set that is part of the initial set. This subset represents $N_{\text{MELT}} = 1.18 \times 10^6$ models, or 17.94% of the total number of models. This specific ensemble of models can be described as points in the 11-dimension parameter space (one dimension for each inverted parameter, Table 1).

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5.2 Posterior distribution of the inverted parameters

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The distribution in parameter space formed by the subset of models with a crustal melting episode only in the South (red curves, Figure 7) diverges significantly from the complete posterior distribution obtained for all models (blue histograms, Figure 7). The 2D marginal distribution for the subset with crustal melting highlight covariances between parameters which help to explain the emergence of crustal melting (coloured graphs, Figure 7).

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551

552

We obtain a Gaussian distribution for the reference viscosity with a rather low average of 2.3×10^{20} Pa s (Figure 7VII, blue and Table 2): a low viscosity is required to reach a low present-day potential temperature. The reference viscosity in the subset with

Table 2. Averages and standard deviations of inverted parameters and outputs. Related distributions are shown in Figures 7 and 8.

Set name		All inverted Models		Models with partial melting in the southern crust	
Number of models		6.60×10^6		1.18×10^6	
Acceptance		42.54%		17.94%	
Description	Parameter	Average	Standard deviation	Average	Standard deviation
Model parameters					
Reference viscosity	$\log_{10} \eta_0$	20.37	0.63	19.96	0.56
Reference permeability	$\log_{10} k_0$	-9.292	1.247	-9.016	1.144
Initial mantle temperature	T_m^0 (K)	1679	32	1680	33
Crustal density	ρ_{cr} (kg m ⁻³)	2823	156	2960	135
Crustal thermal conductivity	k_{cr} (W m ⁻¹ K ⁻¹)	3.247	0.497	3.138	0.478
Activation energy	A (kJ mol ⁻¹)	327.4	43.0	334.5	42.1
Activation volume	V (cm ³)	5.236	2.812	5.682	2.702
Magmatism fraction	f_{mag}	0.507	0.289	0.522	0.287
Basal magmatism fraction	f_{base}	0.501	0.289	0.496	0.287
Primordial mantle water content	$X_{H_2O}^p$ (%wt)	0.025	0.014	0.028	0.013
Initial perturbation	ΔD_l^0 (km)	7.106	2.885	8.048	2.727
Model outputs					
Potential temperature	T_p (K)	1635	66	1582	52
Thermal lithosphere thickness	D_L (km)	424.4	51.3	416.9	49.5
InSight crust thickness	D_{InS} (km)	43.49	4.90	45.34	4.44
Average crust thickness	D_{cr}^{avg} (km)	58.78	7.14	65.63	6.58
Dichotomy amplitude	ΔD_{cr} (km)	20.72	7.41	27.63	8.64
Internal heating in the crust	F_{HPE}^{cr} (%)	54.38	6.52	58.78	7.75
CMB temperature	T_c (K)	1874	72	1821	61
Temperature gradient at R_l	$\frac{dT}{dz} R_l$ (K km ⁻¹)	2.491	0.328	2.333	0.332
Temperature gradient at R_{cr}	$\frac{dT}{dz} R_{cr}$ (K km ⁻¹)	4.081	0.239	3.920	0.252

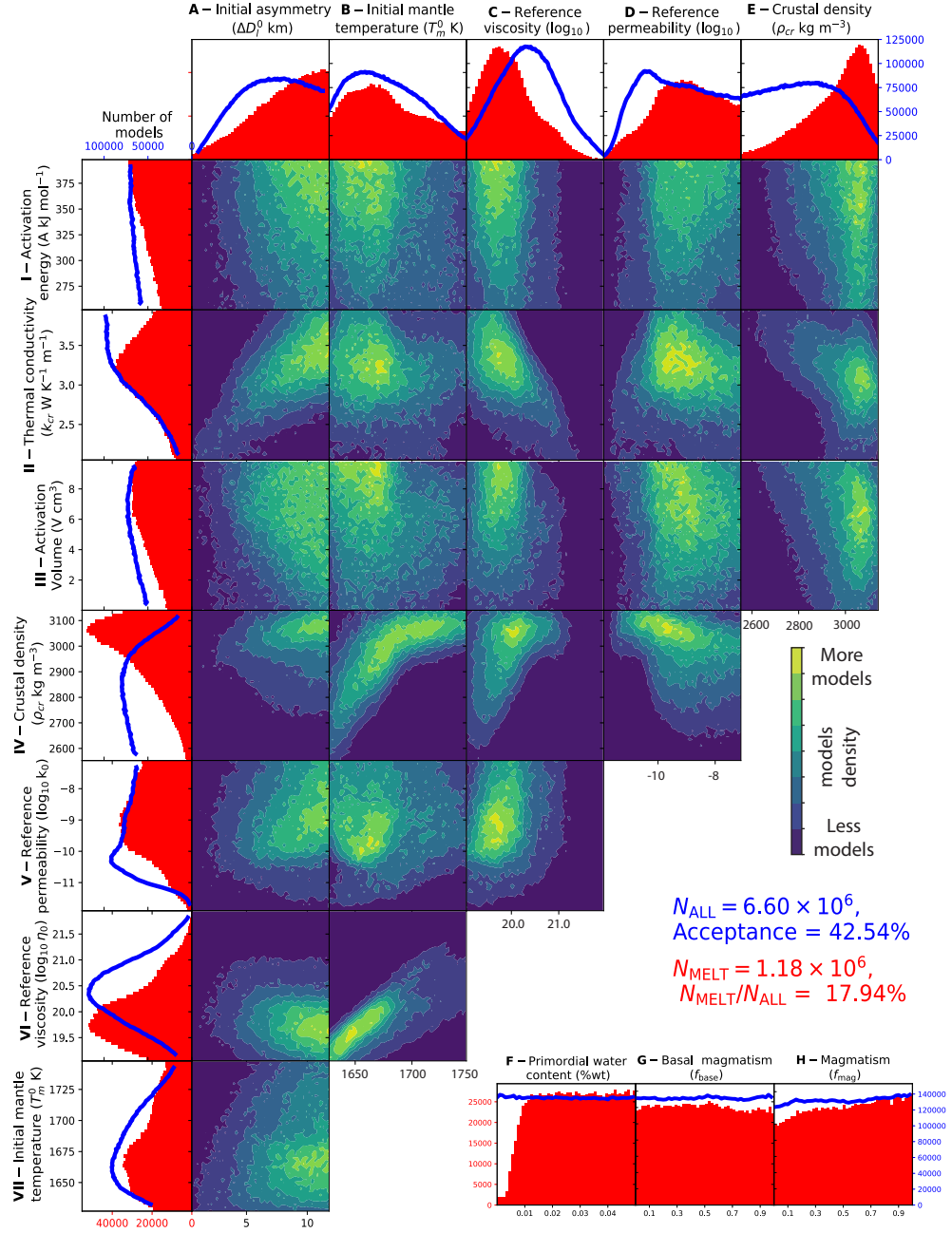


Figure 7. Projection along different inverted parameters of the probability distribution of our model, i.e. 1D and 2D marginal distributions. Red histograms and 2D marginal distribution (with dark blue to yellow coloured scale) are for the subset of N_{MELT} models with crustal melting in the south. This subset represents 17.94% of the total number of models fitting our 4 constraints, represented by the blue curve which features the histogram envelope. In the following, capital letters denote columns and roman numerals, rows. A) Initial perturbation in lid thickness (km), B/VII) initial temperature at the top of the convective mantle, C/VI) mantle reference viscosity (log scale), D/V) mantle reference permeability (log scale), E/IV) crustal density (kg m $^{-3}$), F) primitive mantle water content (wt% H $_2$ O), G) fraction of magmatism H) fraction of basal magmatism, I) activation energy, (kJ mol $^{-1}$), II) crust thermal conductivity (W m $^{-1}$ K $^{-1}$), III) activation volume (cm 3). The graphs in coloured scale represent the 2D marginal distribution between the row and column parameters for the subset of models with crustal melting in the South.

553 crustal melting (Figure 7C & VI, red and Table 2) is shifted towards even smaller val-
 554 ues with an average of 9.12×10^{19} Pa s. Lower viscosity leads to thinner lids and thicker
 555 crusts, hence to stronger temperature gradients and hotter temperatures at the base of
 556 the crust, favouring crustal melting. The inversion points to rather cold initial mantle
 557 temperatures (~ 1680 K) in both sets (Figure 7 B & VII, Table 2). The strong positive
 558 correlation between the initial mantle temperature and the reference viscosity (Figure 7B-
 559 VI) is induced by the choice of our initial state: the reference viscosity increases with
 560 the initial temperature to maintain a sufficiently thin initial lid thickness to result in an
 561 initial mantle fraction characteristic of the rheological transition.

562 The distribution of the amplitude of the initial thermal perturbation in the global
 563 set (Figure 7A, blue and Table 2) shows that there exists an optimal perturbation around
 564 8 km for this parameter. Stronger initial perturbations produce dichotomies of larger am-
 565 plitudes, which do not match with observations. Below 8 km, it is more difficult for the
 566 dichotomy to grow to expected amplitude. The subset of models with crustal melting
 567 in the South covers the upper range of initial perturbations because large initial pertur-
 568 bations trigger rapid formation of large dichotomies, more favourable to crustal melt-
 569 ing. (Figure 7A, red and Table 2). If a parameter value is tuned such that it favours di-
 570 chotomy growth (such as a large initial thermal perturbation), the values of the other
 571 parameters also influencing on its growth, such as the crust thermal conductivity, must
 572 be adjusted to limit it such that it fits observational data.

573 For the global set, large crustal thermal conductivities are favoured, though solu-
 574 tions are found for all values. The distribution in the subset with crustal melting is Gaussian-
 575 like with a maximum at ~ 3.2 W m $^{-1}$ K $^{-1}$ (Figure 7II). It is shifted towards lower val-
 576 ues compared to the global set because the lower the thermal conductivity, the larger
 577 the growth of the dichotomy and the warmer the temperature at the base of the crust
 578 is. The combination of these two effects strongly favours melting at the base of the south-
 579 ern crust. Dichotomy growth is favoured by smaller crustal conductivities, as a higher
 580 thermal conductivity favours heat diffusion which dampens the positive feedback mech-
 581 anism leading to dichotomy growth (Bonnet Gibet et al., 2022). Higher crustal thermal
 582 conductivities thus correlate with larger initial perturbations (Figure 7A-II).

583 Similarly, in the subset with crustal melting, the activation volume decreases as the
 584 initial perturbation increases (Figure 7A-III). The pressure-dependence of the viscosity
 585 leads indeed to another positive feedback between lid thickness and lid thickening (Watson
 586 et al., 2022), which tends to amplify the feedback between crust thickness and crust ex-
 587 traction and the growth of the dichotomy (Bonnet Gibet et al., 2022). The activation
 588 volume is on average higher in the subset with crustal melting than in the global case
 589 (Figure 7III) because larger activation volumes result in lower viscosities at low pressure
 590 (Bonnet Gibet et al., 2022). The lid then initially thickens less rapidly, promoting crust
 591 melting. However, as viscosity increases more with pressure, the lid growth rate increases
 592 then sharply during cooling.

593 The average value of the reference permeability (Figure 7D & V, blue line) is 10^{-9}
 594 m 2 in the global set, which shows a distribution skewed towards low values. The distri-
 595 bution shows a maximum for reference permeability values between $\simeq 10^{-10}$ and $\simeq 10^{-9}$
 596 m 2 . Low reference permeabilities, lower than 10^{-9} m 2 , are less frequent in the subset
 597 with crustal melting than for all models (Figure 7D & V, red histogram) because they
 598 imply a prolonged and delayed crustal extraction occurring on thicker, colder lids, less
 599 favourable to crustal melting. These low reference permeabilities induce long extraction
 600 times which are more favourable to dichotomy growth (Bonnet Gibet et al., 2022) and
 601 hence favour low initial perturbations (Figure 7A-V). High permeabilities ($> 10^{-9}$ m 2)
 602 result in large crustal extraction rates and rapid crust growth on a thin lithosphere, more
 603 favourable to crustal melting.

604 Larger viscosities and warmer initial mantle temperatures tend to generate thicker
 605 crusts and larger dichotomy amplitudes, as they lead to slower cooling and prolonged
 606 crustal extraction timescales. Stronger initial asymmetries ΔD_l^0 thus tend to be com-
 607 pensated by lower initial mantle temperatures and reference viscosities (Figure 7A-VI/VII).
 608 For the same reasons, the reference viscosity correlates negatively with the crust ther-
 609 mal conductivity and positively with the reference permeability (Figure 7C-II/IV) while
 610 the reference permeability correlates negatively with the crust thermal conductivity (Fig-
 611 ure 7D-II).

612 The crustal density is a proxy for the average crustal thickness and dichotomy ampli-
 613 tude (Section 4.4, Figures 5 & 6); it is relatively well constrained by the inversion (Fig-
 614 ure 7E & IV). The global set of accepted models shows a Gaussian distribution centred
 615 around $\simeq 2820 \text{ kg m}^{-3}$ (Table 2). The average crustal density is larger in the subset with
 616 crustal melting (Figure 7E & IV, red and Table 2). Larger crustal density values lead
 617 to thicker crusts and larger north-south differences in crustal thickness, which maximise
 618 the southern crustal thickness and favour melting at the base of the crust. Interestingly,
 619 the 2D marginal distribution for crustal density and other parameters influencing dichotomy
 620 growth tend to be bimodal. Parameter values impeding dichotomy growth (lower ini-
 621 tial temperatures and reference viscosities, higher crust thermal conductivities and smaller
 622 reference permeabilities) are associated to a distribution in crustal density that is simi-
 623 lar to the global set of models, with a peak density around 2900 kg m^{-3} (Figure 7IV).
 624 On the contrary, parameter values favouring a prolonged and larger growth of the di-
 625 chotomy are associated with large crustal densities of 3000 to 3100 kg m^{-3} (Figure 7IV).
 626 Larger dichotomies are also favoured by larger initial asymmetries ; and, as expected,
 627 the crustal density tends to correlate positively with the initial perturbation (Figure 7A-
 628 IV).

629 The activation energy is not well constrained by the inversion in the global set (Fig-
 630 ure 7I). The subset of models with crustal melting tends to slightly favours larger ac-
 631 tivation energy values (Figure 7I, red) because they result in hotter temperatures at the
 632 base of the lid (Davaille & Jaupart, 1993; Thiriet et al., 2019). The water content of the
 633 primordial mantle only affects the crustal solidus temperature, its distribution is thus
 634 constant for the global set of models and does not differ from the prior (Figure 7F, blue).
 635 The posterior water content distribution is constant above 100 ppm in the subset with
 636 crustal melting, but drops sharply below this value (Figure 7F, red). The larger the wa-
 637 ter content in the primordial reservoir, the more water can be stored in the crust and
 638 the easier it is to reach the saturated solidus at depth in the crust.

639 In both sets, the distribution of the fraction of basal magmatism does not differ
 640 significantly from the prior uniform distribution (Figure 7G). The distribution of the frac-
 641 tion of magmatism f_{mag} (Figure 7H, blue) increases very slightly from 0 to 1 in the global
 642 subset. In the subset with crustal melting, larger fractions of magmatism are slightly favoured
 643 as they result in larger crustal temperature gradients (Figure 7H, red).

644 5.3 Posterior distribution of the present-day thermal state

645 The posterior distribution of the current structure of Mars provides information
 646 on how the inversion has enabled to recover our constraints. Comparing the distribu-
 647 tions obtained after inversion for the forecasts (blue curves and red histograms on Fig-
 648 ure 8a-b-c) with the expected distribution from the observations ("likelihood", grey curves)
 649 as well as with the prior distributions, that are obtained without accounting for obser-
 650 vations (black curves), demonstrates that, among our four observational data, crustal
 651 thickness data are clearly the most constraining data of our inversion.

652 The prior distribution projected in terms of predicted mantle potential tempera-
 653 ture covers a broad range of temperatures (Figure 8a black curve). Although in the ex-
 654 pected range, both outcomes diverge from the distribution that we were aiming for (grey

line, Equation 23), demonstrating that our inversion has better constrained the value of the mantle potential temperature than its expected range thanks to other observational data.

The likelihood for the thermal lithosphere thickness is more spread-out than our prior distribution (compare grey and black lines on Figure 8b). This means that our considerations on the lithosphere thickness (Equation A5) does not constrain our thermal evolution scenarios. Such values for the lithosphere thickness are in fact expected, and similar distributions between the global set and the subset with crustal melting are then obtained (Figure 8b and Table 2).

Our inversion corresponds very well to the expected crustal thickness below InSight (i.e. to the likelihood), both for the global set of models and the subset showing crustal melting (Figure 8c and Table 2). The gain in information thanks to our inversion compared to the prior is evident: the prior distribution spreads over a wide range of values from -15 km to +161 km, negative thicknesses below InSight being theoretically possible from Equation 18, for thin crusts and large crustal densities. Crustal melting is favoured by larger crustal thicknesses, in the South in particular ; the average thickness of the distribution is thus slightly higher in the subset of models with crustal melting (65.63 ± 6.58 km) than for the global set (58.78 ± 7.14 km), see Table 2. Similarly, the amplitude of the crustal dichotomy tends to be larger in the subset showing crustal melting than in the global set (Figure 8d).

Crustal melting is also favoured by lower reference viscosities (Figure 7), which induces thinner top thermal boundary layers early in the planet evolution, and hence larger temperature gradients more favourable to crustal melting. Lower reference viscosities tend to induce a colder present-day thermal state for Mars: the mantle potential temperature and the CMB temperature both peak towards colder values for the subset of models with crustal melting than for the global case (Figure 8a, red histogram and Table 2). Present-day temperature gradients at the base of the lid and crust are also shifted to lower values for the subset of models with crustal melting compared to the global set because of the colder present-day thermal states induced by the lower viscosity values (Figure 8h and Table 2). Note that at the present-day, temperature gradients tend to be larger at the lid base than at the crust base indicating a significant change in temperature gradient within the lithospheric mantle (Figure 8g-h, blue curves).

The subset of models with crust melting tend to be associated to bimodal distributions for both the model parameters and the model outputs. This is most visible in the distribution of the percentage of internal heating in the crust : the first peak is similar to the global set, $\sim 54\%$, while the second peaks at higher values, $\sim 67\%$ (Figure 8e). This is also visible, although less clearly, in the dichotomy amplitude and the temperature gradient at the crust base (Figure 8d-h). These two modes correspond to crustal melting occurring either in relatively thin crusts, with low dichotomy amplitudes, or in very thick crusts with large dichotomy amplitudes, as has been described in previous Section 5.2 for the 2D marginal distribution of the crustal density and other model parameters.

5.4 Crustal melting output

Model outputs concerning the characteristics of crustal melting clearly show that the bimodal distributions of the different model parameters and outputs are linked to the two possible phases of crustal melting described in Section 5.2 and Figure 7.

Crustal melting is obtained for average crustal thicknesses that are generally thicker than in the global set of models. This average thickness is 65 km, against 58 km for the global set, (Figure 9I and Table 2), but this single value conceals again a bimodal distribution, with a first peak at ~ 62 km, closer to the average of the global set, and a sec-

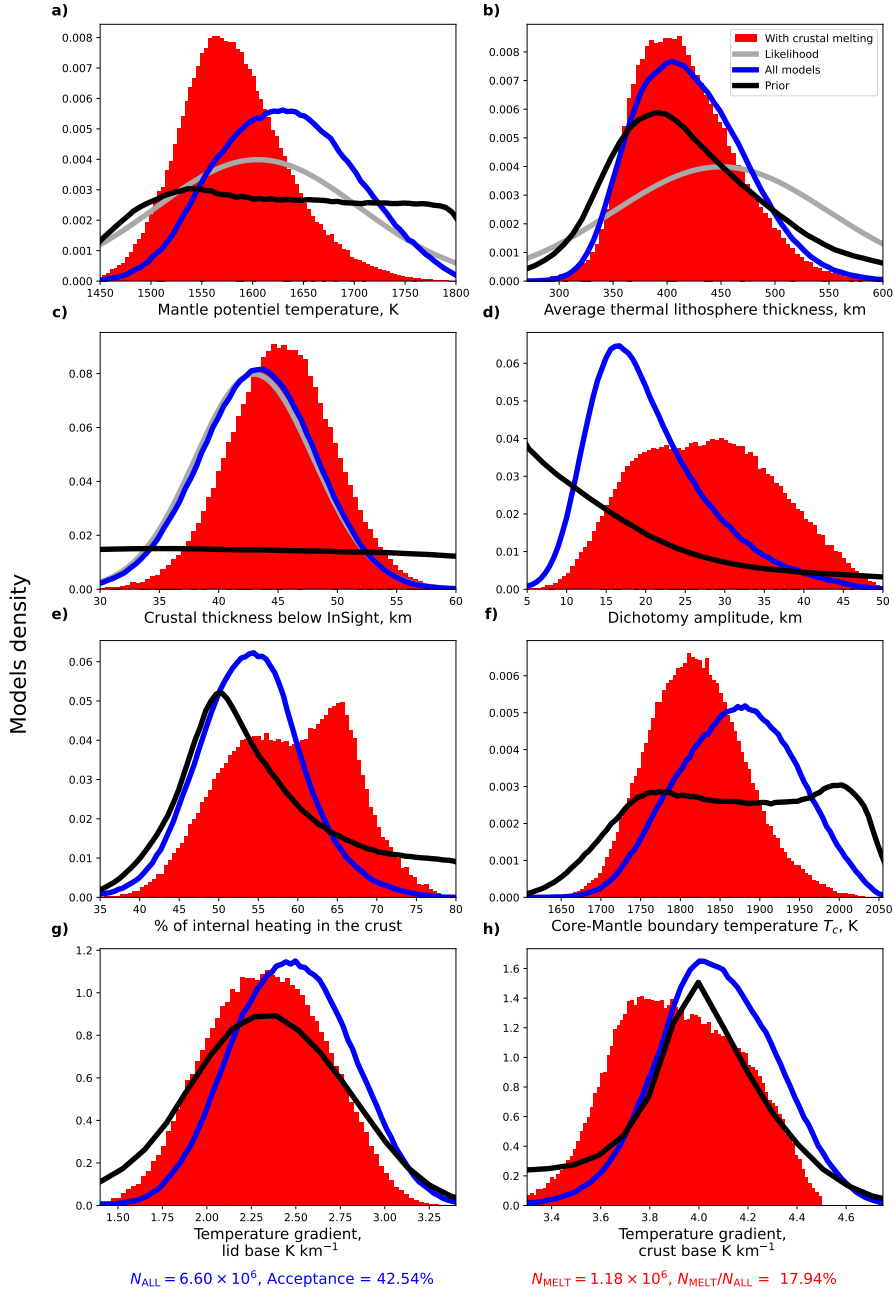


Figure 8. Posterior marginal distribution for the forecasts and various other outputs (red histograms and blue curves) compared to their prior distributions (black curves) and the likelihood for observational data (grey curves, as defined in Section 4.3). The red histograms represent the distribution for the subset of N_{MELT} models showing crustal melting in the South which represent 17.94% of the total inverted models. Blue curves represent histogram envelopes for all the N_{ALL} inverted models, i.e. in the global case. a) Present day mantle potential temperature (K), b) present-day average lid thickness (km), c) present-day crustal thickness below InSight, Equation 18 (km), d) present-day dichotomy in crustal thickness (km), e) percentage of the bulk radioactive heating present in the crust (% of total), f) present-day temperature at the core-mantle boundary (K), g) present-day average temperature gradient at the base of the lid (K km^{-1}), h) present-day average temperature gradient at the base of the crust (K km^{-1}).

705 ond, more significant, peak at ~ 67 km. A bimodal distribution is particularly evident
 706 in the ages associated to crustal melting (start and end age of melting): a very early peak
 707 is observed for both these ages (< 300 Myr, Figure 9A & B). This represents a short and
 708 early melting episode that corresponds to the first phase of crustal melting presented in
 709 the thermal evolution example (Figure 4). These cases correlate with crustal thicknesses
 710 between 50 and 70 km (Figure 4). The second peak ($\simeq 1$ Gyr, Figure 9A & B) repre-
 711 sents a late and longer crustal melting episode that corresponds to the second phase of
 712 crustal melting in the example of Figure 4. Models with a late and prolonged melting
 713 correlate with thicker crustal thicknesses of 60 to 80 km.

714 Models with crustal melting may show either only one or both of these melting episodes.
 715 Typically, for crustal thicknesses between 60 and 70 km, both crustal melting episodes
 716 coexist. For average crustal thicknesses less than 50 km, no partial melting occurs in the
 717 crust.

718 Models characterised by an early and brief episode of crustal melting are associ-
 719 ated to particularly low viscosities ($\lesssim 10^{20}$ Pa s, Figure 9A/B-II) and relatively large
 720 reference permeability values $\gtrsim 10^{-10}$ m² (Figure 9A/B-III). In this case, crustal ex-
 721 traction is rapid, but the lid grows slowly, resulting in very hot temperatures at the base
 722 of the crust. These temperatures exceed the solidus even in the anhydrous case, which
 723 explains the lack of dependence on the bulk water content (Figure 9A/B-IV). These mod-
 724 els are also characterised by high values of the activation energy inducing higher tem-
 725 peratures at the lid base.

726 For models with a late episode of crustal melting, the crust mostly forms later, when
 727 the lid is colder. In this case, the temperature at the crust base does not reach the solidus
 728 if the crust is dry and the bulk water content must be larger than 100 ppm for partial
 729 melting to occur in the crust (Figure 9A/B-IV). These late melting models cover a wider
 730 range of values for the reference viscosity, reference permeability, activation energy and
 731 crust thermal conductivity and therefore different thermal evolution scenarios (Figure 9A/B-
 732 II, A/B-III, A/B-V & A/B-VI). Lower reference permeability, higher viscosity and lower
 733 crust thermal conductivity values tend to prolong crustal melting (Figure 9A/B-II, A/B-
 734 III & A/B-VI).

735 The melt fraction averaged over the partially molten layer in the southern crust
 736 range from 0% to $\simeq 30\%$ at the peak of the melting episode, with an average of 9.3%
 737 and a maximum probability at $\simeq 5 - 6\%$ (Figure 9C). The thickness of the partially
 738 molten layer in the crust range from 0 to a few tens of kilometres with an average of 15
 739 km (Figure 9D) ; with thinner partially molten layers more likely than thicker ones. Cases
 740 with a molten thickness of ~ 10 kilometres and a melt fraction of 5% on average are the
 741 most common.

742 The melt fraction and thickness of the partially molten layer tend to increase with
 743 the crustal thickness (Figure 9C-I & D-I). The molten layer thickness is $\approx 5 - 10$ km
 744 for crustal thicknesses up to 70 km. Above this value, the molten layer thickness and melt
 745 fraction can increase significantly. For some models, more than a third of the crustal thick-
 746 ness can be partially molten.

747 To summarise, cases showing crustal melting in the south are characterised by thick
 748 crusts, particularly in the South, and by a cold present-day initial state caused by a low
 749 reference viscosity (that favours early thin lithospheres and large temperature gradients
 750 in the lid and crust) and by a significant extraction of heat-producing elements from the
 751 mantle. The crust in the South can be partially molten over a thickness of a few to
 752 a few tens of kilometres. The melt fraction can also be significant (more than 10% Fig-
 753 ure 8) and could produce rather large volumes of magma. Crustal melting can either start
 754 very early in the thermal history of Mars (-4.5 Gyr ago) or much later (-3.8 Gyr ago)
 755 and over a variable duration (from ~ 10 s Myr to > 1 Gyr). However, these values could

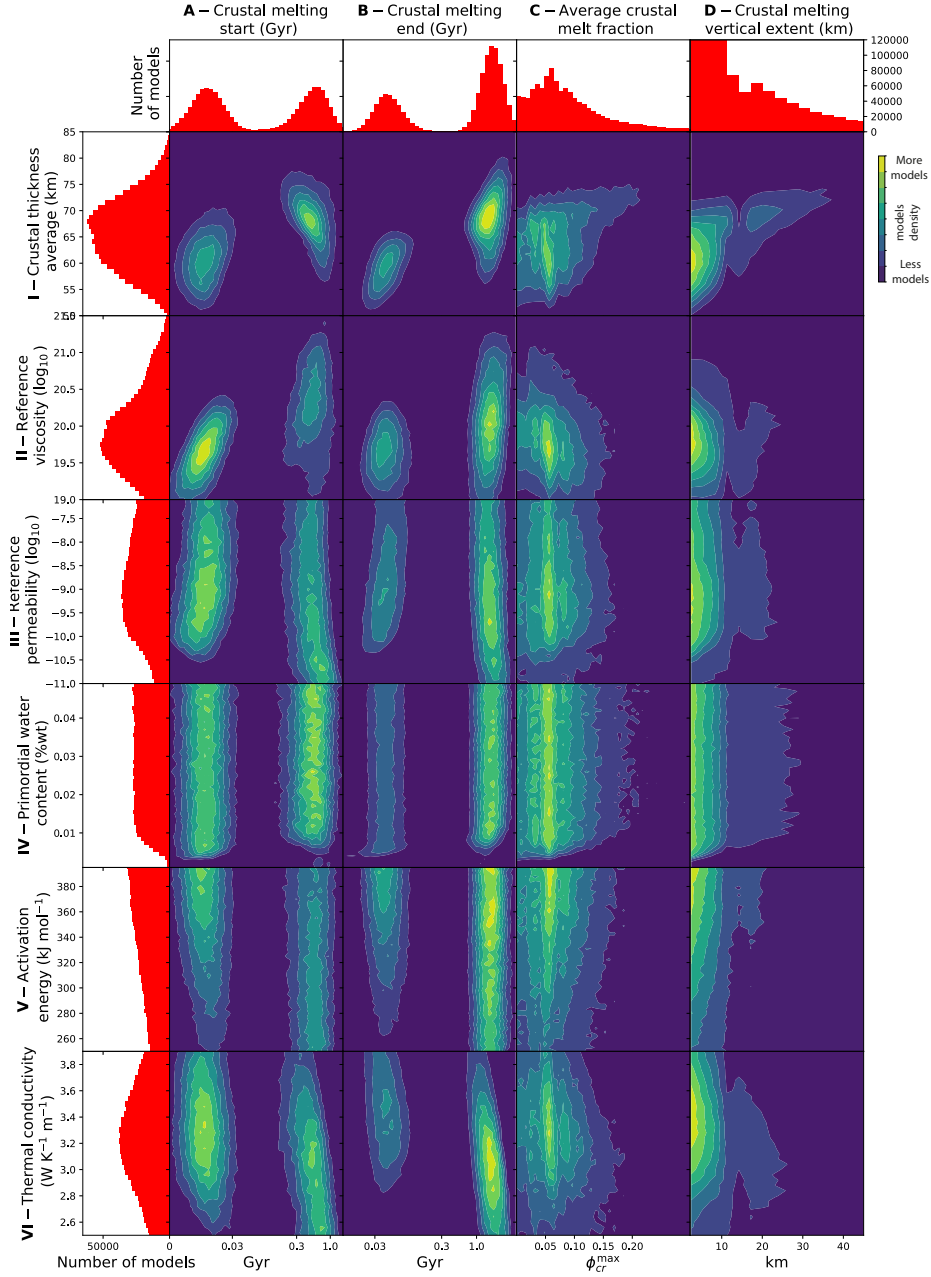


Figure 9. Posterior marginal distribution of different model outputs. The red histograms represent the distribution of the subset of N_{MELT} models with crustal melting which represent 17.94% of the total of inverted models. A) Age of the onset of crustal melting in the Southern Hemisphere (Gyr represented on log scale to highlight the bimodal distribution), B) age of the end of crustal melting in the Southern Hemisphere (Gyr, log scale), C) maximum average melt fraction in the southern crust, D) maximum thickness of the molten layer in the Southern Hemisphere (km), I) average crustal thickness, II) reference viscosity of the mantle (log scale), III) reference permeability of the mantle (log scale), IV) primitive mantle water content (*wt%* H_2O), V) activation energy, (kJ mol^{-1}), VI) thermal conductivity of the crust ($\text{W m}^{-1} \text{K}^{-1}$). The graphs in coloured scale represent the joint inversions between the two parameters corresponding to the row and column. The colour scale ranges from maximum density in yellow to minimum density in purple.

756 be modified if we were accounting for the extraction of differentiated melts that would
 757 cause cooling at depth.

758 **6 Discussion**

759 **6.1 Insights from our Bayesian inversion**

760 **6.1.1 A present-day cold Martian mantle**

761 Our inversion point to a cold present-day thermal state for Mars, which is not sur-
 762 prising as we use constraints from seismology suggesting a cold Martian mantle (Huang
 763 et al., 2022) with a thick lid (Durán et al., 2022; Khan et al., 2021; Drilleau et al., 2022).
 764 However, the most constraining observations on the present-day thermal state of Mars
 765 consist in the crustal thickness data. The potential temperature of the mantle and lid
 766 thickness are both estimated with a significantly smaller dispersion after our inversion
 767 than the initial observation (Table 2). This cold thermal state implies a low reference
 768 viscosity and a large mantle depletion in heat-producing elements (Table 2). If we con-
 769 sider only models with crustal melting in the South, the resulting thermal state is even
 770 colder as even lower viscosity values are preferred.

771 The temperature gradient at the base of the lid is estimated to between 1.5 and
 772 3.25 K/km, in agreement with the geophysical inversions of Khan et al. (2021), (Drilleau
 773 et al., 2022) and Durán et al. (2022). However, the gradient increases from the base of
 774 the lithosphere to the base of the crust, where it is between 3.4 and 4.5 K km⁻¹. Since
 775 the temperature gradient in the lid has a significant influence on the ray path and wave
 776 travel time, it seems important to account for the temperature gradient variation in the
 777 lid thickness in travel-time inversions as in Drilleau et al. (2021, 2022, 2024).

778 **6.1.2 Crustal thickness constraints on Mars' thermal evolution**

779 Constraints on crustal thickness are more restrictive for the inversion than constraints
 780 on the mantle thermal state. The thermal evolution of Mars is indeed very dependent
 781 on the amount of crust and heat producing elements extracted from the mantle. Improv-
 782 ing constraints on the thickness and density of the Martian crust could thus further im-
 783 prove our knowledge on the thermal evolution of Mars. Recent examples include con-
 784 straints brought by the detection of Rayleigh waves for Marsquake S1222a. From the great
 785 circle path of these waves and crustal thickness maps, Kim et al. (2023) deduced a range
 786 of values for the average crustal thickness between 42 and 56 km. Such values, on the
 787 lower range of the one proposed initially by Knapmeyer-Endrun et al. (2021) would not
 788 favour crustal melting in the South. However, more recently, Drilleau et al. (2024) con-
 789 strained lateral variations in crustal thickness using body wave arrival times combined
 790 with topography and gravity field modelling. Their results point to a crustal thickness
 791 below InSight of ~45 km and to an average thickness of ~66 km, that is, in that case,
 792 on the upper end of previous estimates. Such values would, inversely, favour the emer-
 793 gence of crustal melting during crust construction.

794 **6.1.3 A water-rich primitive mantle ?**

795 Our inversion shows that a minimum of ~100 ppm of water in the bulk silicate
 796 is required to induce crustal melting in the South (Figure 7F). In our thermal evolution
 797 model, water only plays on the crustal solidus; its effect on mantle rheology and dynam-
 798 ics is not accounted for. In the literature, estimates of the bulk silicate water content span
 799 several orders of magnitude, from 1 ppm (Mysen et al., 1998) to 1000 ppm (Johnson et
 800 al., 1991). Estimates come from the study of SNC meteorites and are based on geochem-
 801 ical models. Geodynamical estimates rely on the effect of water on mantle rheology, search-
 802 ing for the rheology, among dry or wet olivine, that best explains the planet dynamics.

803 For early Mars, a wet rheology has been proposed to explain the thermal evolution (Hauck
 804 & Phillips, 2002), elastic thickness estimates (Thiriet et al., 2018) and relaxation of the
 805 dichotomy (Guest & Smrekar, 2005), which, according to G. J. Taylor (2013), would cor-
 806 respond to a water content of 600 ppm. Our inversion results converge toward a low refer-
 807 ence viscosity ($\simeq 10^{20}$ Pa s, Figure 8C) which could correspond to an intermediate
 808 rheology, between wet and dry olivine (Karato & Wu, 1993). But the presence of wa-
 809 ter is not the only factor that could induce a more ductile rheology in the past: the pres-
 810 ence of melt also causes a reduction in the bulk viscosity (Breuer & Spohn, 2006). Mei
 811 et al. (2002) proposes an exponential reduction in viscosity as a function of the melt frac-
 812 tion. However, this reduction only affects the partially molten layer at the top of man-
 813 tle that makes a small fraction of the total mantle volume. It is thus not entirely clear
 814 how the reduction in viscosity caused by the presence of melt affect the dynamics of the
 815 whole mantle. Samuel et al. (2019) use for instance a viscosity depending on the melt
 816 rheology, which increases the convective heat flux. Not surprisingly, their results point
 817 to a much higher reference viscosity, as it is then reduced by the presence of melt. Thus
 818 it is not clear whether this low viscosity points to an early water-rich or partially molten
 819 mantle (or both).

820 **6.1.4 Origin of the dichotomy**

821 Our inversion demonstrates that the positive feedback mechanism we identified in
 822 Bonnet Gibet et al. (2022) is able to generate the observed dichotomy from an initially
 823 low perturbation in lid thickness (0.5 to 12 km, Figure 7A) over a very wide range of pa-
 824 rameters (Figure 8d) and this, in the space of parameters required to explain the struc-
 825 ture revealed by InSight. The average initial perturbation in lid thickness from the in-
 826 version is ~ 7 km for the global set (Figure 7A). But solutions exist over the full range
 827 by either amplifying or dampening the perturbation through the effects of other model
 828 parameters influencing the positive feedback. Considering an initial lid thickness of 50
 829 km and a temperature jump of 1300 K in the lid, a hemispheric difference in lid thick-
 830 ness of 7 km corresponds to a difference in heat flux of ~ 15 mW m $^{-2}$ which represents
 831 14.5% of the initial heat flux (that is 104 mW m $^{-2}$). In terms of temperature, a differ-
 832 ence in lid thickness of 7 km between the two hemispheres would represent a temper-
 833 ature difference of 91 K at the average depth of the lid base. Whether a finite hemispher-
 834 ical perturbation is first required, or not, to trigger the growth of our mechanism can
 835 thus be debated. But this inversion, which tests the sensitivity of our thermal evolution
 836 model to the initial perturbation, shows that, after reaching a peak at ~ 8 km, the prob-
 837 ability decreases. We therefore expect that strong initial hemispherical perturbations are
 838 less likely to generate the expected dichotomy, all the more if we consider a perturba-
 839 tion in crustal thickness, the effect of which is considerably larger than that of a differ-
 840 ence in lid thickness (Bonnet Gibet et al., 2022). The small amplitude of the initial per-
 841 turbation required to fit InSight observations seems thus irreconcilable with the hypoth-
 842 esis of a giant impact. Recently, Ballantyne et al. (2023) show that a giant impact that
 843 would affect a whole hemisphere inevitably leads to the formation of a local magma ocean
 844 producing a large quantity of crust. If such an impact occurred on Mars, the resulting
 845 dichotomy would certainly be much larger than observed. This is indeed what is shown
 846 by studies pointing to an impact in the Southern Hemisphere: the obtained hemispher-
 847 ical difference in crustal thickness are about a hundred kilometres larger than expected
 848 (Golabek et al., 2011; Leone et al., 2014; Cheng et al., 2024). In contrast, an initial tem-
 849 perature or heat flux anomaly caused by a degree-1 convection (J. H. Roberts & Zhong,
 850 2006; Šrámek & Zhong, 2012) resulting from a rheologically layered mantle or inherited
 851 from the magma ocean (Morison et al., 2019; Watson et al., 2022) is more consistent with
 852 our results. Finally, the full range of initial perturbations can lead to crustal melting in
 853 the Southern Hemisphere. But crustal melting would be more likely if the initial per-
 854 turbation is not infinitesimal and if our feedback mechanism was triggered by an endo-
 855 genic degree-one mechanism.

856 **6.2 Partial melting of the crust and differentiation of the Southern High-** 857 **lands**

858 **6.2.1 Hemispheric scale**

859 Partial melting of the crust at the scale of the Southern Hemisphere is a likely event
860 during Mars' thermal evolution: crustal melting occurs in the Southern Hemisphere in
861 a substantial part (17.94%) of the models fitting InSight constraints that emerge from
862 our inversion. The growth of a strong hemispheric dichotomy, caused by the positive feed-
863 back mechanism we identify, provides the conditions for melting in the South where the
864 crust is thicker. A thick crust allows not only for higher temperatures but also for lower
865 melting temperatures, as more water can dissolve into the melt at higher pressure, low-
866 ering the solidus. Lower thermal conductivities in the crust also cause larger tempera-
867 ture gradients, favouring crust melting. Similarly, lower reference viscosity values for the
868 mantle also favour crustal melting because (1) it forms thinner lids, larger melt fractions
869 and larger crusts, and (2) the lid is thinner, and its temperature gradient is larger when
870 the crust forms. A water content of 100 ppm in the primordial mantle is sufficient to achieve
871 crustal melting in all cases. On the other hand, heating by magmatism does not seem
872 to significantly modify the temperature gradient in the crust, as the heat deposited com-
873 pensates for the cooling caused by the downward advection of material underneath. Thus,
874 contrary to what we might have expected, magmatic heating does not significantly plays
875 on crustal melting at the hemispherical scale.

876 However, although crustal melting at the scale of the Southern Hemisphere is pos-
877 sible, it appears limited and can not affect more than a third of the crust thickness. Par-
878 tial melting of the crust on a hemispherical scale, with a maximum vertical extent of thirty
879 kilometres and melt fraction 10%, would produce a felsic layer of 3 km at most. These
880 buoyant melts would rise to shallower depths. Given the important thickness of the crust
881 in the South, these small amounts of melts likely crystallised at depth before reaching
882 the surface, potentially forming an intermediate layer of undifferentiated basalt mixed
883 with some felsic rocks. It does thus not appear possible to generate a layered crust with
884 an upper felsic layer overlying an intermediate basaltic layer and a deep layer formed by
885 mafic residues (McCubbin et al., 2008) on a hemispheric scale through this mechanism.
886 This is consistent with the globally basaltic surface composition of the Highlands.

887 **6.2.2 Timing for crustal melting**

888 Episodes of sustained partial melting in the crust can take place at two specific pe-
889 riods. The first period occurs very early, between 4.5 and 4.3 billion years ago. This age
890 corresponds to that of zircons found in NWA 7034 meteorite (Cassata et al., 2018) and
891 to age estimates proposed for the province Terra Cimmeria/Sirenum (Bouley et al., 2020).
892 During this early and short crustal melting episode, less than ~ 10 km of crust can par-
893 tially melt (Figure 8). A second episode of crustal melting can occur towards the end
894 of crustal formation, between 4 and 3 billion years ago and for ~ 1 Gyr. The maximum
895 amplitude of melting is reached when the crust completes its formation at ~ 3.5 Gyr, i.e.
896 during the Hesperian. This period would thus be suitable for the production of magma
897 over a prolonged duration. There is evidence of significant explosive volcanism in the High-
898 lands at that time (Brož et al., 2021). Explosive volcanism is characteristic of magma
899 enriched in volatiles, particularly water. On Mars, explosive volcanoes can be fed by basaltic
900 magmas enriched in volatiles through their interaction with underground water (Carr,
901 1979); they could also come from crustal differentiation, in the presence of water.

902 **6.2.3 Terra Cimmeria-Sirenum: A continental crust under formation?**

903 The thickness of the crust is not uniform in the Highlands, and there are strong
904 variations in between provinces. A small increase in crustal thickness, over a sufficiently

905 large province, can lead to a significant increase in the crustal melt fraction and the thick-
 906 ness of the partially molten layer through the increase in the basal temperature and the
 907 decrease in melting temperature (Section 2.3, Figure 3). Models where melting on a hemi-
 908 spheric scale is limited could locally lead to larger volumes of differentiated magma. Ther-
 909 mal evolutions where melting is not reached on a hemispheric scale could also sustain
 910 limited crustal melting in thick crustal provinces. As a significant proportion of these
 911 differentiated melts may crystallise at depths ; they could constitute a barrier to the as-
 912 cent of denser melts and prevent the resurfacing of the province. Terra Sirenum/Cimmeria
 913 is a good candidate for this scenario: it is a geological province characterised by a very
 914 thick crust (Figure 1 & Bouley et al. (2020)) and feldspar-rich outcrops (Payré et al.,
 915 2022). It may be the region of origin of NWA 7034, and it is bounded by the Gusev and
 916 Gale craters, where differentiated rocks have been observed. Zircon ages in the NWA 7034
 917 breccia are between 4.42 and 4.47 Gyr (Cassata et al., 2018) and are compatible with
 918 an early and rapid melting of the crust. In addition, the compositions of the rocks present
 919 in Gale crater seems to be consistent with the mechanism we propose (Udry et al., 2018).

920 Sautter et al. (2015) suggested that the presence and composition of the differen-
 921 tiated rocks found in Gale crater could indicate the presence of a continental crust on
 922 Mars. This raises the question of the extent to which the Terra Cimmeria/Sirenum province
 923 fits this description. The Earth’s continental crust is characterised by rocks richer in sil-
 924 ica than the basaltic oceanic crust. The majority ($\sim 60\%$) of the rocks making up the
 925 continental crust belong to the TTG series (Tonalite-Trondhjemite-Granodiorite, Rud-
 926 nick & Holland, 2005). The felsic samples described by Sautter et al. (2015) are petro-
 927 logically quite similar to these TTGs. However, Udry et al. (2018) argue that their chem-
 928 istry better corresponds to Icelandic rocks than to TTGs. From a geodynamic point of
 929 view, the continental crust is characterised by a low density, allowing it to ‘float’ at the
 930 surface (S. R. Taylor & McLennan, 2009). Considering our scenario for the evolution of
 931 the Terra Cimmeria/Sirenum province, the region may be composed of differentiated rocks,
 932 basalts and mafic residues at the base of the crust. Differentiated rocks are less dense
 933 than basalt, but mafic residues, that are much more voluminous, are denser. The total
 934 density of the crust changes little by the process of differentiation and cannot by itself
 935 generate a low-density crust. On Earth, in absence of orogen, the maximum thickness
 936 of the continental crust is ~ 40 km (Laske et al., 2013). This, together with the rather
 937 low continental crust density, is explained by the loss of dense mafic residues, that be-
 938 come dynamically unstable, because denser than the mantle (Jull & Kelemen, 2001) at
 939 pressures characteristics of the base of the Earth’s crust. These dense mafic residues could
 940 sink back to the mantle as the lithosphere was not strong enough to hold them (Jaupart
 941 et al., 2018). By losing these mafic roots, the bulk density of the continental crust is largely
 942 reduced. In this study, we demonstrated that mafic residues could form in thick crustal
 943 regions on Mars. Whether these mafic residues could be lost is an open question. Since
 944 lid thickening is rapid on a small planet like Mars, which prevents crustal recycling, dif-
 945 ferentiation should then occur very early, which is possible, as shown in this study (Fig-
 946 ure 8). A low-density crustal component could thus form through crustal differentiation
 947 and extraction of evolved melts in provinces of thick crust. This low-density component
 948 would however be offset by large and dense mafic roots in the lower crusts, if these residues
 949 remain in the crust. However, gravity data being more sensitive to shallower layers, the
 950 low densities found in the Highlands are probably more representative of the upper lay-
 951 ers of the crust than of its bulk properties and does not provide any evidence for the loss
 952 of mafic residues (Pauer & Breuer, 2008; Goossens et al., 2017).

953 7 Conclusion

954 We investigated the possibility that differentiated rocks observed in the Martian
 955 Highlands were formed during crust construction, by fractional crystallisation of a basaltic
 956 crust. To enable fractional crystallisation, part of the crust must be maintained above

957 its solidus temperature so that magma can evolve in composition before being extracted
 958 to form differentiated rocks. We show that this mechanism is possible at the base of the
 959 Martian Highlands, at the scale of an hemisphere, and given the constraints we have on
 960 Mars' crustal thickness. Thicker crusts lead to higher temperatures at the Moho. Pres-
 961 sures characteristics of the base of thick crusts on Mars also enable a significant quan-
 962 tity of water to be dissolved in the melt which significantly reduces the solidus. We demon-
 963 strate that the combined effects of hotter temperatures and a lower solidus, together with
 964 a rather weak mantle rheology, allow to sustain partial melting and crustal differenti-
 965 ation over geological times in the Southern Hemisphere. Using our thermal evolution model
 966 in a Bayesian inversion scheme with constraints on Mars' crustal structure and present-
 967 day thermal state, we find that partial melting of the southern crust during its construc-
 968 tion is a non-negligible possibility. Partial melting of the crust may occur early and over
 969 a short duration, or later and over a prolonged duration. Crustal differentiation can thus
 970 occur in absence of plate tectonics, but seems limited in vertical extent to a fraction of
 971 the crustal thickness. Whether the loss of mafic residues could occur and generate a low
 972 density crust remains an open question.

973 Appendix A Details on the parametric thermal evolution modeling

974 We use a parametric stagnant lid convection model, which considers a well-mixed
 975 convective mantle topped by a conductive lid, where the heat is transported by conduc-
 976 tion (Hauck & Phillips, 2002; Breuer & Spohn, 2006; Morschhauser et al., 2011). We as-
 977 sume a well-mixed mantle characterised by a temperature T_m at its top and an isentropic
 978 temperature profile (Thiriet et al., 2018). We thus neglect lateral temperature variations
 979 that naturally arise in convection flows (J. H. Roberts & Zhong, 2006). We consider, as
 980 in Thiriet et al. (2018) and Bonnet Gibet et al. (2022), a lid separated in two different
 981 hemispheres with different temperature profiles $T(r, t)^{N/S}$, lid thicknesses $D_l^{N/S}$, man-
 982 tle average melt fraction $\phi_a^{N/S}$, crustal thicknesses $D_{cr}^{N/S}$ and crust enrichments in heat-
 983 producing elements compared to bulk silicate Mars $\Lambda_{cr}^{N/S}$, where the subscripts N/S refer
 984 to values for the Northern (N) or Southern Hemisphere (S) respectively. We impose
 985 an initially small hemispherical perturbation ΔD_l^0 in lid thickness to trigger a differ-
 986 ential growth of the crust and lid in between the two hemispheres.

The convective heat flow q_{cm} that controls both the mantle temperature and the
 growth of the lid is parameterised from the Rayleigh number $Ra = \frac{\alpha \rho_m g (T_m - T_l) d^3}{\kappa \eta}$ and
 the boundary layer theory (Turcotte & Schubert, 2002):

$$q_{cm} = k_m \frac{T_m - T_l}{\delta_u} = k_m \frac{\Delta T}{d} \left(\frac{Ra}{Ra_{crit}} \right)^{1/3}, \quad (A1)$$

987 where k_m is the thermal conductivity of the mantle, $d = R_p - R_c - D_l$ the convective
 988 layer thickness, T_l the temperature at the base of the lid (Davaille & Jaupart, 1993; Thiriet
 989 et al., 2019) and Ra_{crit} the critical Rayleigh number. The Rayleigh number depends es-
 990 sentially on the mantle viscosity which follows an Arrhenius law:

$$\eta(T, P) = \eta_0 \exp\left(\frac{A + PV}{RT} - \frac{A + P_0V}{RT_0}\right), \quad (A2)$$

991 where T is temperature, P pressure, η_0 the reference viscosity at the reference temper-
 992 ature $T_0 = 1600$ K and pressure $P_0 = 3$ GPa, R the gas constant, A the activation
 993 energy and V the activation volume. Heat conservation in the mantle and core give their
 994 thermal evolution:

Table A1. Parameter values and description for our model

Parameter	Description	Value	Unit
R_p	Planet radius	3390	km
R_c	Core radius	1825	km
f	Lowlands area fraction	0.41	
ρ_c	Core density	6200	kg m ⁻³
ρ_p	Primordial mantle density	3472	kg m ⁻³
ρ_{cr}	Crustal density	2550 to 3150	kg m ⁻³
k_{cr}	Crustal thermal conductivity	2 to 4	W m ⁻¹ K ⁻¹
k_m	Mantle thermal conductivity	4	W m ⁻¹ K ⁻¹
c_c	Core Heat capacity	840	J K ⁻¹ kg ⁻¹
c_{cr}	Crust Heat capacity	1000	J K ⁻¹ kg ⁻¹
c_m	Mantle Heat capacity	1142	J K ⁻¹ kg ⁻¹
α_m	Thermal expansion coefficient	2.5×10^{-5}	K ⁻¹
L_m	Latent Heat of mantle crystallization	5×10^5	J kg ⁻¹
L_{cr}	Latent Heat of crust crystallization	3×10^5	J kg ⁻¹
D_i	Partition coefficient	0.01	
ρ_{liq}^0	Magma density at 0 GPa	2600	kg m ⁻³
χ	Isothermal compressibility	0.04	GPa ⁻¹
f_{mag}	Magmatism fraction	0 to 1	
f_{base}	Basal magmatism fraction	0 to 1	
g_u	Surface gravity	3.7	m s ⁻²
g_c	Core-Mantle boundary gravity	3.4	m s ⁻²
ϵ_c	Ratio of the mean to upper core temperature	1.1	
P_0	Reference pressure	3	GPa
T_0	Reference temperature	1600	K
A	Activation energy	250 to 400	kJ mol ⁻¹
a_{rh}	Rheological coefficient	2.54	
R	Gas constant	8.314462	J mol ⁻¹ K ⁻¹
η_0	Reference viscosity	10^{19} to 10^{22}	Pa s
V	Activation volume	0 to 8	cm ³
β_u	Upper boundary layer exponent	0.335	
β_c	Lower boundary layer exponent	1/3	
Ra_{crit}^u	Upper critical Rayleigh number	450	
k_0	Mantle reference permeability	10^{-12} to 10^{-7}	m ²
η_l	Melt viscosity	1	Pa s
ϕ_c	Critical melt fraction	0.02	
D_{ref}	Crust thickness corresponding to 20% of silicate volume	191	km
ΔT_{sol}	Increase in solidus for a crust thickness D_{ref}	150	K
$X_{H_2O}^p$	Primordial mantle water content	0.00 to 0.05	%wt H ₂ O
D_l^0	initial lid thickness	20 to 200	km
D_{cr}^0	initial crust thickness	4	km
T_s	Surface Temperature	220	K
T_m^0	Initial upper mantle temperature	1625 to 1750	K
ΔT_c^0	Initial superheating of the core	150	K
Λ_{cr}^0	Initial enrichment of the crust	10	
ΔD_l^0	Initial N-S difference in lid thickness	0.5 to 12	km

$$\rho_m c_m V_{cm} \epsilon_m (St + 1) \frac{dT_m}{dt} = - \sum^{N/S} \left(q_{cr}^{N/S} + q_{cm}^{N/S} \right) A_{cm}^{N/S} + q_c A_c + H_{cm} V_{cm}, \quad (\text{A3})$$

$$\rho_c c_c V_c \epsilon_c \frac{dT_c}{dt} = -q_c A_c, \quad (\text{A4})$$

995 where ρ_m is the mantle density, c_m the mantle heat capacity, V_{cm} the volume of
 996 the convective mantle, $St = \frac{L_m V_\phi}{c_m V_{cm}} \frac{d\phi_a}{dT_m}$ the time-dependent Stefan number, ϵ_m the ra-
 997 tio between the average temperature of the convective mantle and the temperature at
 998 the top, $q_{cr}^{N/S}$ the heat flux caused by melt extraction, q_c the heat flux at the core-mantle
 999 boundary, A_c the surface of the core-mantle Boundary, H_{cm} the mantle internal heat-
 1000 ing. Initially, a temperature at the top T_m^0 of the convective mantle and the lid thick-
 1001 ness D_l^0 are prescribed (see Section 4.2). The core is considered to be superheated ini-
 1002 tially by ΔT_c^0 due to core formation and associated dissipation of gravitational poten-
 1003 tial energy (Breuer & Spohn, 2003). The initial Core-Mantle boundary temperature is
 1004 given by $T_c^0 = T_m^0 + \frac{\alpha g T_m^0}{c_m} (R_l^0 - R_c) + \Delta T_c^0$. The evolution of the lid thickness is then
 1005 determined from a heat balance at the interface between the lid and the convective man-
 1006 tle:

$$\rho_m \left(c_m (T_m - T_l) + L \phi_a^{N/S} \right) \left(\frac{dD_l^{N/S}}{dt} - w^{N/S} \right) = -q_{cm}^{N/S} - k_m \left. \frac{\partial T}{\partial r} \right|_{r=R_l}^{N/S}, \quad (\text{A5})$$

1007 where L is the latent heat of crystallisation, w the melt extraction rate and $\left. \frac{\partial T}{\partial r} \right|_{r=R_l}^{N/S}$ the
 1008 temperature gradient at the base of the lid. The rate of crustal extraction depends on
 1009 the melt percolation rate in the partially molten layer of the convective mantle and may
 1010 differ in between both hemispheres (McKenzie, 1985; Richter & McKenzie, 1984):

$$\frac{dD_{cr}^{N/S}}{dt} = w^{N/S} \left(\frac{R_l^{N/S}}{R_{cr}^{N/S}} \right)^2 = \left[\frac{k_0 \phi_{\text{eff}}^3 \Delta \rho g u}{\eta} (1 - \phi_{\text{eff}}) \left(\frac{R_l}{R_{cr}} \right)^2 \right]^{N/S}, \quad (\text{A6})$$

1011 where k_0 is a reference permeability for the host rocks (Miller et al., 2014), ϕ_{eff} the ef-
 1012 fective average melt fraction of the partially molten zone (Bonnet Gibet et al., 2022),
 1013 η the melt viscosity, $\Delta \rho = \rho_m - \rho_0^{\text{liq}} (1 + \chi P)$ the melt-host rock density difference ac-
 1014 counting for melt compressibility $\chi = \frac{1}{\rho_0^{\text{liq}}} \frac{\partial \rho}{\partial P}$. The enrichment in heat-producing ele-
 1015 ments and water of the liquid forming the crust is obtained by considering a chemical
 1016 equilibrium and the same partition coefficient D_i for all heat-producing elements and
 1017 water. Conservation of the amount of radio elements and water give the evolution of their
 1018 concentrations in the crust and mantle.

1019 Open Research Section

1020 The data production and post-processing software used in this study, as well as the
 1021 data, can be accessed at the following link: <https://zenodo.org/records/11203205>.
 1022 The data production software will be updated at the following GitHub page : [https://](https://github.com/ValentinBonnetGibet/1PIECE---1D-Planetary-Interior-Evolution-with-Crust-Extraction)
 1023 [github.com/ValentinBonnetGibet/1PIECE---1D-Planetary-Interior-Evolution-with-](https://github.com/ValentinBonnetGibet/1PIECE---1D-Planetary-Interior-Evolution-with-Crust-Extraction)
 1024 [-Crust-Extraction](https://github.com/ValentinBonnetGibet/1PIECE---1D-Planetary-Interior-Evolution-with-Crust-Extraction)

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 1031 XXX.

1032 References

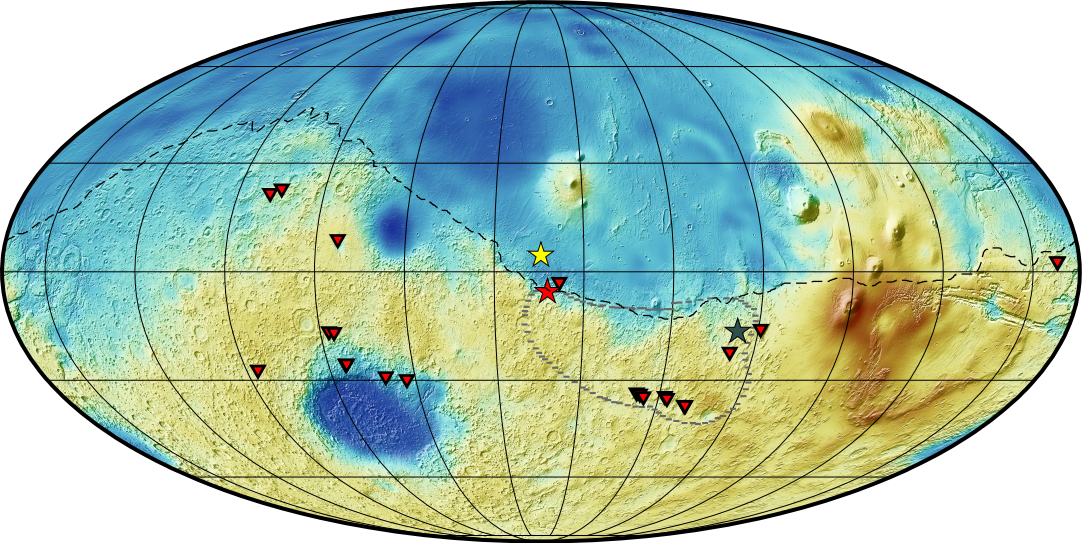
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Crustal thickness (km)