

A disturbing view of life history evolution

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29

30 **Abstract**

31 Species' lifetime schedules of survival, growth and reproduction generally assort
32 along a principal axis called the "fast-slow" continuum, with positions attributed to the
33 value of producing many, fragile offspring early, versus few, high-quality offspring
34 later. Fast species are classically associated with surplus or pulsed resources, and
35 slow species with stable, limiting resources. Here we demonstrate that the fast-slow
36 continuum emerges as a zone of highest fitness in the face of random, structured
37 demographic disturbances, regardless of resource supply, competition, or life history
38 trade-offs. Our resilience framework measures resistance, recovery, and fitness of
39 stage-structured life histories in disturbed environments. Random disturbances
40 favour either fast or slow life history variants due to their respective weak resistance
41 and fast recovery, or strong resistance and slow recovery. Demographic disturbance
42 regimes are important in shaping nature's diversity of life histories, and the resilience
43 framework is a useful tool for understanding species' responses to environmental
44 change.

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50 **Introduction**

51 The life history of any individual organism is its lifetime schedule of survival, growth
52 and reproduction; the life history of a genotype, population or species is summarised
53 as statistics describing the expected lifetime schedule of its constituent members
54 (Stearns 1998). Life history associates with fitness, because natural selection
55 favours schedules of survival and reproduction that maximise numerical
56 representation in future generations. Life histories also associate with ecological
57 features of species, including extinction risk (Purvis *et al.* 2000, Hutchings *et al.*
58 2012), invasiveness (Hamilton *et al.* 2005, Jelbert *et al.* 2015), crop yields (Mifflin
59 2000) and ecosystem function (Jeppesen *et al.* 2010, Adler *et al.* 2014). For these
60 reasons, a great deal of effort has been invested in understanding the diversity of life
61 histories found in nature. Prevailing schools of thought have converged on theory
62 and observation that collapses most life history variation along a principal axis of
63 variation, from “fast” to “slow” (Stearns 1983, Franco and Silvertown 1996, Salguero-
64 Gómez *et al.* 2016). Secondary axes of variation are observed in several broad taxa
65 (Bielby *et al.* 2007, Salguero-Gómez *et al.* 2016), but to date, theory and observation
66 agree on the features of the main axis. Fast species invest in rapid maturation and
67 the production of large numbers of offspring, at the expense of survival and somatic
68 maintenance. Slow species invest in survival and maintenance, producing small
69 numbers of offspring that tend to survive.

70 Formal theory explains the fast-slow continuum in terms of selection pressures
71 acting on the timing and magnitude of reproductive output (Stearns 1998), coupled
72 with presumed trade-offs between maintenance and reproduction (Stearns 1983). In
73 stable environments, investment in survival and self-maintenance, at the expense of
74 early reproduction, can be favoured if it results in increased lifetime reproductive

75 output (Cole 1954, Gadgil and Bossert 1970, Bell 1980, Roff 1981). If the population
76 is growing, this increase must also exceed the inflationary costs of delayed
77 reproduction (future offspring will be worth less, per capita, than current ones).

78 Furthermore, when adults survive better than juveniles, iteroparity (the repeated
79 production of offspring through an extended reproductive lifespan) is favoured over
80 semelparity (single-bout or “big bang” reproduction, followed by death) (Gadgil and
81 Bossert 1970, Charnov and Schaffer 1973, Stearns 1998).

82 A recent synthesis (Wright *et al.* 2019), which aligns fast-slow thinking with classical
83 r-K theory (MacArthur 1962, Boyce 1984, Lande *et al.* 2017), argues that the relative
84 success of fast versus slow life histories is mediated by density-dependent selection,
85 with fast favoured by surplus resources in small populations, and slow favoured
86 under competition for limited resources. This theory aligns well with observation:
87 species like aphids scramble for predictably pulsed resources, reproducing rapidly to
88 maximise fitness during rapid population growth; while elephants invest heavily in
89 survival and somatic maintenance, achieving large body size that helps them
90 compete for limiting but reliable resources, replacing themselves by producing small
91 numbers of high-quality offspring over long lifespans.

92 In environments that offer unpredictable, fluctuating resources, fitness benefits of
93 longer lifespans can be amplified by spreading the risk of reproduction through time
94 (Tuljapurkar 1990), despite the associated costs of somatic maintenance and
95 survival. These benefits are gained because geometric mean fitness increases with
96 arithmetic mean fitness but decreases with its variance (Gillespie 1977). Extreme
97 environmental fluctuations can favour extreme bet-hedging life histories like
98 diapausing egg stages of water fleas and seed dormancy in many plants (Evans and
99 Dennehy 2005), but the adaptive benefits of life-history buffering or lability

100 (McDonald *et al.* 2017) can favour a range of life history strategies in unpredictable
101 environments (Wilbur and Rudolf 2006). In semelparous species (in which
102 reproduction and death coincide), delayed reproduction can be favoured among slow
103 species when fertility varies through time, and among fast species when survival
104 varies (Koons *et al.* 2008).

105 Overall, prevailing wisdom suggests that selection pressures on life-history
106 strategies arrange species along a fast-slow continuum, with their positions
107 depending first on the relationship between age-specific survival, development and
108 reproductive output (Stearns 1998), then on a combination of intensity of competition
109 for limited resources (Wright *et al.* 2019), environmental uncertainty and current
110 position on the fast-slow axis (Koons *et al.* 2008).

111 Here we offer an alternative to that synthesis, proposing instead that random
112 demographic disturbances alone can impose the selection pressures that generate
113 the fast-slow life history continuum in the first place.

114 In stable environments with surplus resources, stage-structured populations settle to
115 a stable stage structure with a stable rate of increase (Caswell 2000). The stable
116 structure and dynamic are determined by stage-specific probabilities of survival and
117 rates of reproduction, i.e. by the vital rates that comprise the organism's life history.
118 Stage-structured disturbances harm different life histories differently (Stott, Townley
119 and Hodgson 2011, White *et al.* 2022, Appendix 1), hence life histories vary in their
120 resistance to disturbance. When demographic disturbances knock populations away
121 from their stable structure, transient dynamics are invoked that differ from the stable
122 rate of increase (Stott *et al.* 2011), hence life histories also vary in their recovery
123 from disturbance (Appendix 2). Resistance and recovery are the two main

124 components of engineering resilience (Holling 1996, Hodgson *et al.* 2015), and here
125 we show that the differential resilience of stage-structured life histories determines
126 the fitness value of fast, slow and other strategies in the face of random, structured,
127 demographic disturbances.

128 **Methods**

129 We consider simple life histories with any possible combination of stage-specific
130 survival and reproduction, subject to the constraint that their fitnesses in undisturbed
131 environments, i.e. their stable rates of increase, are identical. In a stable
132 environment with unlimited resources, these life histories are equally fit. We then
133 subject populations to demographic disturbances that are random in their timing,
134 structure and magnitude, serving as a type of time-varying environmental model
135 (Caswell, 2000). But, our approach to environmental stochasticity differs from
136 prevailing approaches in demographic research. Rather than introduce variation to
137 the stage-dependent rates of survival and reproduction directly in the demographic
138 system defined by the stage-structured projection matrix, we choose instead to
139 implement removals from the population by culling random proportions of individuals
140 from the state vector describing the abundance of each stage. This approach allows
141 us to tease apart the resistance and recovery aspects of population responses
142 (Hodgson *et al.*, 2015). In Supplementary Materials we show that the same
143 outcomes are seen when disturbances are modelled into the demographic system.

144 Our simulation models are in discrete time, and disturbances occur with fixed
145 probability per timestep. Our life histories are described as projection matrices
146 composed of two stages, with four vital rates. In our first scenario, all surviving stage-
147 1 individuals progress to stage-2 at the end of the first timestep, with stage-specific

148 survivals s_1 and s_2 and stage-specific productivities p_1 and p_2 . We call this the
 149 “structured reproduction” model. In our second scenario, we prevent stage-1
 150 individuals from reproducing and introduce a maturation parameter ϕ , the per-
 151 timestep probability of progression from stage-1 to stage-2. We call this the “delayed
 152 maturation” model. In each scenario, three vital rates of the life history are free to
 153 vary while the fourth is constrained by the fixed stable rate of increase, which is the
 154 dominant eigenvalue of the projection matrix, λ_1 . The system is monitored post-
 155 reproductively, such that during any timestep, individuals survive then produce
 156 offspring then are counted. At any timestep and in the absence of disturbance, the
 157 vector of stage-specific abundances, \mathbf{x} , updates according to

$$158 \quad \mathbf{x}_{t+1} = \mathbf{A}\mathbf{x}_t \quad \text{[Equation1]}$$

159 We introduce structured, random disturbance regimes to each scenario, by culling a
 160 random proportion of individuals from each lifestage, with the per-timestep flip of a
 161 weighted coin, f , prior to the processes of survival and reproduction. Extending the
 162 culling algebra of Hauser *et al.* (2006) and the harvesting algebra of Lefkovich
 163 (1967), we define the culling/disturbance matrix \mathbf{C}_t to contain the proportion of each
 164 stage class remaining following disturbance at time t

$$165 \quad \mathbf{C}_t = \begin{bmatrix} c_{1,t} & 0 \\ 0 & c_{2,t} \end{bmatrix} \text{ where } c_{i,t} = \begin{cases} Unif(0,1) & \text{if } Bernoulli(f) = 1 \\ 1 & \text{if } Bernoulli(f) = 0 \end{cases} \quad \text{[Equation2]}$$

166 When exposed to the risk of disturbance, the single timestep projection of the
 167 population vector becomes

$$168 \quad \mathbf{x}_{t+1} = \mathbf{A}\mathbf{C}_t\mathbf{x}_t = \mathbf{A}_t^*\mathbf{x}_t = \begin{bmatrix} a_{1,1}c_{1,t} & a_{1,2}c_{2,t} \\ a_{2,1}c_{1,t} & a_{2,2}c_{2,t} \end{bmatrix} \mathbf{x}_t \quad \text{[Equation 3]}$$

169

170 **Scenario 1: Stage-structured reproduction**

171 Consider a two-lifestage model of juveniles and adults where adults survive with
172 probability $0 < s_2 < 1$ and reproduce with fecundity $0 < p_2$, and where juveniles
173 mature in one timestep with survival $0 < s_1 < 1$ and either cannot reproduce (i.e. $p_1 =$
174 0) or have productivity at the end of their first timestep of life ($0 < p_1 < 2$). We
175 simulated life histories across all feasible combinations of s_1 , s_2 and p_1 that achieved
176 a nominal stable rate of increase of 1.2. This choice of undisturbed fitness value is
177 arbitrary, chosen to keep simulated populations approximately stable in the face of
178 disturbance, but all our findings are robust to different choices. Juvenile and adult
179 survivals were set to span from 0.05 to 1 in increments of 0.05, juvenile productivity
180 to span a sequence from 0 to 2 and adult productivity was calculated from these and
181 the PPM eigenvalue constraint ($\lambda_1 = 1.2$).

182
$$\mathbf{A} = \begin{bmatrix} s_1 p_1 & s_2 p_2 \\ s_1 & s_2 \end{bmatrix} \quad \text{[Equation 4]}$$

183 and the time-varying disturbed projection matrix is

184
$$\mathbf{A}_t^* = \begin{bmatrix} s_1 p_1 c_{1,t} & s_2 p_2 c_{2,t} \\ s_1 c_{1,t} & s_2 c_{2,t} \end{bmatrix} \quad \text{[Equation 5]}$$

185

186 **Scenario 2: Delayed maturation**

187 In this scenario we extend Scenario 1 by introducing a parameter φ governing the
188 probability with which juveniles mature, i.e. transition from stage 1 to stage 2, and by
189 preventing juveniles from reproducing ($p_1 = 0$), sometimes known as ‘coin-flipping
190 maturation’. We simulated life histories across all feasible combinations of s_1 , s_2 , φ
191 and p_2 that achieved the nominal stable rate of increase of 1.2.

192

193
$$\mathbf{A} = \begin{bmatrix} s_1(1 - \varphi) & s_2 p_2 \\ s_1 \varphi & s_2 \end{bmatrix} \quad \text{[Equation 6]}$$

194 And the time-varying disturbed projection matrix is

195
$$\mathbf{A}_t^* = \begin{bmatrix} s_1(1 - \varphi)c_{1,t} & s_2 p_2 c_{2,t} \\ s_1 \varphi c_{1,t} & s_2 c_{2,t} \end{bmatrix} \quad \text{[Equation 7]}$$

196

197 **Realised stochastic dynamics**

198 The abundance of each population at any timepoint is $n_t = \sum x_t$. Over any single
199 timestep, the geometric dynamic of each population is

200
$$\frac{\|x_{t+1}\|}{\|x_t\|} = \frac{\|\mathbf{A}C_t x_t\|}{\|x_t\|} \quad \text{[Equation 8]}$$

201 Where $\|\mathbf{x}\|$ is the one-norm, or column-sum, of the vector \mathbf{x} . This geometric dynamic
202 can be re-expressed as the product of the two main components of resilience:

203 resistance, and recovery. Resistance is the proportion of the current population that
204 survives demographic disturbance ($d_t = \frac{\|C_t x_t\|}{\|x_t\|}$). While all simulated life histories are

205 exposed to disturbances with the same expected value of d_t , it is the relationship
206 between the stable stage structure and the variance in d_t that causes variation in

207 resistance (Appendix 1). The second component of resilience, recovery, has two

208 sub-components: the stable rate of increase λ_1 , and any extra, transient growth or
209 decline caused by deviation from stable stage structure (transient reactivity, $a_t =$

210 $\frac{\|\mathbf{A}C_t x_t\|}{\lambda_1 \|C_t x_t\|}$ (Stott *et al* 2011)). We show the association between life-history parameters,

211 disturbed stage structure, and reactivity, in Appendix 2.

212 During a single timestep, the geometric change in abundance of a disturbed
 213 population can be expanded to describe the distinct processes of resistance and
 214 both stable and transient recovery:

$$215 \frac{\|x_{t+1}\|}{\|x_t\|} = \frac{\|AC_t x_t\|}{\|x_t\|} = \frac{\|C_t x_t\|}{\|x_t\|} \cdot \lambda_1 \cdot \frac{\|AC_t x_t\|}{\|C_t x_t\| \lambda_1} = d_t \lambda_1 a_t \quad \text{[Equation 9]}$$

216 Over multiple timesteps (T), the long-term stochastic rate of increase (λ_s , AKA
 217 fitness) is estimated as the geometric average of the temporal product of this
 218 product.

$$219 \hat{\lambda}_s = \left(\prod_{t=1}^T d_t \lambda_1 a_t \right)^{\frac{1}{T}} \quad \text{[Equation 10]}$$

220 Taking logs and denoting \hat{r}_s as our estimator of $\log(\lambda_s)$,

$$221 \hat{r}_s = \frac{\sum_{t=1}^T (\log(d_t) + \log(\lambda_1) + \log(a_t))}{T} = \frac{\log(n_T/n_0)}{T} \quad \text{[Equation 11]}$$

222 In each modelling scenario, we create life histories that span all possible
 223 combinations of stage-specific survival, productivity and /or maturation that, in the
 224 absence of disturbance, achieve a stable rate of increase of 1.2. We project each of
 225 these life histories from a starting density of 1, and initial structure equal to the stable
 226 stage structure (dominant right eigenvector) of the life history, for 1000 timesteps,
 227 disturbing each timestep with a probability of $f = 0.2$. We monitor \mathbf{x} , and therefore n ,
 228 per timestep for each projection. We replicate projections for each life history 100
 229 times. All results are robust to lengthening the duration of simulations (tested up to
 230 100,000 timesteps). All visualisations of stochastic fitness, resistance and recovery,
 231 are among-replicate averages of per-timestep averages of log-transformed rates of
 232 increase or decline.

233 Results are visualised using two-dimensional heatmaps, coloured by measurements
234 of average recovery, resistance and stochastic growth rate \hat{r}_s , over all viable
235 combinations of s_1 , s_2 , p_1 , p_2 and φ . Only two of the four parameters can appear on
236 the bivariate axes, hence we describe a third parameter using panels, and use
237 contours for the fourth (noting that each model includes a parameter constrained by
238 constant λ_1). Plot shading is a purple-to-green gradient to indicate the magnitude of
239 recovery, resistance or the stochastic growth rate from values low-to-high.

240 In Supplementary Materials we show that the same patterns in stochastic fitness are
241 seen when disturbances are modelled into the demographic system (Equations 5
242 and 7).

243 **Results**

244 **Model 1: Stage-structured productivity**

245 This scenario introduces a constraint on parameter space because when $s_1 p_1$
246 exceeds 1.2, $\lambda_1 > 1.2$ so the nominal stable rate of increase is exceeded by the first
247 lifestage alone. This constraint is seen as white space in the third row of panels in
248 Figure 1, i.e. for large values of p_1 . We simulated life histories across all feasible
249 combinations of s_1 , s_2 , p_1 and p_2 that achieved the nominal stable rate of increase of
250 1.2.

251 [Figure 1 HERE]

252 With increasing magnitude of yearling productivity, the zone of highest fitness shifts
253 from a simple negative association between productivity and juvenile survival, to a
254 more generalised negative association between productivity and survival (Figure 1).
255 Highest fitness occurs along a ridge of increasing survival probabilities, with an
256 associated decline in productivity, very much resembling the fast-slow continuum.
257 Highest fitness is enjoyed by life histories with relatively high survival and moderate
258 yearling productivity, and lowest fitness is suffered by life histories with very different
259 yearling and adult rates of survival.

260

261 [Figure 2 HERE]

262 [Figure 3 HERE]

263

264 The patterns in fitness shown in Figure 1 are explained by associated patterns in
265 resistance to, and recovery from, random demographic disturbances (Figures 2 and
266 3). Resistance is maximised along a ridge of negative association between yearling
267 survival and adult survival, and for intermediate magnitudes of yearling productivity,
268 this ridge lies along a contour of equal adult productivity. Recovery shows a very
269 different saddle-shaped pattern with high rates of recovery among the fastest and
270 slowest life histories and low rates of recovery for life histories with divergent stage-
271 specific rates of survival. The combined effect of resistance and recovery yields the
272 emergent patterns of stochastic growth in Figure 1.

273 In the special case where juvenile productivity is set to zero (i.e. juveniles are
274 prevented from reproducing), demographic disturbance favours an optimal rate of
275 adult survival, regardless of values of juvenile survival and adult productivity (top-left
276 panel in Figure 1). The contours of productivity reveal a negative association with

277 juvenile survival along this ridge of highest fitness, implying a simple trade-off
278 between the quality and quantity of juveniles. Underpinning this pattern is a clear
279 negative association between the resistance of life histories to random disturbance
280 regimes (top-left panel Figure 2), and rate of recovery from them (top-left panel
281 Figure 3). Highest resistance lies along a ridge described by intermediate
282 productivity and a negative association between adult survival and juvenile survival.
283 Highest rates of recovery, meanwhile, are enjoyed by life histories with very low
284 rates of juvenile survival, low-medium adult survival and medium-high productivity.

285 **Model 2: Delayed Maturation**

286 In this delayed-maturation model, demographic disturbances favour relatively low
287 rates of maturation, and hence delayed reproduction, surrounded by a zone of high
288 fitness resembling the fast-slow continuum, i.e. a negative association between rates
289 of survival and of productivity (Figure 4). For high rates of maturation, the fitness
290 patterns move towards the special case of zero juvenile productivity in Scenario 1,
291 favouring moderate values of adult survival and a negative association between
292 productivity and juvenile survival, but with one key difference: high juvenile survival
293 and low productivity is favoured.

294 [Figure 4 HERE]

295 [Figure 5 HERE]

296 [Figure 6 HERE]

297 Patterns of resistance and recovery, for the delayed-maturation scenario, explain the
298 observed patterns in fitness across the simulated life histories. Resistance is low
299 among life histories that mature slowly, then is maximised along a ridge of negative
300 association between juvenile survival and adult survival, with intermediate

301 magnitudes of productivity (Figure 5). Recovery is fastest among slow-maturing life
302 histories, but as maturation rate increases, the life histories that achieve slowest
303 recovery change from those with high juvenile survival to those with low juvenile
304 survival (Figure 6).

305

306 **Discussion**

307 Using two simple life history scenarios, we have shown that the introduction of
308 random, stage-structured disturbances, changes flat fitness surfaces into landscapes
309 that favour an axis of life history variation closely resembling the fast-slow
310 continuum. Generally, fast life histories that favour productivity and rapid maturation
311 over survival, have weak resistance to unpredictable disturbances, but recover
312 quickly. Meanwhile, slow life histories that favour survival over productivity and rapid
313 maturation, are resistant to disturbances but recover slowly. Fitness, which
314 integrates across resistance and recovery, is maximised for life histories along the
315 fast-slow axis. Fundamentally, there is no need for differences among species in the
316 frequency, intensity or structure of demographic disturbances to place those species
317 along the fast-slow continuum: the continuum itself emerges as a contour of equal
318 fitness in the face of stochastic disturbances. There is also no need for differences
319 among species in the supply of resources or the ability to compete for them.

320 Life histories that deviate from this emergent fast-slow axis, for example by having
321 very different rates of adult and juvenile survival, tend to perform badly in the face of
322 random disturbances. On face value this is surprising because, in nature, variation in
323 survival, among ages or stages, is prevalent. A simple explanation for natural
324 patterns of age-structured mortality is the typical ontogeny of increasing size with

325 maturation – physical constraints require offspring to be smaller than their mothers,
326 and survival often scales allometrically with size (Promislow 1993) – but other
327 explanations for differences in age-specific survival might include the actual
328 structure, amplitude and frequency of demographic disturbances experienced in
329 nature (White *et al.* 2022). Perhaps natural disturbance regimes favour the
330 production of atypically fragile (altricial) or robust (precocious) offspring. We note that
331 a special case of both our modelling scenarios, when juveniles cannot reproduce
332 and all individuals mature at the same age, favours a trade-off between productivity
333 and juvenile survival and hence a dissociation of age-specific rates of survival. For
334 this special case, further work is required to explain the observation that random
335 disturbances favour a fixed adult survival, regardless of the values of juvenile
336 survival and productivity.

337 When productivity is introduced for stage-1 individuals, the fitness value of survival
338 rates in the two stages become aligned, and it is this lifetime survival rate that trades
339 off against productivity to form the fast-slow continuum. This pattern is governed by
340 opposing patterns of resistance and recovery, across life histories. The saddle-
341 shaped recovery surface, highest for both high-productivity, low survival and for low
342 productivity, high survival life histories, deserves further study. If stochastic fitness is
343 linked strongly to rates of recovery, then this saddle-shape could describe divergent
344 selection along the fast-slow continuum.

345 When we introduce variation in the rate of maturation, we find that the fast-slow axis
346 is governed mainly by weak resistance but strong recovery in slow-maturing life
347 histories and vice versa for fast-maturing life histories, while subtle variations in
348 these patterns yield a ridge of highest fitness along the fast-slow continuum. The
349 alignment of adult and juvenile survival, along this ridge, weakens as the rate of

350 maturation increases, however high rates of maturation have relatively low fitness,
351 implying that stochastic disturbance is sufficient to favour delayed reproduction. If all
352 juveniles mature in their first timestep, we return to the simple scenario that favours a
353 negative association between quantity and quality of offspring.

354 Beyond this demonstration that random demographic disturbances can select for the
355 fast-slow axis of life history variation, the resilience framework (Hodgson *et al.* 2015,
356 Capdevila *et al.* 2020) has great potential for more detailed and mechanistic
357 understanding of real-world life histories in disturbed environments. All natural
358 populations have vital rates of survival and reproduction that vary through time, and
359 it is not unusual for populations to be affected by structured demographic
360 disturbances like fire (Caswell and Kaye 2001), flood (Smith *et al.* 2005), extreme
361 weather (Abernathy *et al.* 2019), cull (Lachish *et al.* 2010) or epidemic (Benhaiem *et*
362 *al.* 2018). Typically this variation is modelled using projection models containing age-
363 or stage-specific vital rates that vary through time or among environments (Boyce *et*
364 *al.* 2006, Tuljapurkar 2013). Our alternative, i.e. the use of fixed vital rates but with
365 disturbances applied to stage structures, opens the large (and growing) toolbox of
366 transient dynamic analysis (Stott *et al.* 2011), and lends itself to questions around
367 the resistance of structured systems to disturbance regimes, and the subsequent
368 rates of recovery.

369 Resilience in the face of disturbance is an increasingly important feature of natural
370 systems in an era of anthropogenic environmental change (Hodgson *et al.* 2015).
371 Life histories have evolved in disturbed environments since life began, and it is
372 intriguing to observe that random demographic disturbance regimes can favour
373 delayed reproduction, age-structured reproduction and the arrangement of life
374 histories along the fast-slow continuum. Demographic resilience is a clear rival to the

375 classic explanations of why fast- and slow-living species coexist in nature. Natural
376 populations are subject to a variety of structures, amplitudes and frequencies of
377 demographic disturbances and it would be interesting to consider how natural
378 selection has shaped, and will shape, the resilience of genotypes, populations and
379 species to current and future disturbance regimes.

380

381 **References:**

382 Abernathy, H. N., D. A. Crawford, E. P. Garrison, R. Chandler, M. Conner, K. Miller
383 and M. J. Cherry (2019). Deer movement and resource selection during
384 Hurricane Irma, implications for extreme climatic events and wildlife. *Proc.*
385 *Roy. Soc. B* 286(1916), 20192230.

386 Adler, P. B., R. Salguero-Gómez, A. Compagnoni, J. S. Hsu, J. Ray-Mukherjee, C.
387 Mbeau-Ache and M. Franco (2014). Functional traits explain variation in
388 plant life history strategies. *Proc. Nat Acad. Sci.* 111, 740-745.

389 Bell, G. (1980). The costs of reproduction and their consequences. *Am. Nat.* 116, 45-
390 76.

391 Benhaiem, S., L. Marescot, M. L. East, S. Kramer-Schadt, O. Gimenez, J.-D.
392 Lebreton and H. Hofer (2018). Slow recovery from a disease epidemic in the
393 spotted hyena, a keystone social carnivore. *Commun. Biol.* 1, 201.

394 Bielby, J., G. M. Mace, O. R. Bininda-Emonds, M. Cardillo, J. L. Gittleman, K. E.
395 Jones, C. D. L. Orme and A. Purvis (2007). The fast-slow continuum in
396 mammalian life history: an empirical reevaluation. *Am. Nat.* 169, 748-757.

397 Boyce, M. S. (1984). Restitution of gamma-and k-selection as a model of density-
398 dependent natural selection. *Ann. Rev. Ecol Syst.* 15, 427-447.

399 Boyce, M. S., C. V. Haridas, C. T. Lee and N. S. D. W. Group (2006). Demography
400 in an increasingly variable world. *Trends Ecol. Evol.* 21, 141-148.

401 Capdevila, P., I. Stott, M. Beger and R. Salguero-Gómez (2020). Towards a
402 comparative framework of demographic resilience. *Trends Ecol. Evol.* 35,
403 776-786.

404 Caswell, H. (2000). Matrix population models, Sinauer Sunderland, MA.

405 Caswell, H. and T. N. Kaye (2001). Stochastic demography and conservation of an
406 endangered perennial plant (*Lomatium bradshawii*) in a dynamic fire regime.
407 *Adv. Ecol. Res.* 32, 1-51.

408 Charnov, E. L. and W. M. Schaffer (1973). Life-history consequences of natural
409 selection, Cole's result revisited. *Am. Nat.* 107, 791-793.

410 Cole, L. C. (1954). The population consequences of life history phenomena. The
411 *Quart. Rev. Biol.* 29, 103-137.

412 Evans, M. E. and J. J. Dennehy (2005). Germ banking, bet-hedging and variable
413 release from egg and seed dormancy. *Quart. Rev. Biol.* 80, 431-451.

414 Franco, M. and J. Silvertown (1996). Life history variation in plants, an exploration of
415 the fast-slow continuum hypothesis. *Phil. Trans. Roy. Soc. B* 351, 1341-
416 1348.

417 Gadgil, M. and W. H. Bossert (1970). Life historical consequences of natural
418 selection. *Am. Nat.* 104, 1-24.

419 Gillespie, J. H. (1977). Natural selection for variances in offspring numbers, a new
420 evolutionary principle. *Am. Nat* 111, 1010-1014.

421 Hamilton, M. A., B. R. Murray, M. W. Cadotte, G. C. Hose, A. C. Baker, C. J. Harris
422 and D. Licari (2005). Life-history correlates of plant invasiveness at regional
423 and continental scales. *Ecol. Letts.* 8, 1066-1074.

424 Hauser, C., E. Cooch and J.-D. Lebreton (2006). Control of structured populations by
425 harvest. *Ecol. Model.* 196, 462-470.

426 Hodgson, D., J. L. McDonald and D. J. Hosken (2015). What do you mean, 'resilient'?
427 *Trends Ecol. Evol.* 30, 503-506.

428 Holling, C. S. (1996). Engineering resilience versus ecological resilience. In Schulze,
429 P. (Ed.) *Engineering within ecological constraints*. National Academies
430 Press.

431 Hutchings, J. A., R. A. Myers, V. B. García, L. O. Lucifora and A. Kuparinen (2012).
432 Life-history correlates of extinction risk and recovery potential. *Ecol. Appl.*
433 22, 1061-1067.

434 Jelbert, K., I. Stott, R. A. McDonald and D. Hodgson (2015). Invasiveness of plants is
435 predicted by size and fecundity in the native range. *Ecol. Evol.* 5, 1933-1943.

436 Jeppesen, E., M. Meerhoff, K. Holmgren, I. González-Bergonzoni, F. Teixeira-de
437 Mello, S. A. Declerck, L. De Meester, M. Søndergaard, T. L. Lauridsen and
438 R. Bjerring (2010). Impacts of climate warming on lake fish community
439 structure and potential effects on ecosystem function. *Hydrobiol.* 646, 73-90.

440 Koons, D. N., C. J. E. Metcalf and S. Tuljapurkar (2008). Evolution of delayed
441 reproduction in uncertain environments, a life-history perspective. *Am. Nat.*
442 172, 797-805.

443 Lachish, S., H. McCallum, D. Mann, C. E. Pukk and M. E. Jones (2010). Evaluation
444 of selective culling of infected individuals to control Tasmanian devil facial
445 tumor disease. *Cons. Biol.* 24, 841-851.

446 Lande, R., S. Engen and B.-E. Sæther (2017). Evolution of stochastic demography
447 with life history tradeoffs in density-dependent age-structured populations.
448 *Proc. Nat. Acad. Sci.* 114, 11582-11590.

449 Lefkovitch, L. (1967). A theoretical evaluation of population growth after removing
450 individuals from some age groups. *Bull. Ent. Res.* **57**(3), 437-445.

451 MacArthur, R. H. (1962). Some generalized theorems of natural selection. *Proc. Nat.*
452 *Acad. Sci.* **48**, 1893-1897.

453 McDonald, J. L., M. Franco, S. Townley, T. H. Ezard, K. Jelbert and D. J. Hodgson
454 (2017). Divergent demographic strategies of plants in variable environments.
455 *Nature Ecol. Evol.* **1**, 0029.

456 Miflin, B. (2000). Crop improvement in the 21st century. *J. Exp. Bot.* **51**(342), 1-8.

457 Promislow, D. E. (1993). On size and survival, progress and pitfalls in the allometry
458 of life span. *J. Geront.* **48**, B115-B123.

459 Purvis, A., J. L. Gittleman, G. Cowlishaw and G. M. Mace (2000). Predicting
460 extinction risk in declining species. *Proc. Roy. Soc. B* **267**, 1947-1952.

461 Roff, D. (1981). On being the right size. *Am. Nat.* **118**, 405-422.

462 Salguero-Gómez, R., O. R. Jones, E. Jongejans, S. P. Blomberg, D. J. Hodgson, C.
463 Mbeau-Ache, P. A. Zuidema, H. De Kroon and Y. M. Buckley (2016). Fast–
464 slow continuum and reproductive strategies structure plant life-history
465 variation worldwide. *Proc. Nat. Acad. Sci.* **113**, 230-235.

466 Smith, M., H. Caswell and P. Mettler-Cherry (2005). Stochastic flood and
467 precipitation regimes and the population dynamics of a threatened floodplain
468 plant. *Ecol. Appl.* **15**, 1036-1052.

469 Stearns, S. C. (1983). The influence of size and phylogeny on patterns of covariation
470 among life-history traits in the mammals. *Oikos* **41**, 173-187.

471 Stearns, S. C. (1998). *The evolution of life histories*, Oxford university press.

472 Stott, I., S. Townley and D. J. Hodgson (2011). A framework for studying transient
473 dynamics of population projection matrix models. *Ecol. Letts.* **14**, 959-970.

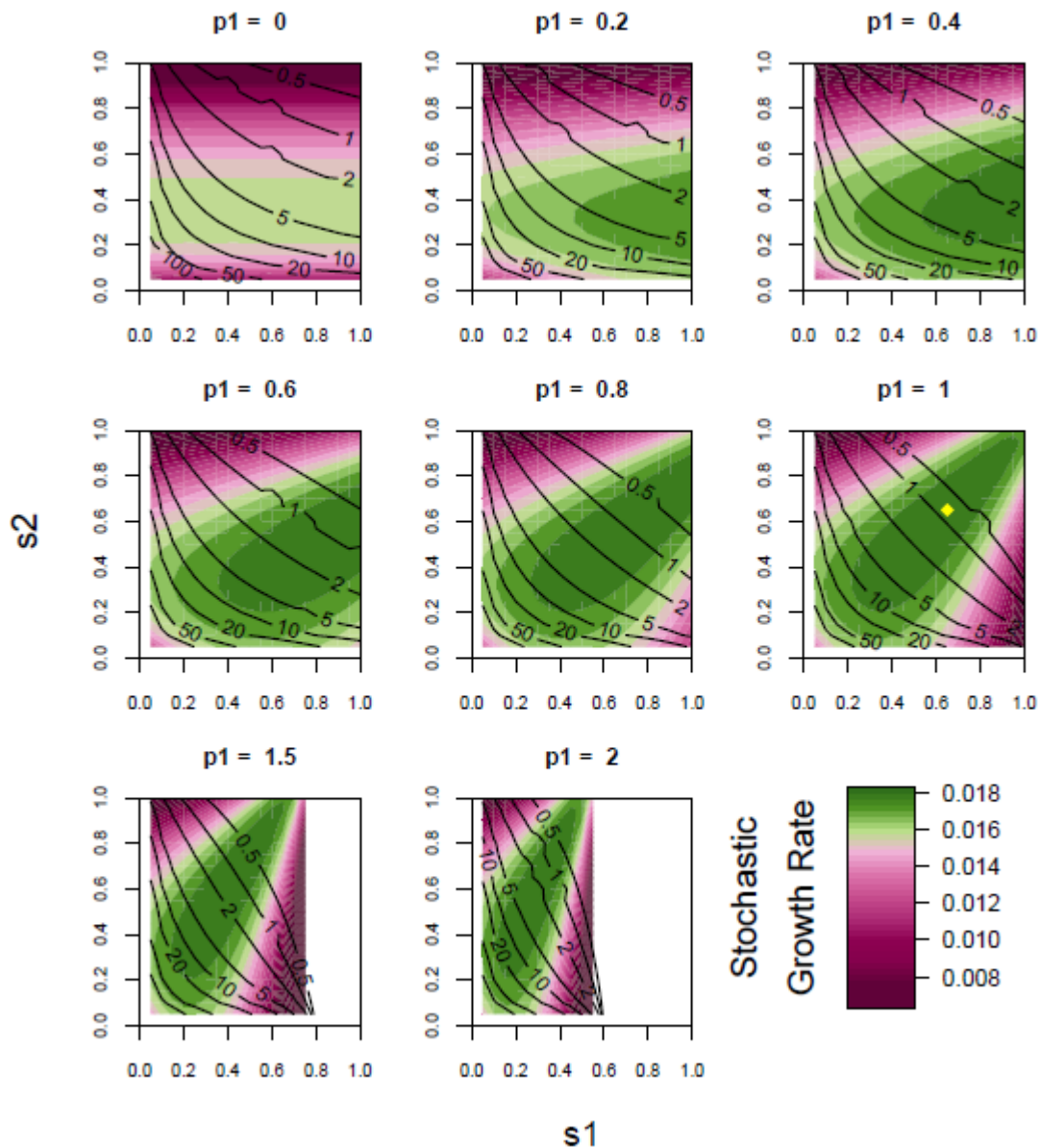
- 474 Tuljapurkar, S. (1990). Delayed reproduction and fitness in variable environments.
475 *Proc. Nat. Acad. Sci.* 87, 1139-1143.
- 476 Tuljapurkar, S. (2013). *Population dynamics in variable environments*, Springer
477 Science & Business Media.
- 478 White, J. W., C. Barceló, A. Hastings and L. W. Botsford (2022). Pulse disturbances
479 in age-structured populations, Life history predicts initial impact and recovery
480 time. *J. Anim. Ecol.* 91, 2370-2383.
- 481 Wilbur, H. M. and V. H. Rudolf (2006). Life-history evolution in uncertain
482 environments, bet hedging in time. *Am. Nat.* 168, 398-411.
- 483 Wright, J., G. H. Bolstad, Y. G. Araya-Ajoy and N. J. Dingemanse (2019). Life-history
484 evolution under fluctuating density-dependent selection and the adaptive
485 alignment of pace-of-life syndromes. *Biol. Rev.* 94, 230-247.
- 486 Young, W. E. and R. H. Trent (1969). Geometric mean approximations of individual
487 security and portfolio performance. *J. Finance Quant. Anal.* 4, 179-199.

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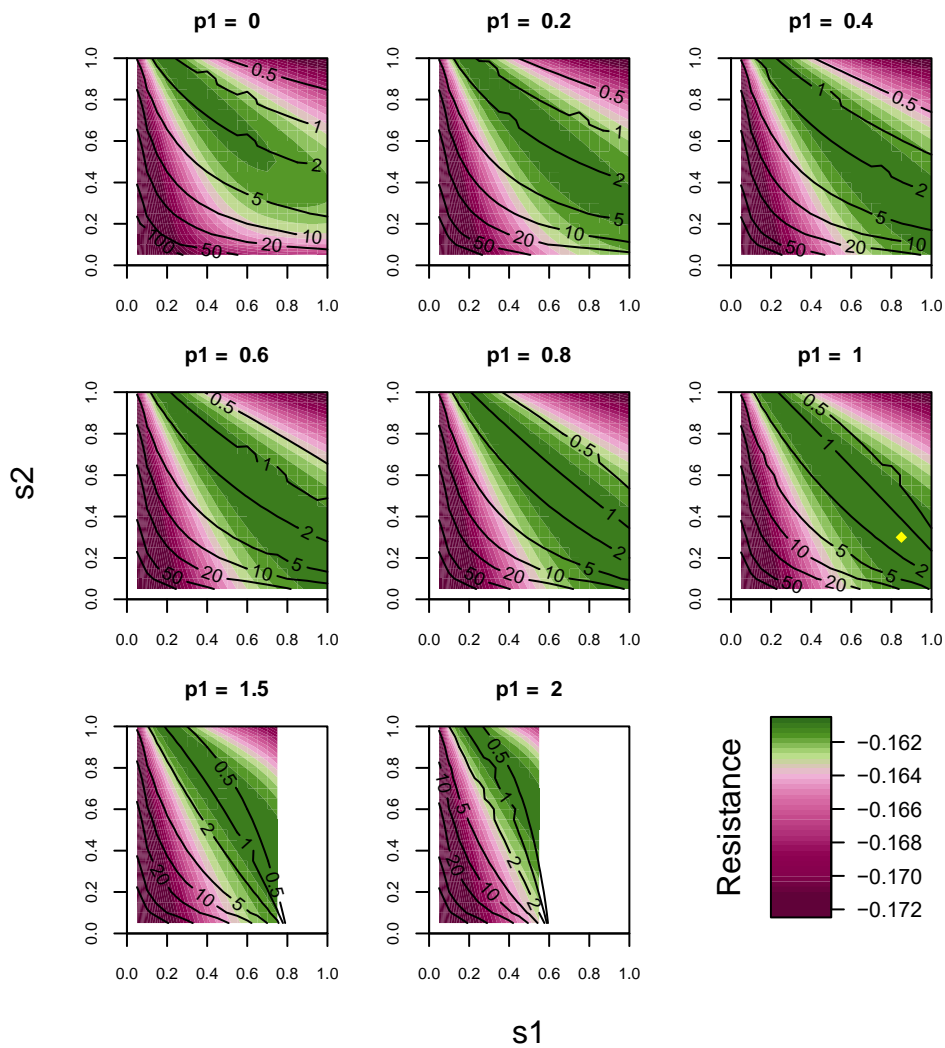
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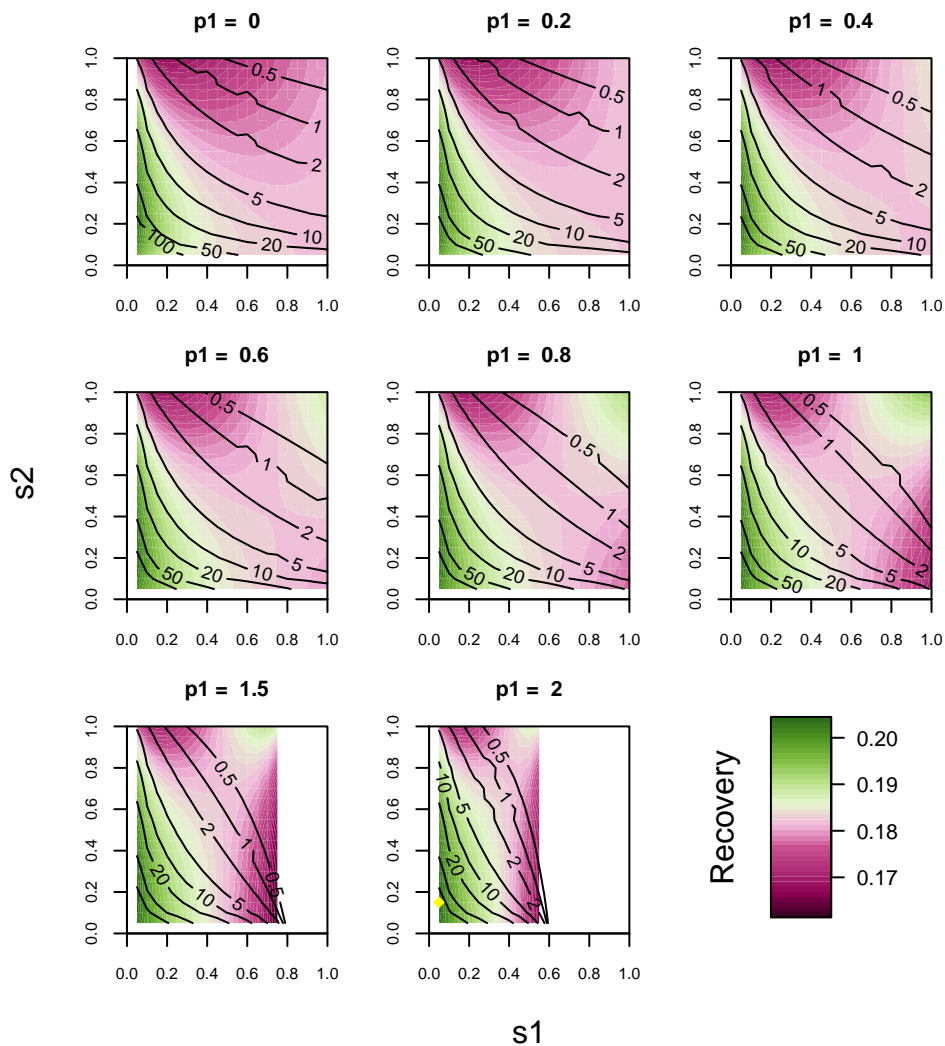
493 **Figure 1:** Heatmaps showing the stochastic growth rates (\hat{r}_s) for combinations of
 494 adult (s_2) and juvenile (s_1) survival, with contours describing adult productivity (p_2)
 495 and panels for different values of juvenile productivity (p_1). All populations disturbed
 496 by stage-specific, Uniform-distributed, proportional culls with per-timestep probability
 497 $f = 0.2$. The yellow diamond symbol represents the maximum parameter combination
 498 over all plots. The areas of block white represent the parameter combinations that
 499 are not biologically feasible ($s_1 p_1 > 1.2$).

500



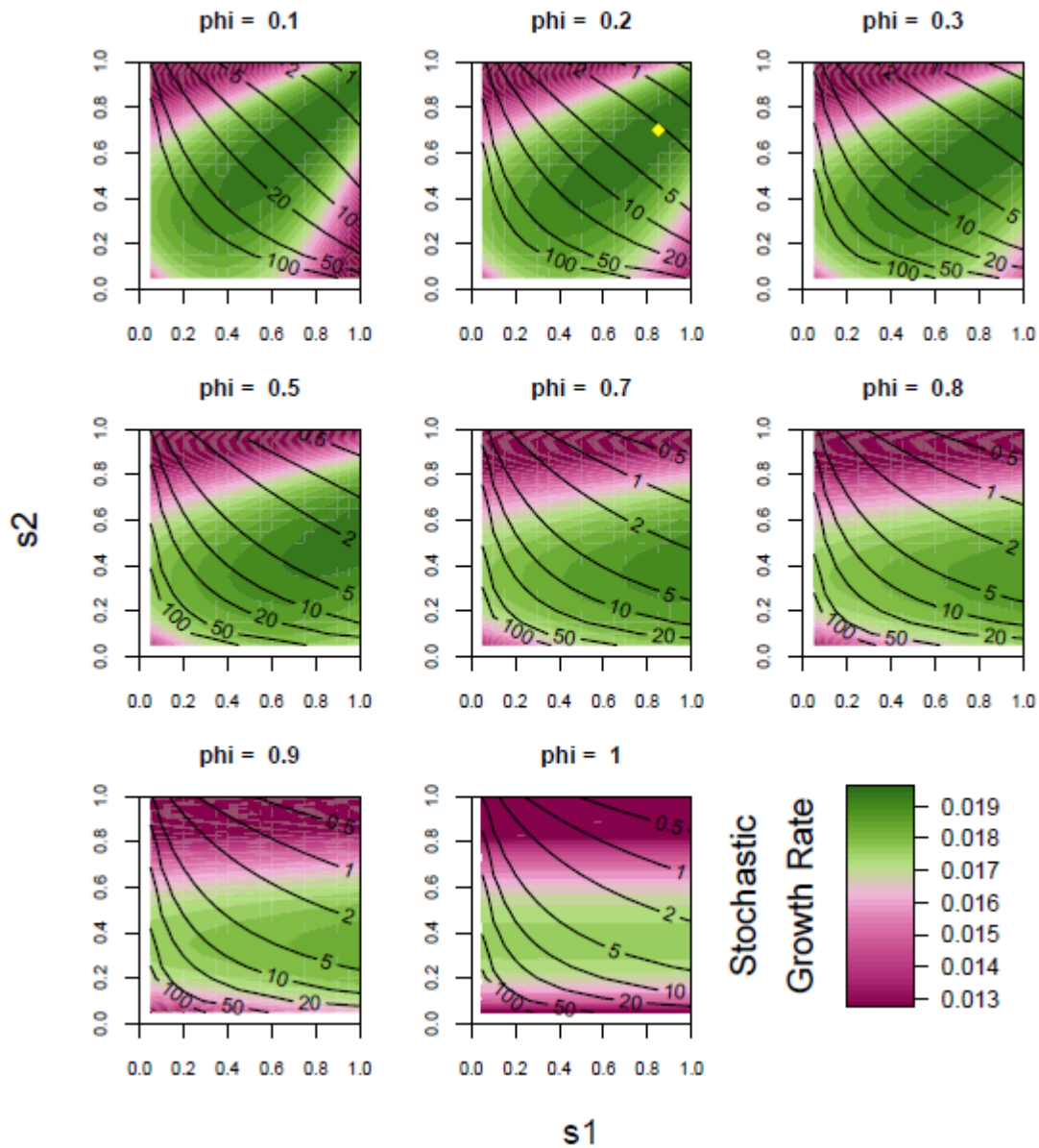
501

502 **Figure 2:** Heatmaps showing demographic resistance, measured as the mean of the
 503 log of the ratio of disturbed to undisturbed population size per timestep, for
 504 combinations of adult (s_2) and juvenile (s_1) survival, with contours describing adult
 505 productivity (p_2) and panels for different values of juvenile productivity (p_1). All
 506 populations disturbed by stage-specific, Uniform-distributed, proportional culls with
 507 per-timestep probability $f = 0.2$. The yellow diamond symbol represents the
 508 maximum parameter combination over all plots.



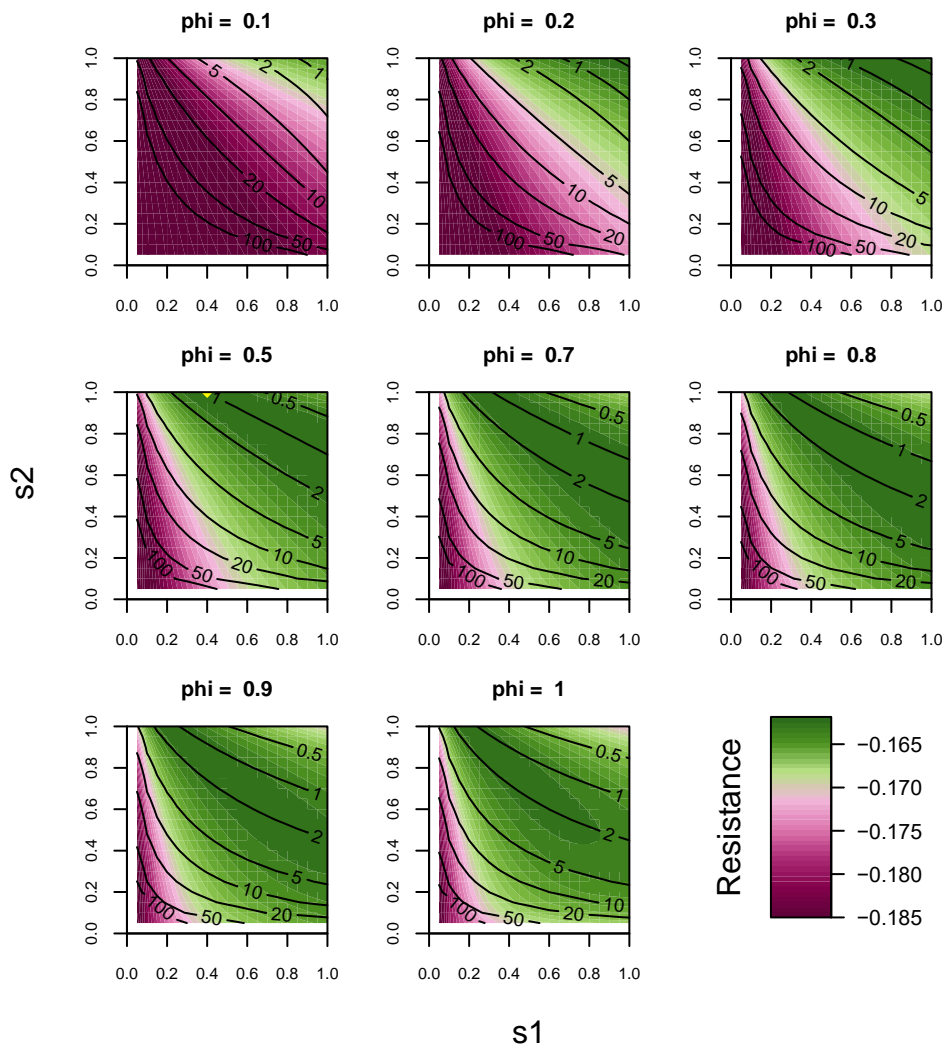
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510 **Figure 3:** Heatmaps showing demographic recovery, measured as the mean of the
 511 log of the ratio of projected to disturbed population size per timestep, for
 512 combinations of adult (s_2) and juvenile (s_1) survival, with contours describing adult
 513 productivity (p_2) and panels for different values of juvenile productivity. All
 514 populations disturbed by stage-specific, Uniform-distributed, proportional culls with
 515 per-timestep probability $f = 0.2$. The yellow diamond symbol represents the
 516 maximum parameter combination over all plots.



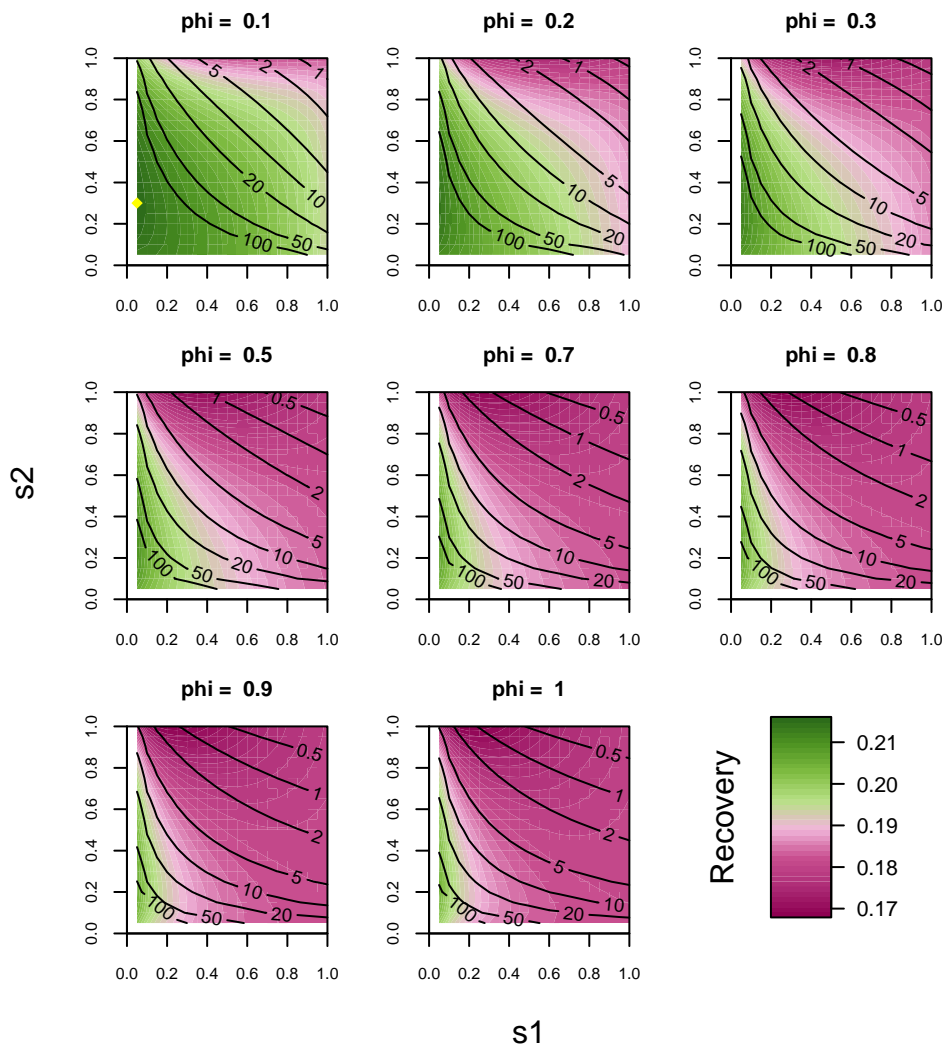
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518 **Figure 4:** Heatmaps showing the stochastic growth rates (\hat{r}_s) for combinations of
 519 adult (s_2) and juvenile (s_1) survival, with contours describing adult productivity (p_2)
 520 and panels for different values of maturation rate (ϕ). All populations disturbed by
 521 stage-specific, Uniform-distributed, proportional culls with per-timestep probability $f =$
 522 0.2. The yellow diamond symbol represents the maximum parameter combination
 523 over all plots.



524

525 **Figure 5:** Heatmaps showing demographic resistance, measured as the mean of the
 526 log of the ratio of disturbed to undisturbed population size per timestep, for
 527 combinations of adult (s_2) and juvenile (s_1) survival, with contours describing adult
 528 productivity (p_2) and panels for different values of maturation rate (ϕ). All populations
 529 disturbed by stage-specific, Uniform-distributed, proportional culls with per-timestep
 530 probability $f = 0.2$. The yellow diamond symbol represents the maximum parameter
 531 combination over all plots.



532

533 **Figure 6:** Heatmaps showing demographic recovery, measured as the mean of the
 534 log of the ratio of projected to disturbed population size per timestep, for
 535 combinations of adult (s_2) and juvenile (s_1) survival, with contours describing adult
 536 productivity (p_2) and panels for different values of maturation rate (ϕ). All populations
 537 disturbed by stage-specific, Uniform-distributed, proportional culls with per-timestep
 538 probability $f = 0.2$. The yellow diamond symbol represents the maximum parameter
 539 combination over all plots.

540

541 **Appendix 1: Why do structured life histories vary in *resistance* to stochastic**
542 **disturbances?**

543 We have modelled stochastic disturbances as the culling of a Uniform-distributed
544 proportion of members of each age/stage class. The population-level impact of
545 disturbance is therefore the sum across all age/stage-classes following their
546 respective culls. This is the sum of two independent samples from Uniform
547 distributions with bounds defined by 0 below and the abundance of each stage,
548 above.

549 If we set $n = x_1 + x_2 = 1$ (i.e. working with relative abundance of each age/stage-
550 class), call the stochastic culls U_1 and U_2 , and their combined impact $Z = U_1 + U_2$, we
551 find the pdf of Z is

552

$$553 \quad f(z) = \begin{cases} \frac{z}{x_1(1-x_1)}, & \text{for } 0 < z < x_1 \\ \frac{1}{(1-x_1)}, & \text{for } x_1 < z < (1-x_1) \\ \frac{1}{(1-x_1)} + \frac{1}{x_1} - \frac{z}{x_1(1-x_1)}, & \text{for } (1-x_1) < z < 1 \end{cases} \quad \text{[Equation A1.1]}$$

554

555 The expected resistance is

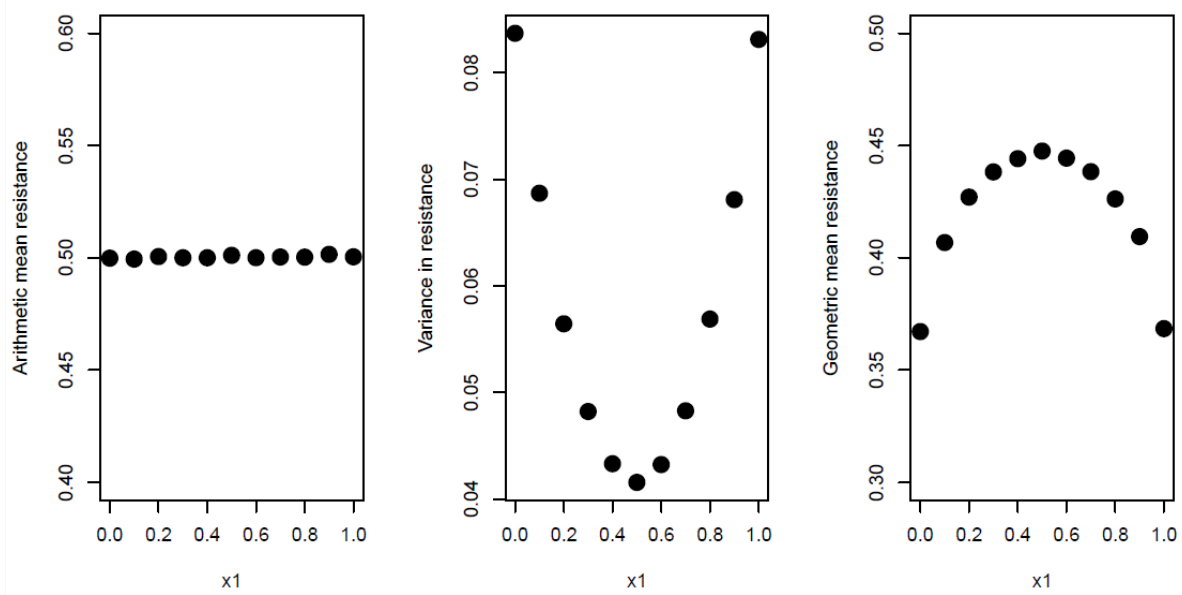
$$556 \quad E(U_1 + U_2) = E(Z) = 0.5 \quad \text{[Equation A1.2]}$$

557 And its variance is

$$558 \quad \text{Var}(Z) = \frac{1}{12} - \frac{x_1}{6} + \frac{x_1^2}{6} \quad \text{[Equation A1.3]}$$

559 Since the expected value of resistance to the combined cull is constant but its
560 variance is quadratic-up in x_1 , the geometric process of multiple culls favours life

561 histories with even relative abundance of each age/stage (Figure A1). Life histories
 562 with stage structures dominated by one stage class, or the other, will be less
 563 resistant to stochastic disturbance. This is because the geometric mean gets smaller
 564 with constant arithmetic mean and increasing arithmetic variance (Young and Trent
 565 1969, Gillespie 1977). Unbalanced stage structures are typical of the asymmetric
 566 projection matrices that describe life histories, hence variation among life histories, in
 567 resistance to stochastic disturbances, is not surprising.



568

569 **Figure A1:** Mean and variance in resistance of 2-stage life histories that vary in the
 570 relative abundance (x_1) of the first lifestage. Resistance defined as the instantaneous
 571 impact on population abundance caused by Uniform-distributed culling of each
 572 lifestage. Means and variances calculated from 100K simulated disturbances.
 573 Arithmetic mean resistance is constant, but variance is quadratic in x_1 , and
 574 geometric mean (measuring the product of repeated disturbances) peaks at $x_1=0.5$,
 575 i.e. is maximised for life histories with even stable stage structure.

576

577 **Appendix 2: Why do structured life histories vary in *recovery* from stochastic**
578 **disturbances?**

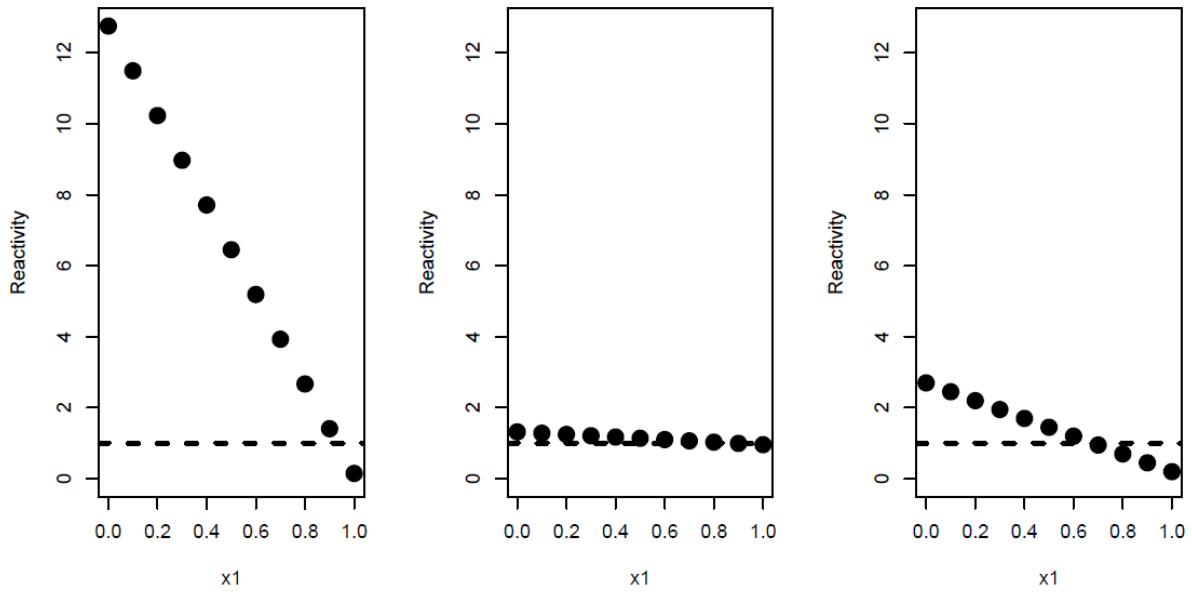
579 When demographic disturbance pushes age/stage structure away from the stable
580 structure, transient dynamics are invoked while the age/structure settles back to
581 stability through time (Stott, Townley and Hodgson 2011). The only stage structure
582 that grows according to the stable rate of increase is the stable structure. All other
583 stage structures attenuate (have growth rate less than the dominant eigenvalue) or
584 amplify (growth rate greater than the dominant eigenvalue) (Figure A2). In the first
585 timestep following disturbance, if **A** is the population projection matrix then
586 abundance will be the 1-norm (sum) of the disturbed stage structure projected
587 through **A**:

$$588 \quad N_{t+1} = \|Ax_t\|_1 \quad \text{[Equation A2.1]}$$

589 And the first-timestep rate of recovery, as a multiplier on the stable rate of increase,
590 also known as *reactivity*, is

$$591 \quad \textit{reactivity} = \frac{\|Ax_t\|_1 / \|x_t\|_1}{\lambda_1(A)} \quad \text{[Equation A2.2]}$$

592 Recovery will be fastest for life histories constituted by stage classes that are
593 particularly highly productive and/or survive well. These are unlikely to resemble the
594 life histories that are most resistant to disturbance by virtue of having evenly
595 distributed stage structures.



596

597 **Figure A2:** First-timestep recovery from stochastic disturbance for stage structures
 598 starting with relative abundance of lifestage 1 (x_1) ranging between 0 and 1, when
 599 projected through (a) a fast life history with $A = \begin{bmatrix} 0.25 & 12.65 \\ 0.1 & 0.1 \end{bmatrix}$; (b) a slow life history
 600 with $A = \begin{bmatrix} 0.16 & 0.52 \\ 0.8 & 0.8 \end{bmatrix}$; (c) a mixed-pace life history with $A = \begin{bmatrix} 0 & 1.8 \\ 0.2 & 0.9 \end{bmatrix}$. All three life
 601 histories have dominant eigenvalue = 1.2, but very different patterns of recovery from
 602 demographic disturbance.

603 Overall we expect a negative association between resistance and recovery, but the
 604 relative strength of these two components of resilience will depend on the structure,
 605 amplitude and frequency of the disturbance regime, and on the life history described
 606 by the projection matrix **A**.

607

608

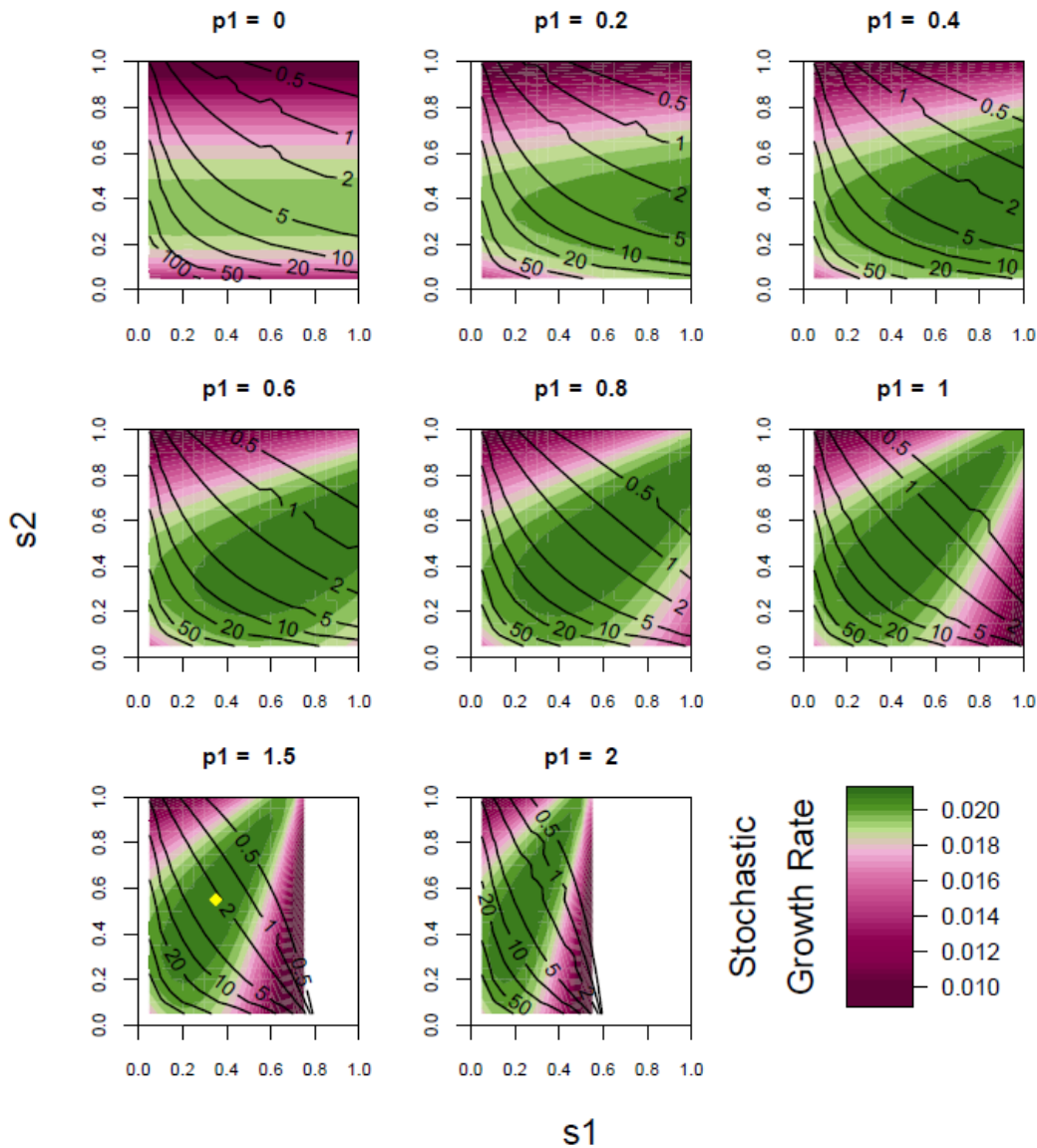
609 Supplementary Material

610 **Modelling random disturbances in the projection matrix A**

611 Our main description, of findings from demographic disturbance simulations, applied
612 disturbances to population state vectors, allowing us to unpack the relative
613 contributions of demographic resistance and demographic recovery to the resulting
614 stochastic population growth rate or fitness. The usual approach, in stage-structured
615 demographic modelling, is to introduce stochasticity into the demographic system
616 model, in other words into the vital rates that form the population projection matrix.

617 According to equations 5 and 7, the outcome of modelling disturbances as culls of
618 the population state vector, versus modelling them as variation in the vital rates in
619 the population projection matrix, should be identical. Here we present the analogous
620 code and figures that display stochastic population growth rates (AKA fitness) of
621 simple life histories exposed to random disturbances of their vital rates, using Model
622 1: Stage-structured Reproduction. The patterns and measurements in the figures are
623 identical (give or take small noise coming from the simulated disturbance regimes) to
624 Figure 1 in the main manuscript.

625 Hence the findings are indeed equivalent to those shown in the main manuscript.
626 But, by disturbing vital rates instead of culling the population state, we are unable to
627 unpack the relative contributions of demographic resistance and demographic
628 recovery, without recourse to the same algebra used in our culling analysis.



629

630 **Figure S1:** Heatmaps showing the stochastic growth rates (\hat{r}_s) for combinations of
 631 adult (s_2) and juvenile (s_1) survival, with contours describing adult productivity (p_2)
 632 and panels for different values of juvenile productivity (p_1), when random
 633 disturbances are modelled to affect vital rates in the projection matrix **A**. All survival
 634 rates disturbed by stage-specific, Uniform-distributed, proportional culls with per-
 635 timestep probability $f = 0.2$. The yellow diamond symbol represents the maximum
 636 parameter combination over all plots. The areas of block white represent the
 637 parameter combinations that are not biologically feasible ($s_1 p_1 > 1.2$).